# Sensitivity of ozone production rate to ozone precursors

Lawrence I. Kleinman, Peter H. Daum, Yin-Nan Lee, Linda J. Nunnermacker, and Stephen R. Springston

Atmospheric Sciences Division, Brookhaven National Laboratory, Upton, New York 11973

Judith Weinstein-Lloyd

Chemistry/Physics Department, SUNY/Old Westbury, Old Westbury, New York 11568

Jochen Rudolph

Chemistry Department and Centre for Atmospheric Research, York University, Toronto, Ontario M3J 1P3, Canada

Abstract. The photochemical equations describing  $O_3$  formation in the lower troposphere contain 2 major sink terms for free radicals; combination reactions and reactions with  $NO_x$ . Knowing the fraction of radicals removed by reactions with  $NO_x$ , termed  $L_N/Q$ , allows one to predict the sensitivity of  $O_3$  production to NO and VOCs. We derive an analytic formula that gives  $L_N/Q$  in terms of readily measured  $O_3$  precursors and test this formula using constrained steady state calculations based on field observations gathered in Phoenix, Arizona. The formula quantifies well-known results regarding the effects of dilution, oxidation, and the production of oxidants on the transition from VOC to  $NO_x$  sensitive behavior as an air parcel is advected away from an urban source.

#### 1. Introduction

Ozone is formed in the lower atmosphere by a sequence of chemical reactions requiring sunlight, NO<sub>x</sub> (NO + NO<sub>2</sub>), and VOCs. Determining the relation between O<sub>3</sub> and its precursors has been the object of more than 4 decades of research [NARSTO, 2000]. It has been found that O<sub>3</sub> formation depends on NO<sub>x</sub> and VOC emissions in a complicated and non-linear way. Several qualitative generalizations are, however, possible. In an urban plume O<sub>3</sub> becomes more VOC sensitive (i.e., more responsive to a change in VOCs) at high NO<sub>x</sub> to VOC ratios and at high absolute concentrations. As an urban plume is advected away from its source it tends to become more dilute and have a lower NO<sub>x</sub> to VOC ratio. For both reasons a plume will evolve in the direction of being VOC sensitive near its source to being NO<sub>x</sub> sensitive far away [Staffelbach et al., 1997; Duncan and Chameides, 1998; Sillman, 1999].

In this article we consider the sensitivity of the rate of  $O_3$  production,  $P(O_3)$ , to changes in atmospheric concentrations of  $NO_x$  and VOCs. This problem is a prerequisite to the more complicated problem of determining the response of  $O_3$  to an emissions change. The behavior of  $P(O_3)$  is a property of an air mass and can be characterized reasonably well by means of chemical measurements. In contrast, a sensitivity to an emissions change is not a local property [Kleinman, 2000]. It

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Paper number 2000GL012597. 0094-8276/01/2000GL012597\$05.00 depends on the entire time history of an air mass and therefore cannot be directly observed, although several indirect techniques are available [Cardelino and Chameides, 1995; Sillman, 1995]. In a general sense, we know that the two problems must be related as O<sub>3</sub> concentration is due to O<sub>3</sub> production occurring over the time history of an air mass.

We showed in a previous study [Kleinman et al., 1997] that the sensitivity of  $P(O_3)$  to NO and VOCs is given by a simple analytic function of  $L_N/Q$ , the fraction of free radicals removed by reactions with  $NO_x$ .  $L_N/Q$  enters our equations from a starting point which is a conservation statement for free radicals (also known as odd-hydrogen and consisting primarily of OH,  $HO_2$ , and  $RO_2$ s). Production of free radicals occurs principally from photolysis reactions. Radicals are removed by two major categories of reactions; combination reactions between radicals, including  $HO_2 + HO_2 \rightarrow H_2O_2$ ; and reactions between radicals and  $NO_x$ , principally  $OH + NO_2 \rightarrow HNO_3$ . The conservation statement for free radicals can be written as,

$$Q = L_R + L_N \tag{1}$$

where Q is the production rate,  $L_R$  is the loss rate due to radicalradical reactions, and  $L_N$  is the loss rate due to all reactions of radicals with  $NO_x$ .

In this study we examine the variable  $L_N/Q$ . We provide an analytic formula that gives  $L_N/Q$  in terms of  $O_3$  precursors. This formula can be used to estimate  $NO_x$  and VOC sensitivity based on readily measured concentrations. From the analytic expression for  $L_N/Q$  it is easy to show how  $NO_x$  and VOC sensitivity depends on the  $NO_x$  to VOC ratio and on absolute concentration.

## 2. Experiment

During the late spring of 1998, the Atmospheric Chemistry Program of DOE in collaboration with the Arizona Department of Environmental Quality conducted a photochemistry field campaign in the Phoenix metropolitan area. The DOE G-1 aircraft was used to sample the atmosphere upwind, over, and downwind of the metropolitan area. Measurements included, O<sub>3</sub>, CO, VOCs, NO, NO<sub>2</sub>, NO<sub>y</sub>, HCHO, H<sub>2</sub>O<sub>2</sub>, organic peroxides, actinic flux, temperature, and dew point. We will use these observations to illustrate and check a series of analytic results that we believe are generally applicable to urban plumes.

Characteristics of the Phoenix air basin during the field campaign were a very low humidity, high temperature and solar

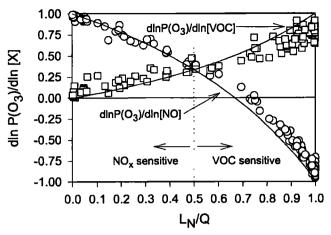


Figure 1. The relative sensitivity of  $O_3$  production rate to [NO] and [VOC], dlnP( $O_3$ )/dln[NO] and dlnP( $O_3$ )/dln[VOC], as a function of the fraction of radicals removed by reactions with NO or NO<sub>2</sub>,  $L_N$ /Q. Symbols are from CSS calculation. Lines are the analytic functions (2) and (3). A value of 1 (-1) for dlnP( $O_3$ )/dln[X] means that an n% increase in [X] produces an n% increase (decrease) in P( $O_3$ ).

insolation, an emissions mixture dominated by transportation sources, and low biogenic emissions. Twenty two flights were conducted with about half of the flight time used for sampling over high emission rate regions. Clean air was observed in the early morning in the nighttime residual layer and later in the day above the convective boundary layer. A wide range of chemical concentrations were encountered. For example NO<sub>x</sub> concentration varied from 70 ppt to 39 ppb, O<sub>3</sub> from 29 to 92 ppb, and CO from a background of about 120 ppb to 470 ppb. Results are presented in greater detail elsewhere [Fast et al., 2000].

## 3. Model

We have applied a constrained steady state (CSS) photochemical box model to the Phoenix observations. This model uses as input the trace gas concentrations (excluding NO<sub>2</sub>) observed from the DOE G-1. The limiting factor in the use of this model is the availability of VOC data which is determined from discrete canister samples. Model predictions include the concentrations of free radicals and NO2 that are in rapid equilibrium with the observed mixture of trace gases. Of particular importance to this study are predictions of the production rate of O<sub>3</sub>, P(O<sub>3</sub>); the formation rate of free radicals, Q; and the rate at which radicals are lost by different reaction pathways, L<sub>N</sub> and L<sub>R</sub>. The kinetic equations in the model are from the chemical mechanisms of Stockwell et al. [1990] and Paulson and Seinfeld [1992]. PAN is not a calculated variable as it is assumed to be in steady state. The CSS model is the same as previously used and is described in more detail elsewhere [Kleinman et al., 1997; 2000].

CSS calculations have been performed for 123 locations during the Phoenix field campaign. Calculations were repeated with perturbed values of NO or VOCs. A finite difference formula was used to determine the relative sensitivity of P(O<sub>3</sub>) to NO and VOCs. In Figure 1 we compare those results with sensitivities calculated from the following formulas derived by *Kleinman et al.* [1997]:

$$d\ln P(O_3)/d\ln[NO] = (1 - 3/2 L_N/Q)/(1 - 1/2 L_N/Q)$$
 (2)

$$d\ln P(O_3)/d\ln[VOC] = (1/2 L_N/Q)/(1 - 1/2 L_N/Q)$$
 (3)

It is seen that the variable  $L_N/Q$  provides information on  $NO_x$  and VOC sensitivity similar to that obtained from the CSS calculations. A low value of  $L_N/Q$  yields  $NO_x$  sensitive chemistry; a high value VOC sensitive chemistry. The tendency to produce peroxides under  $NO_x$  sensitive conditions and  $HNO_3$  under VOC sensitive conditions was first noted by Sillman [1995] and forms the basis of an Indicator Species method. Similar results have already been presented for Nashville, Tennessee and the New York City metropolitan area [Kleinman et al., 1997; 2000].

## 4. Theory

The derivation of an analytic formula for  $L_N/Q$  begins with the conservation condition for free radicals expressed in (1).  $L_R$  includes contributions from peroxide formation and biomolecular radical-radical destruction reactions such as  $OH + HO_2$ . The later reactions are generally less important and will be ignored. As in previous work we express the rate of peroxide formation using an effective rate constant,  $k_{eff}$ , defined in terms of the ratio of  $[HO_2]$  to  $[RO_2]$  and the individual rate constants for forming  $H_2O_2$  and ROOH [Kleinman et al., 1997].  $RO_2 + RO_2$  reactions are ignored in the analytic equations but not in the CSS model. For each peroxide molecule formed, 2 radicals are lost and

$$L_R = 2 k_{eff} ([HO_2] + [RO_2])^2$$
 (4)

Combining (1) and (4), we obtain

$$2 k_{eff} ([HO_2] + [RO_2])^2 = Q(1 - L_N/Q)$$
 (5)

The primary NO<sub>x</sub> - radical reaction is

$$OH + NO_2 \rightarrow HNO_3$$
 (R1)

and we approximate L<sub>N</sub> as

$$L_{N} = k_{1} [OH] [NO_{2}]$$
 (6)

So far we have dealt with sources and sinks of radicals. Under many conditions each radical that is formed participates in a multi-step chain reaction before that radical is removed [e.g., Sillman et al., 1990; Jeffries and Tonnesen, 1994; Seinfeld and Pandis, 1997; Tonnesen and Dennis, 2000]. The chain contains the following 2 links

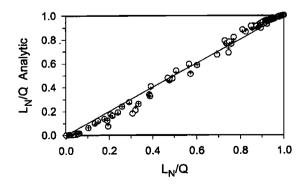


Figure 2. A comparison between  $L_N/Q$  calculated from the analytic formula, (12-13), and CSS model. Open symbols use model derived values for  $HO_2$  to  $RO_2$  ratio. Plus signs use a value of 2:1 for this ratio. Line shows 1 to 1 agreement.

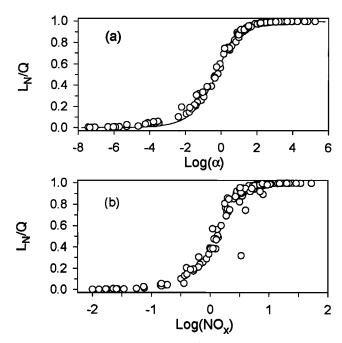


Figure 3. (a) The dependence of  $L_N/Q$  on log  $(\alpha)$ . Solid line is the analytic relation in (12). Data points are determined from Phoenix observations which yield values for  $\alpha$ . CSS calculations yield the corresponding values of  $L_N/Q$ . (b) The dependence of  $L_N/Q$  on  $log(NO_x)$ .

$$OH + VOC \rightarrow HO_2$$
 (R2)

$$HO_2 + NO \rightarrow OH$$
 (R3)

Note that the full reaction sequence can be more complicated as OH+VOC can produce RO<sub>2</sub>s, but eventually (in the absence of a radical loss event) an HO<sub>2</sub> will be produced to regenerate OH. In the limit that chain propagation is much more important than chain initiation (or equivalently, chain termination) we obtain

$$k_2 [OH] [VOC] = k_3 [HO_2] [NO]$$
 (7)

The term  $k_2[VOC]$  in (7) is an abbreviation for a summation over all VOCs, including CO and CH<sub>4</sub>, which can participate in (R2).

From this point on no additional approximations are made. A "constant"  $\gamma$  is defined by

$$\gamma = [HO_2]/[HO_2 + RO_2] \tag{8}$$

Substituting (8) into (5), we get

$$2k_{\rm eff} ([HO_2]/\gamma)^2 = Q (1-L_N/Q)$$
 (9)

Combining (6) and (7) to eliminate [OH] yields

$$[HO_2] = k_2[VOC] L_N/(k_3[NO] k_1[NO_2])$$
 (10)

Substituting (10)into (9) gives a quadratic equation for L<sub>N</sub>/Q

$$(1-L_{N}/Q) = \frac{2k_{\text{eff}}Q}{\gamma^{2}} \left[ \frac{k_{2}[\text{VOC}]}{k_{3}[\text{NO}]k_{1}[\text{NO}_{2}]} \right]^{2} (L_{N}/Q)^{2}$$
(11)

with solution

$$L_N/Q = -\alpha/2 + (\alpha^2 + 4\alpha)^{1/2}/2$$
 (12)

where

$$\alpha = \left(\frac{k_1[NO_2]k_3\gamma[NO]}{k_2[VOC]}\right)^2 \left(\frac{1}{2Qk_{eff}}\right)$$
(13)

Equations (12-13) give  $L_N/Q$  in terms of concentrations and parameters which can be readily observed or estimated. Q can be determined to reasonable accuracy by measuring  $O_3$ ,  $H_2O$ , HCHO, and solar intensity.  $k_{\rm eff}$  and  $\gamma$  depend on the  $HO_2$  to  $RO_2$  ratio which can be estimated based on specific model calculations or on general experience with similar chemical environments.

#### 5. Comparisons with CSS results

We use the CSS calculations to test the analytic equations for  $L_N/Q$ . Figure 2 shows a comparison between  $L_N/Q$  obtained from (12-13) and that obtained from a complete CSS calculation. Two sets of results are shown. In one case (12-13) is evaluated using model predictions for the  $HO_2$  to  $RO_2$  ratio. In the other case the evaluation is done without this information using a representative value of 2 to 1 for the ratio. The later calculation is done to assess the utility of applying (12-13) using commonly available measurements. Both cases show reasonable agreement.

Equations (12) and (13) show how  $L_N/Q$  depends on  $NO_x$ , VOCs, and Q. Perhaps the easiest way to visualize the relation is to note that  $L_N/Q$  is a monotonic, increasing function of  $\alpha$ . Alpha, in turn, is proportional to  $(NO_x^2/VOC)^2/Q$ , assuming that both NO and  $NO_2$  are proportional to  $NO_x$ . Thus,  $L_N/Q$  varies in the same sense as  $(NO_x^2/VOC)^2/Q$ ; i.e., an increase in  $NO_x$  yields a higher value of  $L_N/Q$  (more VOC sensitive) while an increase in VOCs or Q yields a lower value of  $L_N/Q$  (more  $NO_x$  sensitive). Because  $NO_x$  appears to the 4th power in  $\alpha$  and VOCs only to the -2 power,  $L_N/Q$  will be affected more by a change in  $NO_x$  than by a change in VOCs. Note that, according to (13), it is not the VOC concentration itself that is relevant but the VOC reactivity,  $k_2[VOC]$ .

Figure 3a illustrates the monotonic dependence of  $L_N/Q$  on  $\alpha$ . The solid line is the analytic relation given by (12). The data points show the range of values of a observed in Phoenix and the corresponding values of L<sub>N</sub>/Q calculated from the CSS model. There is a good correspondence between analytic and calculated points. In the Phoenix data set  $\alpha$  varies by 13 orders of magnitude. High values occur in samples taken over the downtown high emission rate region, while the lowest values are from the clean free troposphere. As shown in Figure 3b, most of the variability in  $\alpha$  (and hence  $L_N/Q$ ) is due to  $NO_x$  which appears as a 4th power and furthermore varies by almost 3 orders of magnitude. VOC reactivity and radical production rate affect L<sub>N</sub>/Q as described by (12-13). However, these variables are less important than NO<sub>x</sub> because they appear to a lower power in a and also, for the Phoenix data set, their range of values is relatively small. Figure 3b shows that L<sub>N</sub>/O is near 1 for values of NO<sub>x</sub> between the maximum and about 3 ppb. Within this concentration range, P(O<sub>3</sub>) is very VOC sensitive and remains so, until NO<sub>x</sub> is lowered past the 3 ppb threshold value. This threshold depends on chemical conditions, specifically the concentration of VOCs and the rate of radical production. Further decreases in NO<sub>x</sub> are accompanied by a large change in L<sub>N</sub>/Q and hence a transition between VOC and NO<sub>x</sub> sensitivity.

## 6. Discussion and Conclusions

As an air parcel is advected away from its source region, concentrations will change due to oxidation of primary pollutants, dilution and the mixing-in of background air, and the formation of secondary pollutants. We can see how these factors affect  $L_N/Q$  by expressing  $\alpha$  as proportional to  $NO_x^2$  $(NO_x/VOC)^2/Q$ . Oxidation reactions will decrease  $NO_x^2$  and also decrease (NO<sub>x</sub>/VOC)<sup>2</sup> because NO<sub>x</sub> is more reactive than the average VOC [Duncan and Chameides, 1998]. Dilution, accompanied by the mixing-in of background air, will decrease  $NO_x^2$  and also  $(NO_x/VOC)^2$ . The later decrease is due to the circumstance that background air tends to have very little NOx but can have significant VOC reactivity due to CO and CH<sub>4</sub>. Production of O<sub>3</sub> and other photochemical oxidation products such as HCHO will increase Q. All of these factors lead to a decrease in L<sub>N</sub>/Q and therefore contribute to the transition from VOC to NO<sub>x</sub> sensitive behavior as a plume ages.

 $L_N/Q$  is in some ways analogous to photochemical age [e.g., McKeen et al., 1990] in that it is a progress variable that specifies where an air mass is in its chemical and dynamic evolution. Input of fresh emissions into the plume can of course upset the monotonic decrease in  $L_N/Q$ .

The photochemical equations used in typical calculations treat tens to thousands of discrete species. Recently, the photochemical equations have been treated as a dynamical system and the question has been asked as to what number of species is needed to reproduce the behavior of the full set of equations [Field et al., 2001]. Here we are interested in a related question, the number of variables needed to describe steady states. By working with a radical budget equation we are able to write equations for quantities such as  $P(O_3)$  in terms of only 3 variables,  $NO_x$ , VOCs, and Q [Kleinman et al., 1997; Daum et al., 2000]. One variable, namely  $L_N/Q$ , is sufficient to quantify the  $NO_x$  and VOC sensitivity of  $P(O_3)$ . As we have shown here that variable can be evaluated based on readily measured concentrations.

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- P. H. Daum, L. I. Kleinman, Y.-N. Lee, L. J. Nunnermacker, and S. R. Springston, Atmospheric Sciences Division, Environmental Sciences Department, Brookhaven National Laboratory, Upton, NY 11973-5000. (email: phdaum@bnl.gov; kleinman@bnl.gov; ynlee@bnl.gov; lindan@bnl.gov; srs@bnl.gov.)
- J. Weinstein-Lloyd, Chemistry/Physics Department, SUNY/Old Westbury, Old Westbury, NY 11568. (email: jlloyd@bnl.gov.)
- J. Rudolph, Chemistry Department and Centre for Atmospheric Research, York University, Toronto, Ontario M3J 1P3, Canada. (email: rudolphj@yorku.ca.)

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