### PRECISION MICROWAVE FREQUENCY-OFFSET SEPARATED-OSCILLATORY-FIELDS MEASUREMENT OF THE 2<sup>3</sup>P<sub>1</sub>-TO-2<sup>3</sup>P<sub>2</sub> FINE-STRUCTURE INTERVAL IN ATOMIC HELIUM

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## A DISSERTATION SUBMITTED TO THE FACULTY OF GRADUATE STUDIES IN PARTIAL FULFILMENT OF THE REQUIREMENTS FOR THE DEGREE OF

DOCTOR OF PHILOSOPHY

## GRADUATE PROGRAM IN PHYSICS AND ASTRONOMY YORK UNIVERSITY TORONTO, ONTARIO FEBRUARY 2019

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## Abstract

The  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  fine-structure interval in atomic helium is measured using the frequency-offset separated-oscillatory-fields (FOSOF) technique. Two temporally separated microwave fields set up excitation paths that accumulate different quantummechanical phases. To detect the atoms that have changed states due to the microwaves, these atoms are excited to a Rydberg state and Stark ionized. The number of resulting ions is counted on a channel electron multiplier. In a typical SOF experiment, the relative phase between the two microwave pulses is toggled between 0° and 180°, and the change in the signal amplitude between the two phases is detected as a function of applied microwave frequency. In the FOSOF technique, two microwave pulses with a slight frequency offset are applied to the atoms. The relative phase seen by the atoms changes continuously due to the frequency offset, leading to a sinusoidally oscillating atomic signal. The phase of the oscillating signal is measured with respect to the phase of a reference generated by combining the frequency-offset microwaves. The phase difference between the oscillating atomic signal and reference signal crosses zero at resonance and changes linearly as a function of applied microwave frequency.

Major signal-to-noise ratio (SNR) enhancement has been achieved by employing a two-dimensional magneto-optical trap and by using Stark-ionization detection. The excellent SNR allows for a very extensive study of systematic effects. A wide range of experiment parameters has been investigated. The final measured result is 2 291 176 590(25) Hz. This is the most precise measurement of the interval to date and thus the most precise test of the two-electron quantum-electrodynamics theory. When the  $2^{3}P_{0}$ -to- $2^{3}P_{1}$  transition is measured at the same level of precision and the combined result of the  $2^{3}P_{0}$ -to- $2^{3}P_{2}$  fine-structure interval is compared with a sufficiently precise theory, a sub-part-per-billion determination of the finestructure constant using a two-electron system will become possible for the first time. Comparison with other fine-structure constant measurements could lead to tests of possible beyond-the-Standard-Model physics. To My Beloved Family: Kensei, Sara, and Saori

## Acknowledgements

I would like to thank Eric Hessels for an opportunity to work on this excellent experiment. Throughout my PhD career, he taught me everything that it takes to become an expert in the field of precision measurements. He gave me encouragement by showing his determination and enthusiasm towards the measurement. His inspirations and ideas (almost) always worked positively. I also appreciate that he patiently explained physical concepts clearly and intuitively. Without his guidance, I would have been lost. I am truly honoured to have worked with him for the last decade of my life (possibly in the future too).

I would like to thank Nikita Bezginov for being an excellent lab mate. You have always been a person who I could talk about anything. Your ideas and suggestions for the experiment were always helpful. I truly enjoyed the little "fresh air" breaks with you. I would also like to thank you for spotting me at the gym. Without your spot, I might not have survived (literally) my PhD.

I would like to thank Taylor Skinner for his great efforts in simulating the

experiment and analyzing the massive amount of data. Without your contribution to the experiment, I could not have completed the measurement.

To Travis Valdez, thank you for being a good friend and giving me tips on Python. Your success outside academia encourages me to think that I can probably survive anywhere after completing this work.

Nikita, Travis, and Taylor, I will never forget the good times that we spent together both inside and outside 309. I cannot predict where we end up in the future, but hopefully we can talk about atoms in fancier places (not Hoops or Shopsys).

I would like to thank Amar Vutha for his intelligent ideas and suggestions. His inputs and guidance were absolutely necessary for completing this work. Without a doubt, he is one of the most brilliant physicists I have ever seen.

I would like to thank Matthew George for his contribution to the measurement especially during the first few years of my PhD. You also taught me many useful tips to become a good experimentalist. I also enjoyed conversations with you outside Petrie about anything.

I would like to thank Cody Storry for letting me use his expensive equipments. Without his support, the experiment would not have been anywhere near this successful. Also, his valuable ideas and suggestions as an true experimentalist always made ways to tackle on problems.

Thank you Kumar for giving me fresh insights on the experimental work during

research evaluations. You made me realize important things that I would have missed without your comments.

I would like to thank Wendy Taylor for the use of the digital oscilloscope which became an essential part of the experiment.

I wish to thank Derek and Hana Sandy for being my best friends, more like my family, since I started my undergrad at York. You have always been there for me, supported me and encouraged me during the hard times of my life. I will always remember our friendship as the most important thing in my life.

I would like to thank the York Physics and Astronomy department staff for your help and assistance. I would like to give a special thanks to Marlene Caplan. She had always been very nice, and fun to talk to about anything. She also made my life a lot easier by knowing exactly what to do whenever I had administrative issues.

I wish to thank my sisters Michiko and Hisako. They have always supported and encouraged me to do the best in all matters of my life. You were always worried about whether I could actually finish my experiment or not. Here I am, having finished one of the most brilliant and difficult experiments in the world. I will talk to you about atoms next time we meet.

I cannot show enough appreciation to my mother. She gave me a full support throughout my entire life. Even though she lives half way around the globe, I always felt her close. Her warm welcome for every trip back to Japan always makes me feel home and comfortable. I thank you for raising me and making me as I am right now.

Lastly, and most importantly, I would like to say a million thanks to my beloved family Kensei, Sara, and Saori. I cannot say enough to show my appreciation to my wife Saori. Without your support, encouragement, and understanding, my dissertation work would not have been possible. I could focus on my research only because you kept the family safe. Thank you most of all for raising and protecting our children (and not giving up on me). I truly admire and respect you as a person, and I will always love you. Kensei, your smile and laughter always made me feel stronger and encouraged. As a two-year-old father, I might not be the greatest, but I will try not to be the worst. Sara, you are too young to have any interaction yet at this point. However, I wish to thank you for being born healthy, and making my life more delightful. Hopefully there will be a time that I talk to you about this brilliant experiment.

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## 1 Introduction

## 1.1 Fine-Structure Constant

The fine-structure constant was first introduced by Arnold Sommerfeld in 1916 in his effort of including relativistic effects in Bohr's atomic model. In the early days, it was interpreted as a spectroscopic quantity which defines the finer splitting of energy levels in a single-electron system. During the development of quantum electrodynamics (QED), the fine-structure constant gained its significance as a fundamental constant that represents the coupling strength of the electromagnetic interaction between charged particles.

The fine-structure constant is a dimensionless quantity, written in SI units as

$$\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c},\tag{1.1}$$

where e is the elementary charge,  $\epsilon_0$  is the electric permittivity of free space,  $\hbar = h/2\pi$ is the reduced Planck constant, and c is the speed of light in vacuum. QED theory does not predict the value of  $\alpha$ —it needs to be determined experimentally. The value of  $\alpha$  can be determined in a variety of physical systems. Comparison of  $\alpha$  obtained from different systems is of importance for two reasons. One reason is that experimentally measurable quantities in dissimilar systems, such as the electron magnetic moment and the helium fine structure, are represented as different forms of QED expansions in  $\alpha$ ; therefore, different aspects of the QED theory are tested. The second reason is that determinations of  $\alpha$  from different systems are not affected by the same systematic effects, and problems associated with a particular experimental technique can be discovered by comparing results. Various systems showing consistent results confirm the level of understanding of physics; however, any unresolved inconsistency may point to beyond-the-Standard-Model physics.

A number of different systems have been used to obtain a precise value of  $\alpha$ . The most precise determinations of  $\alpha$  come from measurements of the electron magnetic moment ( $g_e$ -2) using the single quantum cyclotron [1], and  $h/m_{Cs}$  atomrecoil measurements using atom interferometry and Bloch oscillations [2]. Both measurements achieve < 0.25 part-per-billion (ppb) determinations of  $\alpha$ . The  $g_e - 2$ measurement tests QED at the 0.25 ppb level, tests for possible substructure of the electron [3,4], tests for the possible presence of dark photons [1,3,5], and puts limits on possible dark axial vector bosons [1,3]. The recoil measurement, along with another  $\alpha$  determination, could be used for an absolute mass standard [6].

The helium fine-structure interval also forms an excellent system for a precise

determination of  $\alpha$ , as well as a precise test of QED. In 1964, Schwartz suggested that a less than 1 part-per-million (ppm) determination of  $\alpha$  might be possible by precisely measuring the helium fine structure intervals and improving the theory for these intervals [7]. Over the last five decades, great efforts in experimental and theoretical work have been made to advance the precision of the helium fine structure [8–18]. With the improvements, the helium fine structure measurement is now approaching a precision of 1 ppb. The current precision of 25 Hz for the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  interval [19] combined with a future < 25-Hz measurement of the  $2^{3}P_{0}$ -to- $2^{3}P_{1}$  interval will lead to an approximately < 1-ppb determination of the  $2^{3}P_{0}$ -to- $2^{3}P_{2}$  transition. This will become a 1 ppb test of QED and a < 0.5 ppb determination of  $\alpha$  when compared to a sufficiently precise theory.

## 1.2 Atomic Structure of Helium

Helium (<sup>4</sup>He) is the second-simplest atom—with the first being hydrogen. It is composed of two electrons bound to a spinless nucleus containing two protons and two neutrons. The set of quantum numbers describing the energy state of the two electrons of helium are the principal quantum number  $n_i$ , the azimuthal quantum number  $l_i$ , the spin quantum number  $s_i$ , and the projections of the  $l_i$  and  $s_i$  onto the  $\hat{z}$  axis ( $m_{l_i}$  and  $m_{s_i}$ ), with the subscript i = 1, 2 denoting the electron number. A helium atom in an arbitrary electronic state is represented as ( $n_1 l_1$ )( $n_2 l_2$ ) where  $l_i$  denotes s, p, d, etc. for  $l_i = 0, l_i = 1, l_i = 2$ , etc. Spectroscopic notation  $n^{2S+1}L$ , where  $S = s_1 + s_2$ ,  $L = l_1 + l_2$ , is used to label the atomic state. The non-relativistic Hamiltonian for a helium atom consists of two hydrogenic Hamiltonians  $H_i$  (i = 1, 2)and an additional term describing the electrostatic repulsion between two electrons. Two electrons in a static Coulomb potential obey a Schrödinger equation of the form,

$$\left[-\frac{\hbar^2}{2\mu}\nabla_1^2 - \frac{\hbar^2}{2\mu}\nabla_2^2 - \frac{\hbar^2}{m_{\alpha}}\nabla_1 \cdot \nabla_2 + \frac{e^2}{4\pi\epsilon_0}\left(-\frac{Z}{r_1} - \frac{Z}{r_2} + \frac{1}{r_{12}}\right)\right]\psi(\mathbf{r}_1, \mathbf{r}_2) = E\psi(\mathbf{r}_1, \mathbf{r}_2),$$
(1.2)

where  $m_{\alpha}$  is the nuclear mass,  $\mu$  is the reduced mass  $\mu = \frac{m_e m_{\alpha}}{m_e + m_{\alpha}}$ , Z = 2 is the atomic number of helium,  $\mathbf{r}_1$  and  $\mathbf{r}_2$  are the position vectors of two electrons with respect to the nucleus, and  $r_{12} = |\mathbf{r}_1 - \mathbf{r}_2|$  is the distance between the two electrons. The electron-electron repulsion term makes the Hamiltonian inseparable and the Schrödinger equation cannot be solved exactly in this case.

#### 1.2.1 Ground State

The ground state of helium is a spin singlet (S = 0) state in which both electrons are in a 1s state with antisymmetric (paired) spin configuration. The Pauli exclusion principle does not allow two electrons to have a same set of quantum numbers; therefore the electrons are forced to be in the singlet state. Helium has the highest ground-state binding energy amongst all of the elements due to its closed-shell configuration in the  $1s^2$  state. The ground-state energy has been calculated very precisely using the variational method [20].

#### 1.2.2 Excited States

Excited states of helium consist of one electron in the hydrogenic ground state and another in the excited state (1snl)—unless it is in a highly unstable doubly excited state. The excited state can be in either the spin singlet (S = 0) or triplet (S = 1)state depending on the spin orientation of the two electrons (spectroscopic notations of  $n^{1}L$  and  $n^{3}L$  for singlet and triplet states, respectively, as shown in Figure 1.1). The singlet state has a symmetric spatial wavefunction that is associated with the antisymmetric spin function, and the total wavefunction of the triplet state is a product of the antisymmetric spatial wavefunction and symmetric spin function. The singlet state has less binding energy than the triplet counterpart because the electron-electron repulsion is larger in the singlet state than the triplet state. The singlet and triplet states are extremely weakly connected by electric dipole transitions, so that they can be treated as separate systems in most cases. The  $2^{1}S$ and  $2^{3}$ S states are metastable states that have very long lifetimes of  $19.7 \pm 1.0 \text{ ms}$  [22] and  $7870 \pm 510$  s [23], respectively. The 2<sup>3</sup>S state is the longest-lived metastable state amongst all of the neutral atoms. The transition between the  $2^{3}$ S and ground state requires an electron spin flip, making it extremely unlikely to occur in free



Figure 1.1: Lowest-lying energy states of helium. Electric-dipole transitions with optical wavelengths are indicated as lines connecting two states. Their wavelengths [21] are labelled on the lines in nm. Transitions relevant to the current experiment are shown in colour.



Figure 1.2: The n=2 triple helium energy-level diagram. The degeneracy of the  $m_J$  states is lifted by a magnetic field (Not to scale).

space. The forbidden transition makes the  $2^{3}$ S state effectively the ground state for the triplet system. Transition from the ground state to the  $2^{1}$ S or  $2^{3}$ S states can be excited using electron bombardment. Figure 1.1 shows the lowest-lying energy states of helium for both singlet and triplet systems in the spectroscopic notation. Some electric-dipole transitions with their corresponding wavelengths are shown in the figure.

#### **1.3 Helium Fine Structure**

#### 1.3.1 Angular Momentum Coupling

Figure 1.2 shows the energy-level diagram of the helium n=2 triplet system. The energy contribution due to the coupling of angular momenta gives rise to the finestructure splitting. The fine-structure splitting of an atom with two electrons is predominantly described by the spin-orbit and spin-spin interactions. The total angular momentum  $\mathbf{J} = \mathbf{L} + \mathbf{S}$  and its projection onto the  $\hat{z}$  axis  $J_z$  lead to the quantum numbers J and  $m_J$ . The spectroscopic notation  $n^{2S+1}\mathbf{L}_J$  describes energy states of an atom including the spin-orbit interaction.

The  $n^{2S+1}L_J$  fine structure energy splitting in helium comes primarily from the spin-dependent part of the Breit-Pauli Hamiltonian (the spin-orbit coupling, spin-spin coupling, and spin-other-orbit coupling). The spin-orbit coupling describes the interaction between the electron magnetic moment and its own orbital angular momentum. The spin-orbit coupling increases with the nuclear charge number Z, and it becomes more significant for atoms with higher-Z nuclei. The spin-spin coupling is the interaction between the spin of one electron and the spin of the other electron. The coupling is described as the interaction that originates from the field produced by the magnetic dipole of one electron at the other electron. The spin-orbit coupling arises from the field produced at the position of one electron by the orbital motion of the other electron. For a helium atom, contributions from the spin-spin and spin-other-orbit interactions are comparable to that of the spin-orbit interaction. As a result, the peculiar  $2^{3}P_{J}$  structure in helium (inverted energy order of J states and the unusually large energy splitting between the J = 0and J = 1 states compared to the splitting between the J = 1 and J = 2 states, as shown in Figure 1.2) arises [24]. The contributions from the leading terms give a reasonable estimate of the energy of the fine-structure state; however, higher-order contributions must be taken into account in order to obtain a precise value of the energy splitting.

#### 1.3.2 QED Description of the Helium Fine Structure

Theoretical calculations for the  $2^{3}P_{J}$  states have been performed by G. W. F. Drake (University of Windsor), T. Shi (Chinese Academy of Sciences), and K. Pachucki (Warsaw University). The most current of these results are listed in Table 1.1. In QED, the energies of the fine-structure states are represented as a power series expansion in  $\alpha$  and can be written as

$$E_{\rm fs} = E_{\rm fs}^{(4)} + E_{\rm fs}^{(5)} + E_{\rm fs}^{(6)} + E_{\rm fs}^{(7)} + \dots$$
(1.3)

The term  $E_{\rm fs}^{(n)}$  represents the energy contribution of the order  $mc^2\alpha^n$ , where m is the electron mass, and c is the speed of light. The leading term  $E_{\rm fs}^{(4)}$  includes corrections of order up to  $mc^2\alpha^4$  described by the Breit-Pauli Hamiltonian. The

Experimental Results					
	$ u_{12} \left( \mathrm{Hz} \right) $	$ u_{01}(\mathrm{Hz})$	$ u_{02}\left(\mathrm{Hz}\right)$		
This work [19] [2018]	2291176590(25)				
Hessels [27,28] [2009,2001]	2291177530(350)	29 616 950 900(900)			
Hu [29] [2017]	2291177560(190)		31908130980(130)		
Gabrielse [30] [2005]	2291175590(510)	29616951660(700)	31 908 126 780(940)		
Shiner [31, 32] [2000,2010]	2291175900(1000)		31908131250(300)		
Theoretical Results					
Pachucki [26] [2010]	2 291 178 900(1700)	29616952300(1700)	31 908 131 200(1700)		
Shi [25] [2015]	2291179510(1700)	29616951850(1700)	31 908 131 360(1700)		

Table 1.1: Summary table of recent  $2^{3}P_{J}$  fine-structure experimental and theoretical results. The symbol  $\nu_{JJ'}$  denotes the energy difference between the  $2^{3}P_{J}$  and  $2^{3}P_{J'}$  fine-structure states. One standard deviation uncertainties in the last digits are shown in parentheses. Numbers in square brackets are the publication year.

current theoretical work on the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  fine-structure interval predicts that  $E_{\rm fs}^{(4)}$  and  $E_{\rm fs}^{(5)}$  together give 2.3-GHz contributions, and  $E_{\rm fs}^{(6)}$  and  $E_{\rm fs}^{(7)}$  give 6.5-MHz and 20-kHz contributions, respectively. The size of the energy contributions from the uncalculated higher-order effects  $\mathcal{O}(\alpha^{8})$  is estimated to be 1.7 kHz by Shi [25] and Pachucki [26]. The theoretical calculations performed by Pachucki and Shi agree with each other.

#### **1.3.3** Measurements of the Helium Fine Structure

The n = 2 triplet system of helium offers a few advantageous features for precision spectroscopy. The narrow natural linewidth of 1.6 MHz allows for a high spectroscopic resolution. The long lifetime (98 ns) of  $2^{3}P_{J}$  states makes the experiment more feasible. The splittings (2.291 GHz and 29.616 GHz) are in the frequency range in which microwave components are commercially available. The  $2^{3}S_{1}$ -to- $2^{3}P_{J}$ transition can be saturated with a small light intensity (0.16 mW/cm<sup>2</sup>) and can easily be driven by a 1083-nm diode laser.

A number of groups have measured the fine structure of helium using different methods over the past five decades. Table 1.1 shows the list of recent measurements and calculations of the helium fine structure. Historical measurements of the finestructure intervals are given in [33]. The research group led by G. Gabrielse (Harvard University) used a saturated absorption spectroscopy setup in a discharge cell to measure the linecentres of all  $2^{3}S_{1}$ -to- $2^{3}P_{J}$  transitions to infer the energy differences for the  $2^{3}P_{J}$ -to- $2^{3}P_{J'}$  intervals. Groups led by D. Shiner (North Texas University) and S. -M. Hu (University of Science and Technology of China) performed optical spectroscopy on the  $2^{3}S_{1}$ -to- $2^{3}P_{J}$  transitions on a thermal beam of triplet helium atoms to probe the fine-structure energy differences. E. A. Hessels' group uses microwaves to drive the magnetic-dipole  $2^{3}P_{J'}$ -to- $2^{3}P_{J'}$  transitions and directly measure the transition frequencies.

A similar microwave spectroscopy setup is used for the current measurement with an improved experiment scheme and a new spectroscopy method. A variation of separated oscillatory fields (SOF) is used in which the frequency of the separated oscillatory fields are offset slightly. This method was recently developed by Hessels and Vutha [34] and is referred to as FOSOF (frequency-offset SOF). The precision of the measurement is improved significantly compared to the previous microwave measurement.

# 2 Experimental System

#### 2.1 Experiment Overview

Figure 2.1 shows the experiment setup for the current measurement. Figure 2.2 shows a helium energy-level diagram with the microwave and laser transitions relevant to the current experiment. As shown at the left of Figure 2.1, a thermal beam of metastable helium atoms is produced through electron bombardment in a DC discharge. The discharge puts equal populations in all magnetic sublevels of the metastable  $2^{3}S_{1}$  state. The helium metastable beam exits a small aperture with an angular spread of approximately 50 mrad, and this spread leads to a significant loss in the number of atoms making it to the main experiment region, which is located 86 cm away from the aperture. To significantly reduce this loss, a two-dimensional magneto-optical trap (2DMOT shown in Figure 2.1) is used to focus and collimate the metastable beam. The 2DMOT cooling transitions are shown in Figure 2.2, labelled as 2DMOT.

The main experiment occurs inside a microwave coaxial airline, and this region is



Figure 2.1: Experimental setup (not to scale). A thermal beam of metastable helium atoms emerging from the DC discharge is intensified using a two-dimensional magneto-optical trap (2DMOT). Optical pumping of the metastable  $2^{3}S_{1}$  state (OP) is performed before the atoms enter the microwave region through a 0.5-mm-by-5-mm slit. Only atoms that experience a complete SOF sequence are ionized and detected by channel electron multiplier (CEM).



Figure 2.2: Experiment energy-level diagram. Arrows represent laser and microwave excitations. Degeneracy of the magnetic sublevels is lifted by a DC magnetic field

shown on a larger scale in the inset of Figure 2.1. A DC magnetic field in the vertical  $\hat{z}$  direction is applied to lift the degeneracy between  $m_J$  states. A circularly polarized continuous-wave (CW) 1083-nm laser (OP in Figures 2.1 and 2.2) is directed along the  $\hat{z}$ -direction, and intersects the atomic beam before the atoms enter the airline. This laser optically pumps atoms into the  $2^3S_1(m_J=-1)$  state and empties out the rest of the  $2^3S_1$  magnetic sublevels. The optically-pumped helium atoms then enter the airline through a small slit (He<sup>\*</sup> entrance slit in Figure 2.1). Once atoms travel past the inner conductor of the airline, the main experimental sequence starts.

Figure 2.3 shows the timing of the experiment sequence and the populations


Figure 2.3: Experiment timing diagram. (a) A continuous series of laser and microwave pulses are shown. A (red), B (blue), and C (green) indicate 1083-, 447-, and 1532-nm laser pulses. The purple boxes are the microwave pulses used in the experiment. Panel (b) shows the population transfer during a single experiment sequence (indicated in (a) as a black rectangle). The red wavy arrows represent radiative decay of the  $2^{3}P_{J}$  states during the experiment. The green dot represents the atoms that are detected by Stark-ionization of Rydberg atoms. The timing for the pulses varies as discussed in Section 2.11.4

of the atomic states during the experiment sequence. A pulse of linearly polarized 1083-nm laser (A in Figures 2.1, 2.2, and 2.3) tuned to the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  transition is sent through the airline to prepare atoms into the  $2^{3}P_{1}(m_{J}=-1)$  state. Two temporally separated microwave pulses (purple arrows and boxes in Figures 2.2 and 2.3) drive the  $2^{3}P_{1}(m_{J}=-1)$ -to- $2^{3}P_{2}(m_{J}=-1)$  transition. The second microwave pulse is followed by subsequent pulses of 447- and 1532-nm lasers (B and C in Figures 2.1, 2.2, and 2.3). The 447-nm laser drives the transition from the  $2^{3}P_{2}$  state to the

 $4^{3}D_{3}$  state, and the 1532-nm laser brings the  $4^{3}D_{3}$  atoms up to the  $18^{3}P_{2}$  Rydberg state. The 18P state lives long enough to exit from the airline before a significant fraction decays down to lower-energy states. At the downstream exit of the airline, an electric field is applied to the Rydberg atoms to induce Stark-ionization, and the number of resulting ions is counted using a channel electron multiplier (CEM) detector.

# 2.2 Beamline and Vacuum System

Figure 2.4 shows the vacuum system used for the current experiment. The beam of metastable helium atoms produced at the start of the beamline goes through a series of vacuum chambers. The beamline is composed of five sections (as indicated in Table 2.1 and Figure 2.4) and atoms go through the sections in the following order: the metastable helium source, 2DMOT section, main experiment chamber, 1532nm laser frequency stabilization chamber (laser-locking chamber), and atom-speed measurement chamber. Metastable atoms are produced inside the source chamber and they exit the chamber through a 1-mm-diameter skimmer (as will be discussed in Section 2.3). The atoms then expand into the 2DMOT chamber where the beam of atoms is focused and collimated by the 2DMOT (as will be discussed in Section 2.9). The collimated beam of atoms enters the main experiment chamber where the atoms go through the microwave coaxial airline (shown in Figure 2.1) inside of



Figure 2.4: Beamline and vacuum system. Main sections of the beamline and vacuum components that constitute the beamline are shown. HV:high voltage, MW:microwave, LN<sub>2</sub>:liquid nitrogen.

which the FOSOF experiment happens. The atoms then travel to the laser-locking chamber, in which some of the atoms are excited up to the 18<sup>3</sup>P Rydberg state and ionized, and the resulting ion signal is used to stabilize the 1532-nm laser (as will be discussed in Section 2.6.2). The atoms are then sent to the last section of the beamline that hosts an atom-speed measurement system (which will be discussed in Section 2.4). The length of the beamline is 3.8 m in total.

Section name	Primary pump	$C_V [L/s]$	Backing pump	$C_V  [\mathrm{L/min}]$	Base pressure [torr]
Metastable helium source chamber (0–0.3 m)	Agilent V1001	1000	Agilent Triscroll300	250	$5 \times 10^{-5}$
2DMOT chamber $(0.30.8\mathrm{m})$	Agilent V250	250		250	$5 \times 10^{-7}$
Main experimental chamber $(0.81.5\mathrm{m})$	Agilent V1001	1000	Agilent Triscroll300	250	$3 \times 10^{-9}$
Laser-locking chamber $(1.5-2.2\mathrm{m})$	Agilent V250	250		110	$9\times 10^{-10}$
Speed-measurement chamber $(2.2–3.8\mathrm{m})$	Agilent V1001	1000	Agilent SH110	110	$8 \times 10^{-9}$

Table 2.1: List of vacuum pumps used in the experiment. The symbol  $C_V$  denotes the pumping speed of the vacuum pumps. Merged rows in the backing pump column indicate that the backing pump is shared by multiple turbo pumps.

It is important to achieve the highest vacuum possible in all sections in order to avoid a loss in number of atoms due to the elastic scattering and collisional ionization with the background gas in the system. The vacuum pressure in each of the sections is maintained by a turbo-molecular pump backed by a dry-scroll pump. Table 2.1 summarizes the vacuum pumps used in the system and the ultimate pressure in each section. A large amount of helium gas is leaked into the source chamber for the metastable helium production. It is critical to maintain the lowest pressure possible especially in the main experiment chamber to ensure the cleanest experiment environment (problems with the increased background pressure will be addressed in Section 2.7). A 1-L/s pumping restriction is installed at the junction between the 2DMOT and main experiment chambers to limit the amount of helium gas leaking into the main experiment chamber. Additionally, a residual gas analyzer (SRS RGA100) is installed on the main experiment chamber to help in understanding the background gas characteristics. Pressures in all chambers and their roughing lines are monitored using ionization (Granville-Phillips 355) Micro-Ion) and Pirani vacuum-pressure gauges (Granville-Phillips 275 Convectron). Roughing-line pressures are typically lower than the lowest measurable pressure of the Pirani gauge, so they are not listed in Table 2.1. Analog outputs from the gauge controllers are used for the interlock system to protect sensitive devices from vacuum failure. In each section of the beamline, a valve is installed to use nitrogen as a back-filling gas instead of ambient air when breaking vacuum. This prevents water molecules in the ambient air to be adsorbed on the vacuum chamber wall, and this makes the successive pump-down process be much faster than the case of air-filling vacuum breaking.



Figure 2.5: Metastable helium source

# 2.3 Metastable Helium Source

Detailed descriptions on the metastable atom source can be found elsewhere [33, 35–38], so only technical details are presented in this section. A liquid-nitrogencooled DC-discharge metastable atom source design is employed in the current experiment. Figure 2.5 shows a schematic of the metastable helium source. It produces metastable atoms by the electron bombardment in the DC discharge via the following process:

$$\text{He} + e^{-}(T) \to \text{He}^{*} + e^{-}(T - 20 \,\text{eV}),$$
 (2.1)

where the kinetic energy T of an electron is transferred to a helium atom by an inelastic collision. The source produces about  $10^{15}$  He<sup>\*</sup> $(2^{3}S_{1})$ /sterad/s. The main source assembly consists of a needle cathode that is enclosed in an insulating alumina tube capped and sealed with a boron nitride piece with a 0.3-mm-diameter, 1-cm-long nozzle machined at its centre. The source assembly is held by a copper mount that is thermally attached to a liquid-nitrogen-cooled cold finger with copper braids. Sheets of indium are used to make a good thermal contact between the copper braids and the main source assembly. The copper braids are used instead of a solid copper structure to allow for an adjustment of the nozzle position (for signal optimization) using a xyz translation stage. Ultra-pure (99.999%) helium gas from a cylinder is fed into the source chamber and its flow is regulated using a mass-flow controller (model 1179A51CS1BV-S). PTFE tubing inside the chamber guides the helium gas to the main source assembly. The helium atoms supersonically expand into the low-pressure side of the vacuum chamber through the boron-nitride nozzle [35]. The large pumping restriction of the boron-nitride nozzle ensures a large pressure gradient between the high- and low-pressure regions of the vacuum chamber. The pressure inside the alumina tube is measured using a capacitance gauge (Edwards 600AB 100TR) and is at 50 torr in a typical source operation. The DC discharge essential in producing the metastable atoms is maintained between the needle cathode and stainless-steel grounded skimmer hole through the boron-nitride

nozzle. Ignition of the arc is achieved by applying 5 kV (supplied by the Glassman high-voltage power supply (model PS/FR06R50.0GA1)) between the needle cathode and skimmer hole. A 100-k $\Omega$  resistor chain ensures the current-limited operation of the power supply. Once the arc is ignited, the voltage output from the power supply drops down to 3.1 kV and draws a typical set current of 25 mA. The voltage drop across the needle cathode to the skimmer hole is approximately 600 V.

The source operation without liquid-nitrogen cooling is avoided due to the low melting point of indium, as molten indium falling into the turbo pump damages the pump. An interlock is installed to shut down the source in case the temperature of the source reaches a set threshold value, which ensures a safe operation of the source in the case of liquid-nitrogen exhaustion. To avoid exhaustion of the liquid nitrogen and to allow for a round-the-clock operation of the experiment, an automatic liquidnitrogen filling system has been implemented. Two cryogenic solenoid valves (ASCO 8222G002LT) are installed in series in the liquid-nitrogen transfer line. When a low level of liquid nitrogen is detected by the cryogen-level sensor (J.C. CONTROLS SN2-7), the sensor outputs AC power to the solenoid valves, enabling the transfer line. The AC power line is controlled by a computer-controlled power strip.

Stable operation of the source is essential in performing precision measurements. The design of this source is very robust, and requires no regular maintenance. The typical failure mode of similar DC-discharge sources is wearing of the boron-nitride nozzle due to the constant exposure to an intense plasma. Another typical issue is the formation of an insulating layer on the needle cathode, making it more difficult to ignite an arc over time. These failure modes do not appear to be issues with the source design used here. This source has been fully operational without performing any maintenance for over three years.

#### 2.4 Atom-Speed Measurement

Figure 2.6 shows the atom-speed measurement setup. The speed of atoms emerging from the metastable helium source is monitored in the last section of the beamline. The chamber (shown in Figure 2.4) hosts an optical chopper (Stanford Research Systems SR540), a Stern-Gerlach (SG) magnet, and a CEM detector on a translation stage. The beam produced by the DC-discharge source consists of singlet- and triplet-metastable helium atoms, as well as UV photons. When the beam is chopped (with a 98% off, 2% on chopper), it becomes a series of pulses that contain all three components of the beam. The pulse then travels through a 1.1-m drift section. During the travel, the UV photons and atoms separate spatially due to their speed difference. From the difference in arrival time and the length of travel, the speed of atoms can be determined (using what we refer to as the time-of-flight (TOF) method). Figure 2.7 shows the typical TOF signal. The data gives information about the beam's most probable speed and its speed distribution. The peak on the



Figure 2.6: Time-of-Flight (TOF) measurement setup. A chopped beam of metastable atoms separates from UV photons in the 1.1-m drift section. The Stern-Gerlach (SG) magnet separates different magnetic sublevels. The time-resolved signal from the CEM is monitored.

left is the chopped UV signal, and the one on the right is the mixture of triplet and singlet atoms. The TOF signal is constantly monitored on an oscilloscope for diagnostics of the 2DMOT and source operation.

The location of the CEM is occasionally changed to check the distribution of atoms in the magnetic sublevels of  $2^{3}S_{1}$  states. The SG magnet deflects  $m_{J}=\pm 1$ states in the vertical direction and by changing the position of the CEM, the distribution of atoms in different  $m_{J}$  states is probed. No significant difference in the TOF signal is found for different  $m_{J}$  states—indicating that the singlet and triplet atoms have the same speed distribution.



Figure 2.7: A typical Time-of-Flight (TOF) signal. The speed of atoms is determined from the time difference and flight distance. From the data, the speed is estimated to be around 1100 m/s.

# 2.5 1083-nm Laser Systems

Two 1083-nm lasers are used in the current experiment. One of the lasers is locked to the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  transition and it is used for multiple applications: the 2DMOT (2DMOT in Figure 2.2), optical pumping (OP in Figure 2.2), and frequency stabilization of detection lasers (lasers B and C in Figures 2.1, 2.2, and 2.3). The other laser is used to excite the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  transition (laser A in Figures 2.1, 2.2, and 2.3) to prepare atoms in the  $2^{3}P_{1}$  state for the experiment. Details of the optics setup of each laser are presented in this section.

Application	Locking	1532-nm pump	Optical pumping	447-nm pump	2DMOT	
Frequency [MHz]	$f_0$	$f_0$	$f_0 - 20 \pm f_{\rm EOM}$	$f_0 - 20 + 185$	$f_0 - 20$	

Table 2.2: Summary of the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser frequencies. The frequency of the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser is adjusted for each application.  $f_{0}$  is the resonance frequency of the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  transition. Two AOMs are used to generate frequencies given in the table. The AOM frequencies are set to  $f_{AOM1} = 185$  MHz and  $f_{AOM2} = 175$  MHz.  $f_{EOM}$  denotes the driving RF frequency of the fiber-EOM.

#### 2.5.1 $2^{3}S_{1}$ -to- $2^{3}P_{2}$ Laser System

Figure 2.8 shows the schematic diagram of the 1083-nm  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser system. This laser is used for the 2DMOT, optical pumping of the  $2^{3}S_{1}$  state, and stabilization of the detection lasers (447- and 1532-nm lasers). Table 2.2 summarizes the applications and corresponding frequencies of the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser.

The 1083-nm laser light is emitted from a distributed Bragg reflector (DBR) laser diode (Photodigm PH1083DBR) (DL in Figure 2.8). The laser diode outputs 40 mW of optical power. The diode is driven by a Melles Griot diode laser driver (06DLD203A). The laser light from the diode goes through two 30-dB (OFR IO-5-1083-HP and Conoptics 715) optical isolators (30dB in Figure 2.8) before coupling into the 15-W Nufern fiber amplifier (NuAmp NUA-1064-PB-0015-C2). The fiber coupler (FC in Figure 2.8) is mounted on a x-y translation stage to optimize the coupling. A 30-dB isolator is installed on the output of the fiber amplifier to suppress



Figure 2.8: 1083-nm  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser system. DL:diode laser, M:mirror, 30dB:30-dB optical isolator, FC:fiber coupler,  $\lambda/2$ :half-wave plate, PBS:polarizing beam splitter, NPBS:non-polarizing beam splitter, AOM:acousto-optic modulator, L:lens, CL:cylindrical lens,  $\lambda/4$ :quarter-wave plate, BD:beam dump, EOM:electro-optic modulator, LP:linear polarizer, W:glass wedge, PD:photodiode.

any back-reflection.

The amplified output is first split into two paths using a half-wave plate and a polarizing beam splitter cube ( $\lambda/2$  and PBS in Figure 2.8) (this combination will be referred to as  $\lambda/2$ -PBS). One of the paths is used for the 2DMOT. The 2DMOT laser path (labelled as 2DMOT in Figure 2.8) is split into four paths using a  $\lambda/2$ -PBS and two 50-50 non-polarizing beam splitter cubes (NPBS in Figure 2.8). A circular polarization required for the 2DMOT operation is produced by having each of the four paths to go through a quarter-wave plate ( $\lambda/4$  in Figure 2.8). These beams then go through pairs of cylindrical lenses (1- and 10-cm focal lengths, CL in Figure 2.8) for beam expansion. The expanded laser beams are sent to the 2DMOT chamber (details of the 2DMOT setup are given in Section 2.9).

The other path is used for multiple applications: optical pumping and frequency stabilization of the detection lasers (447- and 1532-nm lasers). The laser frequency is adjusted by using two acousto-optic modulators (AOMs) for each application. This path first goes through a PBS and an AOM (AOM1 in Figure 2.8) in the dual-pass configuration [33, 39]. The AOM is driven by a continuous wave (CW) RF signal with the frequency  $f_{AOM1} = 185$  MHz. This AOM produces three laser paths with different frequencies. The frequency-unshifted laser path (OP in Figure 2.8) is used for the optical pumping of the  $2^3S_1$  state. This path is coupled into a fiber-based electro-optic modulator (fiber-EOM in Figure 2.8) (the use of the

EOM is explained in Section 2.8). The output of the fiber-EOM goes through a linear polarizer and a quarter-wave plate (LP and  $\lambda/4$  in Figure 2.8) to produce an appropriate polarization for the optical pumping. It is then sent to the main experiment chamber. The first-order diffracted path is retro-reflected back into the AOM. The dual-pass produces two paths with frequency shifts of  $+f_{\rm AOM1}$  and  $+2f_{AOM1}$ . The path with the frequency shift of  $+f_{AOM1}$  (labelled as 447 locking in Figure 2.8) is used as a pump laser for the 447-nm laser frequency stabilization (the 447-nm laser system is described in Section 2.6.1). The path with the  $+2f_{AOM1}$ frequency shift (labelled as locking in Figure 2.8) is sent to the second AOM (AOM2) in Figure 2.8). This AOM is also in the dual-pass configuration driven by a CW RF signal with the frequency  $f_{AOM2} = 175$  MHz. AOM2 is configured such that the dual-pass output path acquires a frequency shift of  $-2f_{AOM2}$ . The dual-pass output of AOM2 acquires a net frequency shift of  $2f_{AOM1} - 2f_{AMO2} = +20 \text{ MHz}$ with respect to the initial laser frequency (laser diode output frequency). This path is split by a  $\lambda/2$ -PBS and sent to the frequency stabilization setups for this laser itself (which locks it to the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  transition) and for the 1532-nm laser (the 1532-nm laser system is described in Section 2.6.2).



Figure 2.9: 1083-nm  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  laser system. DL:diode laser, M:mirror, 30dB:30-dB optical isolator, FC:fiber coupler,  $\lambda/2$ :half-wave plate, PBS:polarizing beam splitter, AOM:acousto-optic modulator, L:lens,  $\lambda/4$ :quarter-wave plate, BD:beam dump, LP:linear polarizer, PD:photodiode. Dashed lines indicate the pulsed laser paths.

#### 2.5.2 $2^{3}S_{1}$ -to- $2^{3}P_{1}$ Laser System

Figure 2.9 shows the schematic diagram of the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  laser system. This laser excites the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  transition to prepare atoms in the  $2^{3}P_{1}$  state. A same model of DBR laser as in the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  laser system is used (DL in Figure 2.9). The laser light from the diode first goes through a 30-dB optical isolator to reduce the back-reflection into the laser diode. It is then split into two paths. One is used for the frequency stabilization (sub-Doppler DAVLL in Figure 2.9, which will be discussed in Section 2.5.3), and another path is sent to the Keopsys 2-W fiber amplifier. The output of the amplifier goes through a 30-dB isolator to minimize the back-reflection into the amplifier. The amplified output goes through two AOMs in the dual-pass configuration. The first AOM (AOM1 in Figure 2.9) is driven by a CW 200-MHz RF signal. The dual-pass output of this AOM acquires a net downward frequency shift of 400 MHz. The second AOM (AOM2 in Figure 2.9), driven by a pulsed RF signal, produces laser pulses used for the main experiment (laser pulsing is detailed in Section 2.11.3). AOM2 shifts up the laser frequency so that the net frequency shift from the two AOMs is close to zero. The laser pulses are sent to the main experiment chamber after being combined with the detection lasers (Sections 2.6.1 and 2.6.2). The polarization of the pulsed laser is adjusted by using the combination of a half-wave plate, a linear polarizer, and a quarter-wave

plate ( $\lambda/2$ , LP, and  $\lambda/4$  in Figure 2.9, respectively). The linear polarizer sets the polarization orientation for the experiment, and the  $\lambda/4$ -plate compensates for the birefringence associated with optics that this laser beam goes through before interacting with atoms. The half-wave plate controls the optical power used for the experiment by rotating the polarization before the linear polarizer. The unshifted output from the AOM1 is used for diagnostics of the polarization of this laser when interacting with atoms.

#### 2.5.3 Stability of the 1083-nm Lasers

The sub-Doppler dichroic-absorption-vapor-laser lock (DAVLL) technique [40–42] is employed for the frequency stabilization of both 1083-nm lasers. The sub-Doppler DAVLL setup is shown in both Figures 2.8 and 2.9. A typical saturated absorption spectroscopy setup with a pair of Helmholtz coils around the RF-discharge cell constitutes the sub-Doppler DAVLL setup. The Helmholtz coils set up a DC magnetic field aligned with the laser propagation axis. Linearly polarized counter-propagating pump and probe beams are overlapped within the cell. The applied magnetic field lifts the degeneracy of the magnetic sublevels and sets the quantization axis of the atoms. The linearly polarized light that propagates along the atom's quantization axis can be represented as light whose polarization is a linear combination of  $\sigma^+$ and  $\sigma^-$  polarizations. This implies that both  $\Delta m = +1$  and  $\Delta m = -1$  transitions are driven simultaneously within the cell. The  $\Delta m = +1$  and  $\Delta m = -1$  transitions are Zeeman shifted by  $\pm g\mu_B B/h$ , where g is the Lande g-factor,  $\mu_B$  is the Bohr Magneton, B is the applied magnetic field, and h is the Planck constant. The  $\sigma^+$ and  $\sigma^-$  polarization components are split by a quarter-wave plate and a polarizing beam splitter. The two signals,  $\Delta m = +1$  and  $\Delta m = -1$  absorption signals, are then subtracted to obtain the error signal necessary for the frequency stabilization. The error signal is fed to a 100-kHz analog PID controller (SRS SIM960). The correction signal is applied to the current modulation input of the diode laser controller. To enhance the long-term stability of the laser frequency, a secondary feedback is applied to the temperature fine-adjust input of the laser controller.

Unlike the original DAVLL technique [43] where a Doppler broadened transition is used to obtain the error signal, the sub-Doppler DAVLL technique uses a narrow Doppler-free absorption signal for the error signal generation. The sub-Doppler DAVLL technique provides a higher frequency-noise sensitivity and a smaller magnetic field requirement for the error signal generation.

A beat-note detection [44] is set up using the two lasers to evaluate the frequency stability of each laser. The two lasers are both tuned to the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  transition for this test and have slightly different lockpoints (~ 20 MHz). The two laser beams are overlapped and sent to a fast photodiode for the beat-note detection. The frequency of the beat-note is monitored and tallied into a histogram. The histogram



Figure 2.10: A histogram showing the 1083-nm laser frequency stability. The beat-note frequency is monitored and beat-note centre is tallied to estimate the frequency jitter.

of the beat-note frequencies is shown in Figure 2.10. The histogram is fit to a Gaussian function to extract the width of the distribution. Fit results show that each 1083-nm laser is locked to about  $\pm 500$  kHz.

## 2.6 Detection Laser Systems

Shortly after the microwave drives the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition, subsequent 447- and 1532-nm lasers (laser B and C in Figures 2.2, 2.1, and 2.3) excite  $2^{3}P_{2}$  atoms up to the 18<sup>3</sup>P Rydberg state for the Stark-ionization detection. This section describes the setup of the 447- and 1532-nm laser systems.

## 2.6.1 447-nm $2^{3}P_{2}$ -to- $4^{3}D_{3}$ Laser System



Figure 2.11: 447-nm  $2^{3}P_{2}$ -to- $4^{3}D_{3}$  laser system. M:mirror,  $\lambda/2$ :half-wave plate, PBS:polarizing beam splitter, AOM:acousto-optic modulator, L:lens,  $\lambda/4$ :quarter-wave plate, BD:beam dump, DM:dichroic mirror, PD:photodiode. Dashed lines indicate the pulsed laser paths.

Figure 2.11 shows the schematic diagram of the 447-nm laser system. The 447-nm laser is used to drive the  $2^{3}P_{2}$ -to- $4^{3}D_{3}$  transition and is also used for the frequency stabilization of the 1532-nm laser. 40-mW of 447-nm laser light is produced by the external-cavity diode-laser system (Toptica DL-PRO HP). The laser beam is first split into two paths. One of the paths is used for the frequency stabilization of the 1532-nm laser, and the other path is used for the main experiment (labelled as experiment in Figure 2.11). The path for the main experiment goes

through an AOM (AOM1 in Figure 2.11) in the dual-pass configuration. This AOM is driven by a pulsed RF signal to generate the laser pulses for the experiment (laser pulsing is detailed in Section 2.11.3). The frequency of the laser pulses is shifted by  $2f_{\rm RF}$  relative to the other path.  $f_{\rm RF}$  is typically set around 200 MHz because the AOM diffraction efficiency peaks at that frequency. The driving frequency of AOM1 is changed slightly for different experiment settings. The laser path for the frequency stabilization goes through another AOM (AOM2 in Figure 2.11). The unshifted path is sent to the laser-locking setup, and the second-order diffracted path is sent to the 1532-nm laser-locking chamber. The second-order diffraction path acquires a same frequency shift ( $2f_{\rm RF}$ ) as the pulsed laser. The laser frequency needs be locked  $2f_{\rm RF}$  away from the resonance to have the pulsed laser path and 1532-nm laser-locking path to be on the atomic resonance.

The laser-locking setup consists of two paths. One of the paths is sent to the helium discharge cell (He<sup>\*</sup> cell in Figure 2.11) and is overlapped with a counterpropagating 1083-nm pump laser inside the cell. The two laser beams are overlapped using a dichroic mirror (DM in Figure 2.11). The 447-nm laser absorption signal is monitored on a photodiode (PD<sub>Abs</sub> in Figure 2.11). The 1083-nm pump laser continuously excites the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  transition to maintain a constant population in the  $2^{3}P_{2}$  state and the 447-nm laser drives the  $2^{3}P_{2}$ -to- $4^{3}D_{3}$  transition. The other path goes straight to a photodiode (PD<sub>Bkg</sub> in Figure 2.11) for background subtraction of the absorption signal.

The compensation for the frequency shift caused by the AOM1 is achieved by using a Doppler-shifted resonance of the 447-nm  $2^{3}P_{2}$ -to- $4^{3}D_{3}$  transition induced by the detuning of the 1083-nm pump laser. The velocity distribution of atoms inside the cell is described by the Maxwell-Boltzmann distribution. The Dopplerbroadening of the transition due to the velocity distribution allows atoms to be on resonance with a wide range of the 1083-nm laser detuning. The Doppler width of a transition is

$$\Delta \nu_{\text{Doppler}} = \frac{2\nu_0}{c} \sqrt{\frac{2\text{ln}(2)k_BT}{m_{\text{He}}}},$$
(2.2)

where  $\nu_0$  is the transition frequency, c is the speed of light in vacuum,  $k_B$  is the Boltzmann constant, T is the temperature in kelvin, and  $m_{\text{He}}$  is the helium mass. At room temperature ( $T \sim 300 \text{ K}$ ), the Doppler width of the 1083-nm 2<sup>3</sup>S<sub>1</sub>-to-2<sup>3</sup>P<sub>2</sub> transition is 1.7 GHz. The detuned pump laser excites atoms in a particular velocity group, and the 447-nm laser interacts with these moving 2<sup>3</sup>P<sub>2</sub> atoms, giving rise to a Doppler-shifted resonance of the 447-nm 2<sup>3</sup>P<sub>2</sub>-to-4<sup>3</sup>D<sub>3</sub> transition. Locking the laser frequency onto the Doppler-shifted absorption signal of the 447-nm 2<sup>3</sup>P<sub>2</sub>-to-4<sup>3</sup>D<sub>3</sub> transition compensates for the AOM frequency shift if the detuning of the 1083-nm laser is appropriately chosen. Since the atoms see a 2.4 times ( $f_{447}/f_{1083}$ ) larger Doppler shift for the 447-nm 2<sup>3</sup>P<sub>2</sub>-to-4<sup>3</sup>D<sub>3</sub> transition than for the 1083-nm 2<sup>3</sup>S<sub>1</sub>-to-2<sup>3</sup>P<sub>2</sub> transition, the relationship between the detuning of the 1083-nm pump laser and 447-nm laser is

$$\Delta f_{\text{lock}}(447) = -2.4 \times \Delta f_{\text{pump}}(1083), \qquad (2.3)$$

where the negative sign results from the fact that the two lasers are counterpropagating. Using Equation 2.3, the 1083-nm pump laser detuning required to compensate for the typical 400 MHz shift on the 447-nm laser is 165 MHz.

A conventional frequency-modulated error signal generation method is used for stabilizing the 447-nm laser frequency [45]. The frequency-modulated 447-nm absorption signal is sent to the integrated servo circuit of the laser diode controller (TOPTICA DLC-PRO) to obtain the error signal. The correction signal is applied to the piezo-controlled grating mount and the driving current of the diode.

#### 2.6.2 1532-nm $4^{3}D_{3}$ -to- $18^{3}P_{2}$ Laser System

Figure 2.12 shows the schematic diagram for the 1532-nm  $4^{3}D_{3}$ -to- $18^{3}P_{2}$  laser system. The 1532-nm laser drives the final transition that brings atoms in the  $4^{3}D_{3}$  state up to the  $18^{3}P_{2}$  state for Stark ionization. The laser light is produced by a DBR laser diode in a butterfly package (Alcatel A1905LMI, DL in Figure 2.12), which outputs an optical power of 20 mW. The laser output is coupled into a 200-mW erbium-doped fiber amplifier (Thorlabs EDFA100P). The output from the amplifier is pulsed using an AOM in a single-pass configuration (laser pulsing is detailed in Section 2.11.3). The laser pulses are sent to the main experiment chamber after



Figure 2.12: 1532-nm  $4^{3}D_{3}$ -to- $18^{3}P_{2}$  laser system. DL:diode laser, M:mirror, FC:fiber coupler,  $\lambda/2$ :half-wave plate, AOM:acousto-optic modulator, L:lens,  $\lambda/4$ :quarter-wave plate, LP:linear polarizer, DM:dichroic mirror. Dashed line indicates the pulsed laser path.

being combined with the 1083- and 447-nm laser pulses (described in Sections 2.5.1 and 2.6.1). The unshifted laser beam is used for the frequency stabilization. This laser is overlapped with the 1083- and 447-nm pump lasers using two dichroic mirrors. The overlapped lasers are sent to the frequency stabilization chamber in which some fraction of metastable helium atoms in the beamline are excited to the Rydberg state and ionized. The laser frequency is stabilized to the resonance of the ion signal. This lock-to-beam method is necessary since the RF electric field in the discharge cell perturbs the Rydberg states and the 1532-nm laser cannot excite the  $4^3D_3$ -to- $18^3P_2$  transition inside the cell. Figure 2.13 shows a cross-sectional view of the Stark ionizer for the frequency stabilization. The overlapped lasers interact with the beam of metastable atoms and produce  $18^3P$  Rydberg atoms. The Rydberg atoms are then ionized by a DC electric field set up between a copper



Figure 2.13: Cross-sectional view of the Stark ionizer for 1532-nm laser frequency stabilization. The energy level diagram for the ionization scheme is shown at the left. The overlapped lasers and metastable helium beam intersect at the field-free region and 18<sup>3</sup>P atoms are created. The 18<sup>3</sup>P atoms then proceed to the region with the ionizing electric field. Resulting ions are accelerated towards the CEM and counted.

plate and a copper mesh with 90% transparency (HV plate and HV mesh in Figure 2.13). The two electrodes are separated by 5 mm. The laser excitation is isolated from the ionizing electric field by a 1-mm-by-5-mm slit with a wall thickness of 5 mm, because any residual electric field at the interaction location would cause a lineshape distortion due to the DC Stark effect on the 18<sup>3</sup>P state. The helium ions are accelerated towards the CEM located above the copper mesh and the number of ions is counted. The frequency of the laser is modulated to obtain an error

signal [45]. The correction signal is applied to the current modulation input of the laser diode controller. A secondary correction is applied to the temperature fine-adjust input of the controller. The frequency shift due to the AOM pulsing is compensated by utilizing the sideband-locking method. The laser diode package contains an integrated bias-Tee for current modulation. Small sidebands are added to the primary laser frequency by applying an RF signal to the bias-Tee. By locking the laser frequency onto the sideband resonance, the laser frequency is properly adjusted for the experiment. The lockpoint of this laser is manipulated by changing the driving frequency of the bias-Tee.

#### 2.7 Stark-Ionization Detector for the Main Experiment

The Stark-ionization detector is shown in Figure 2.14. The energy-level diagram of the detection scheme is also shown. The simulation and design of the detector is done by Daniel Fitzakerly. Pulsed 1083-, 447- and 1532-nm lasers (Sections 2.5.2, 2.6.1, and 2.6.2) are combined and sent through the 14-mm microwave coaxial airline. Atoms that have undergone the microwave transition are excited up to the  $18^{3}P_{2}$  state inside the 14-mm microwave coaxial airline. The  $18^{3}P_{2}$  Rydberg state lives long enough (~ 6  $\mu$ s) to allow the atoms to exit the coaxial airline before a significant fraction decays down to lower-energy states. A high-voltage wire grid composed of five pairs of 50- $\mu$ m-diameter wires is positioned at the exit of the airline.



Figure 2.14: Stark-ionization detector. A number is assigned to each wire for convenience. Atoms excited up to 18P states are ionized in the area within wires 1 to 4. They are then guided by wires 5 to 10 into the copper slit. The number of ions passing through the copper slit is counted by the CEM detector.

An electric field applied by four wires (wires 1 to 4 in Figure 2.14) ionizes the  $18^{3}P_{2}$ atoms and accelerates the resulting ions towards the CEM. Six wires (wires 5 to 10 in Figure 2.14), positioned above the main ionizing wire grid, guide the ions into a 1-mm-wide slit machined into a copper plate. Table 2.3 shows the typical operation voltage setting of the wire grid. The high voltages are applied using two multichannel high-voltage power supplies (CAEN R1471ETD 8-channel and

HV part	1	2	3	4	5	6	7	8	9	10	$\mathrm{Cu}_{\mathrm{slit}}$	CEM
PS channel	ETD0	ETD1	ETD2	ETD3	ET0	ET1	ETD4	ETD5	ET2	ET3	ETD4	ETD5
voltage setting [V]	+1850	+1970	-2260	-1900	-750	-50	+280	+200	-100	-200	-1750	-1000

Table 2.3: Ionizer wire-grid voltage setting. HV part describes the part of the ionizer in Figure 2.14, PS channel are the power supply channels (ETD for R1741ETD and ET for R1740ET). The number after ETD and ET indicates the channel number of the power supply.

R1470ET 4-channel power supplies) The number of ions that passes through the copper slit is measured using a CEM detector. The CEM detector is particularly well suited for the ion detection because of its almost-unity ion detection efficiency and a gain factor which allows the detected signal to rise above the inherent noise floor for current detection. In this detection scheme, the main source of the background signal is collisionally ionized helium atoms and background gas molecules [46]. The background ion counts increase linearly as a function of the chamber pressure, so it is important to maintain the lowest pressure possible. The ionizer is designed such that the Ryderg atoms are ionized very locally, and ions created outside of the main ionization region are deflected away from the copper slit. This design greatly reduces the chance of background ions being detected by the CEM. The low background level and the high detection efficiency enabled us to achieve shot-noise limited detection.

Figure 2.15 shows a Fourier-transformed CEM signal. The nearly-frequency-



Figure 2.15: Fourier transformed CEM signal (see Section 2.11.1.2). The pink rectangle indicates the detected signal. The flat broadband noise spectrum indicates shot-noise limited detection if the FOSOF frequency is tuned away from the noise peaks in the spectrum.

independent noise floor shown is due to shot noise, and the peak shown in pink is the detected signal (see Section 2.11.1.2). The noise is dominated by the shot-noise of the signal itself. The other peaks in the Fourier-transformed signal are due to specific noise sources, such as harmonics of 60 Hz.

# 2.8 Optical Pumping of $2^{3}S_{1}$ state

Figure 2.16 illustrates the optical pumping process of the  $2^{3}S_{1}$  states. The atoms in  $2^{3}S_{1}$  state are optically pumped into either  $m_{J}$ =+1 or  $m_{J}$ =-1 state using the



Figure 2.16: Optical pumping of  $2^{3}S_{1}$  states. Magnetic sublevels of  $2^{3}S_{1}$  states are equally populated before optical pumping. The pumping direction is determined by the circular polarization of the pumping laser. Small dots in the figure indicate left-over population after optical pumping.

1083-nm laser tuned to the  $2^{3}S_{1}$ -to- $2^{3}P_{2}$  transition (OP in Figures 2.2 and 2.5.1) before they enter the main experiment region. The optical pumping ensures a clean experimental environment where only intended transitions are driven by the 1083-nm laser pulse (A in Figure 2.2). Optical pumping also increases the number of atoms that can be used for the experiment by a factor of 3 because the three magnetic sublevels of the  $2^{3}S_{1}$  state are initially equally populated. The handedness of the circular polarization ( $\sigma^{+}$  or  $\sigma^{-}$  polarizations) that determines the direction of the optical pumping is changed by turning a quarter-wave plate by 90 degrees ( $\lambda/4$  after the fiber-EOM in Figure 2.8). Almost all of the population in the  $2^{3}S_{1}$ 



Figure 2.17: Expected lines of  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  Transition. Panel (a) shows the energy level diagram with possible transitions. Note that the  $2^{3}S_{1}$  ( $m_{J} = 0$ )-to- $2^{3}P_{1}$  ( $m_{J} = 0$ ) is a forbidden transition. In a 25-G field, the transitions are expected to shift as shown in (b).

states is transferred into either the  $m_J = -1$  or  $m_J = +1$  state depending on the laser polarization. Half of the experimental data is taken with the optical pumping configured for the  $m_J = -1$  state and the other half is for the  $m_J = +1$  state, to test for any detection-state-dependent systematic effects. An EOM is used to ensure that the optical pumping works efficiently for a wide range of magnetic fields. The EOM driving RF frequency is changed for different magnetic field settings of the experiment (Section 2.10.3).

The efficiency of the optical pumping process is tested by sweeping the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  laser frequency (laser A in Figure 2.14) while observing the Stark-ionization detection and observing the signal strength of possible transitions, as shown in Figure 2.17(b). The signal size of each of the possible transitions indicates the



Figure 2.18: Experimental observation of optical pumping. The figure shows frequency scans of the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  laser. The laser frequency increases from left to right in the figure. Panels (a) and (c) show how the population is transferred with optical pumping into the  $2^{3}S_{1}(m_{J}=-1)$  and  $2^{3}S_{1}(m_{J}=+1)$  states, respectively. Panel (b) shows the distribution of population without optical pumping. The red circles indicate the population left behind due to the imperfect laser polarization.

population in each magnetic sublevel of the  $2^{3}S_{1}$  state. For this test, the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$ laser is intentionally set to elliptical polarization to drive every possible transition in the system, and a large magnetic field ( $\sim 25 \,\mathrm{G}$ ) is applied to the experiment region to Zeeman shift the transitions by a large amount, so that each transition is well resolved. The energy-level diagram of the possible transitions and expected lines as a function of the laser frequency (for a 25-G field) are shown in Figure 2.17. When all of the population is transferred into the  $2^{3}S_{1}(m_{J}=+1)$  state, only lines 1 and 3 are detectable. Only lines 4 and 6 are detectable when atoms are pumped into the  $2^{3}S_{1}(m_{J}=-1)$  state. Figure 2.18 shows the experimental verification for optical pumping. Frequency scans of the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  laser are shown. Figure 2.18(b) shows the transitions without optical pumping. All magnetic sublevels of  $2^{3}S_{1}$  are occupied; therefore, all of the six transitions are visible. Figures 2.18(c) and 2.18(a)indicate the population with optical pumping. Two dominant peaks are visible in these two plots, as expected. The much smaller peaks inside of the red circles indicate left-over populations after the optical pumping due to an imperfect laser polarization. Note that these data were taken at the early stage of the experiment, and further improvements on the optical pumping quality were made later in the experiment. With the improved optical pumping system,  $\sim 99\%$  pumping efficiency was achieved.

# 2.9 Two-Dimensional Magneto-Optical Trap (2DMOT)

The divergence of the metastable helium beam leads to a significant loss in the number of atoms that participate in the main experiment. In the current experiment, a two-dimensional magneto-optical trap (2DMOT) is used to intensify the metastable helium beam. A significant improvement in the signal-to-noise ratio (SNR) is realized. The theoretical framework of the method is well described in the literature [47–49], so only technical details are presented in this section.

#### 2.9.1 2DMOT Setup

Figure 2.19 shows the 2DMOT setup. The inset in Figure 2.19 shows the cross section of the 2DMOT setup with magnetic field lines and laser polarizations. The setup consists of two 10-cm-long cooling sections that are separated by 5 cm (cooling lasers in Figure 2.19). The first section is positioned right after the skimmer hole, where atoms enter the 2DMOT chamber from the source. The role of the first cooling section is to trap as many atoms as possible before the beam expansion exceeds the spatial capture range of the 2DMOT. The second section, which is located 5 cm downstream from the first section, further focuses and concentrates the metastable atomic beam that are trapped in the first section, and it also allows for a small deflection of the beam. Four expanded 1083-nm laser beams that are



Figure 2.19: 2DMOT setup. A two-section 2DMOT is implemented. The inset shows the cross section of the 2DMOT with magnetic field lines and laser polarizations.
detuned by -20 MHz from the  $2^3\text{S}_1$ -to- $2^3\text{P}_2$  transition are used (Section 2.5.1). The polarization of each laser beam ( $\sigma^+$  or  $\sigma^-$ , as shown in Figure 2.19) is chosen appropriately for the 2DMOT operation.

The two-dimensional quadrupole magnetic field required for the 2DMOT operation is produced by four 30-cm-long permanent bar-magnets [49] that are magnetized along their widths. The field within the cooling region is measured and mapped using a 3-axis Gaussmeter (Lakeshore 460 with probe MMZ-2508-UH). The vector plot in Figure 2.20(a) is constructed using the measured field. Figures 2.20(b) and 2.20(c) show the magnitudes of the magnetic fields along the x and z axes (the coordinate system is shown in Figure 2.19). Over the probed area of  $\pm 3 \text{ mm}$  from the beam axis, the magnetic field varies linearly along both axes. The data are fit to a linear model and the field gradients were found to be  $13.8\pm0.1$  and  $13.74\pm0.04$ Gauss/mm along the x and z axes, respectively.

The number of atoms that successfully pass through the entrance slit at the microwave region is occasionally checked with a Faraday cup on a translation stage that is installed between the main experiment chamber and the laser-locking chamber. The ion signal from the locking chamber and the TOF signal from the atom speed measurement chamber act as constant monitors of the 2DMOT operation.



Figure 2.20: Magnetic field generated by the bar-magnets of Figure 2.19. Panel (a) shows the vector plot constructed from the measured fields. Panels (b) and (c) show the measured fields along the centre axes. The data is fit to a linear function to determine the field gradient, and it was found to be  $\approx 13.8 \text{ Gauss/mm}$  in both directions

## 2.9.2 Simulations of Atomic Trajectories

Using the geometry and fields described in the previous section, simple simulations were performed to estimate the operating parameters of the 2DMOT and to predict the atomic trajectories. The helium atoms emerging from the source have an initial diameter of 1 mm, and a uniform distribution of atoms within that area is assumed. The speed distribution of the atoms is estimated by the time-of-flight data described in Section 2.4. The initial speed of an individual atom is chosen using the probability distribution function described in [35]. An initial beam divergence of 50 mrad is assumed. The cooling laser is assumed to have an elongated Gaussian intensity profile. Figure 2.21 shows the simulated atomic trajectories with and without application of the 2DMOT to the beam. Trajectories indicated in green are without application of the 2DMOT. The blue lines are the simulated trajectories within the cooling section. The pink lines are the simulated trajectories after the atoms exit the 2DMOT section. Figures 2.21(a) and 2.21(b) show a significant compression of atoms within the 2DMOT region. Figures 2.21(c) and 2.21(d) indicate that the atomic transverse velocity components  $V_x$  and  $V_z$  are suppressed further by including the second cooling section. Figure 2.22 shows the simulated spatial distribution of atoms at the 0.5-mm-by-5-mm entrance slit to the airline. The green rectangle represents the slit, and the figure shows that the simulation predicts that most of the atoms enter this slit with the 2DMOT included in the system.



Figure 2.21: Simulation results of atomic trajectories. a) and b) show the atomic trajectory within the cooling region in the x and z directions. c) and d) show trajectory in the velocity space  $V_x$  and  $V_z$ . Panels e) and f) are the simulated trajectories after the cooling region. The blue trajectories indicate atoms that experience the cooling process. The green trajectories are without the 2DMOT applied. Pink points are the trajectories after the 2DMOT section.



Figure 2.22: The simulated distribution of atoms at the microwave region. The red points indicate the distribution without application of the 2DMOT, and the blue points indicate the distribution with the 2DMOT. The green rectangle at the centre of the plot indicates the size of the entrance slit.

## 2.9.3 Improvements to the Experiment

The 2DMOT significantly increases the number of atoms that go through the entrance slit located at the main experiment region. The 2DMOT increased the metastable atom flux to  $7 \times 10^{12}$  He<sup>\*</sup>/cm<sup>2</sup>/s. Figure 2.23 shows the TOF signal (obtained using the chopper in Figure 2.6) recorded at the end of the beamline to illustrate the signal gain with the 2DMOT included in the system. In this plot, the signal height increased by about a factor of 25 and the speed distribution is shifted towards lower speeds. The number of atoms detected by the CEM is proportional to the area under the curve. The actual gain in the FOSOF signal of atoms is significantly more than the estimated factor of 25, at least in part due to the fact that slower atoms lead to larger signals. For the actual FOSOF experiment signal (Stark ionization signal described in Section 2.7), a signal gain of about a factor of 60 was observed. The large signal gain allows for a extensive study of systematic effects in a reasonable time frame.

The larger atomic flux along the beamline ensures a better SNR for the ion signal in the 1532-nm laser-locking chamber. As a result, the power of all lasers used in the production of the Rydberg atoms in the locking chamber can be reduced and a larger fraction of the laser power can be allocated for the main experiment.



Figure 2.23: The TOF signal with and without the 2DMOT applied to the helium beam. A significant increase in signal size is observed. A shift in the arrival time is also seen in the plot. This shift is because the 2DMOT works better for the atoms moving slowly and it therefore favours these slower atoms.

## 2.10 Magnetic Field System

The magnetic field system for the current experiment is shown in Figure 2.24. Four pairs of nested coils are used to control the magnetic field around the experiment region. Their geometries and current-to-field conversion factors (k) are summarized in Table 2.4. Each pair of coils is characterized by measuring the field as a function of applied current using a three-axis gaussmeter at the approximate location of the experiment (the laser interaction region in Figure 2.14). The current applied to each pair of coils is monitored with a precision shunt resistor (IET Labs, DCCS/0.01).



Figure 2.24: Coils used in the experiment. Coils in red are the residual field cancelling coils, and coils in green are the main field coils. These coils are centred on the intersection of the atomic beam axis and the airline axis of Figure 2.1.

## 2.10.1 Residual Field Cancelling Coils

The three pairs of coils (the red square coils in Figure 2.24) oriented along the x-, y-, and z-axis, designed based on [50], are used to cancel the three components of the background magnetic field around the experiment. These coils surround the main experiment chamber. The current to each pair of coils is supplied by

	Main Helmholtz coils	$B_x$ -coils	$B_y$ -coils	$B_z$ -coils
Shape	Circular	Square	Square	Square
Dimensions	$20\mathrm{cm}\  imes 10\mathrm{cm}$	$73\mathrm{cm}{\times}73\mathrm{cm}{\times}39\mathrm{cm}$	$78\mathrm{cm} \times 78\mathrm{cm} \times 43\mathrm{cm}$	$83\mathrm{cm} \times 83\mathrm{cm} \times 45\mathrm{cm}$
$k \; [Gauss/A]$	$10.866 {\pm} 0.010$	$3.470 {\pm} 0.010$	$3.241 {\pm} 0.010$	$3.074 {\pm} 0.010$

Table 2.4: Summary of magnetic field coil parameters. The current-to-field conversion factor k is determined by measuring the field as a function of applied current. Dimensions are given in (coil radius)×(coil separation) for the main experiment coils, and (side length)×(side length)×(coil separation) for the background field cancelling coils.

a triple-output DC power supply (Keithley 2231A-30-3). Each component of the background magnetic field is cancelled to approximately 10 mG. The uncertainty of 10 mG is assigned to each residual field component due to the fluctuation of the gaussmeter reading and the uncertainty associated with the position of the probe.

## 2.10.2 Main Helmholtz Coils

The pair of green coils in Figure 2.24 applies a magnetic field to lift the degeneracy of the magnetic sublevels of the  $2^{3}P_{1}$  state, as well as to test for magnetic field related systematic effects. Each coil is made of 123 turns of 2.6-mm enamel-coated copper wire and has a radius of 20 cm. This pair of coils is wound around an aluminium mount that is designed to host the microwave airline at the centre of the coils, where the magnetic field is most uniform. Since the coils are installed inside the vacuum



Figure 2.25: Magnetic field as a function of applied current. The data is fit to a linear model to extract the value of k = B/I. Uncertainties are smaller than the plotted points.

chamber, where the heat generated by the coils cannot be dissipated by convection, chilled water is fed into the vacuum chamber through a VCR feedthrough to cool the entire coil mount. The current to the coils is supplied by a precision current supply (Agilent E3648A). The magnetic field produced by the coils is proportional to the applied current I: B = kI, and a precise determination of the k-value is necessary to apply appropriate corrections to the experimental data. The value of 10.866 G/A listed in the Table 2.4 is determined to a precision of 0.001 G/A from the linear fit shown in Figure 2.25; however, the uncertainty associated with the probe positioning seems to dominates over the fit uncertainty (the position of the

	Optical pumping	1083-nm laser pulse	447-nm laser pulse	1532-nm laser pulse	
Transition	$2^3S_1$ -to- $2^3P_2$	$2^3S_1$ -to- $2^3P_1$	$2^{3}P_{2}$ -to- $4^{3}D_{3}$	$4^{3}D_{3}$ -to- $18^{3}P_{2}$	
Frequency shifting element	EOM	AOM	AOM	bias-Tee	
RF source	Rigol 4162	SynthUSBII	SynthUSBII	Marconi2022	

Table 2.5: Instruments for shifting laser frequencies to compensate for Zeeman shifts. The table summarizes the devices used to compensate for the first-order Zeeman shift for different laser applications. The transition used in each application is also shown. The frequency of the RF is varied for different magnetic field settings. Each entry in the RF source row is the name of the RF generator model.

experiment location cannot be known exactly, and the positioning of the probe is only approximate). An uncertainty of  $10 \,\mathrm{mG/A}$  is assigned to the k value of this pair of coils. The accuracy of k is re-evaluated using the experimental data in Section 4.1.2.

## 2.10.3 Laser Frequency Settings for Various Magnetic Fields

Laser frequencies need to be adjusted for different magnetic field settings to compensate for the first-order Zeeman shifts. Table 2.5 shows the laser applications and devices used to shift the laser frequencies. RF signals from the instruments shown in the table are fed into the frequency shifting elements. Table 2.6 shows the RF setting of each frequency shifting element for different magnetic field settings. Values in Table 2.6(a) are used when the optical pumping is configured to pump the  $2^{3}S_{1}$  population into the  $m_{J}$ =+1 state and Table 2.6(b) for the  $m_{J}$ =-1 state.

B [G]	I [A]	OP1 EOM [MHz]	OP2 EOM [MHz]	1083-nm AOM $[\mathrm{MHz}]$	447-nm AOM [MHz]	1532-nm bias-Tee [MHz]
5	0.461	30	25	196.5	196.0	178.9
10	0.922	40	40	193.0	194.0	178.7
15	1.384	50	55	189.5	192.1	178.5
20	1.845	60	70	186.0	212.5	198.4
25	2.306	70	85	182.5	212.5	195.3
30	2.767	80	100	179.0	212.5	192.1
35	3.228	90	115	175.5	212.5	189.0

(a) RF generator settings when optical pumping is configured for the  $m_J = +1$  state.

B [G]	I [A]	OP1 EOM [MHz]	OP2 EOM [MHz]	1083-nm AOM [MHz]	447-nm AOM [MHz]	1532-nm bias-Tee [MHz]
5	0.461	12.5	0	203.5	196.0	178.9
10	0.922	25.0	10	207.0	194.0	178.7
15	1.384	37.5	20	210.5	192.1	178.5
20	1.845	50.0	30	214.0	212.5	198.4
25	2.306	62.5	40	217.5	212.5	195.3
30	2.767	75.0	50	221.0	212.5	192.1
35	3.228	87.5	60	224.5	212.5	189.0

(b) RF generator settings when optical pumping is configured for the  $m_J = -1$ . state

Table 2.6: RF generator settings for different magnetic field settings. (a) shows the RF settings when optical pumping is configured for the  $m_J = +1$  state. (b) is for the  $m_J = -1$  state. OP1 and OP2 indicate the channel 1 and channel 2 outputs of the 2-channel Rigol 4162 arbitrary waveform generator, respectively.

The RF settings are found experimentally by optimizing the ionizer signal (Section

2.7) for each magnetic field setting.

# 2.11 Microwave and Laser Pulsing Systems for the Separated-Oscillatory-Fields Experiment

## 2.11.1 Separated-Oscillatory-Fields Technique

The present experiment exploits the newly developed frequency-offset separatedoscillatory-fields (FOSOF) technique [34], and is the first demonstration of the technique. The FOSOF technique is a variation of the Ramsey separated-oscillatoryfields (SOF) technique. The objective of this section is to provide an intuitive understanding of the SOF and FOSOF techniques. A brief mathematical description of the SOF and FOSOF lineshapes is given in Section 3.1.

## 2.11.1.1 Separated Oscillatory Fields on 2<sup>3</sup>P<sub>1</sub>-to-2<sup>3</sup>P<sub>2</sub> Transition

Ever since Norman Ramsey's invention of separated-oscillatory-fields technique [51], it has been one of the most widely used methods in the field of precision measurements. The method uses an interference phenomenon to effectively narrow the transition linewidth to acquire higher resolution in measuring a transition linecentre in a quantum system. The natural linewidth, a resolution limit on a typical spectroscopy setup, can be overcome using this SOF interference, and the resulting sub-natural linewidth is used to achieve greater spectroscopic precision.

The two states involved in our measurement are the  $2^{3}P_{1}$  and  $2^{3}P_{2}$  states. Figure



Figure 2.26: SOF overview. Before atoms interact with the first microwave pulse, all of the population is in the  $2^{3}P_{1}$  state. Two excitation paths (path 1 and path 2) accumulate different quantum-mechanical phases and the amplitudes of the two paths interfere.

2.26 shows a SOF scheme for the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition. At time t = 0, all atoms in the two-level system are in the  $2^{3}P_{1}$  state. In an SOF experiment, two temporally separated microwave pulses with a pulse duration D are applied. The first microwave pulse puts the system into a superposition of the  $2^{3}P_{1}$  and  $2^{3}P_{2}$  states. Some time T after the first pulse, a second microwave pulse is applied. During the time T, atoms in the  $2^{3}P_{1}$  and  $2^{3}P_{2}$  states accumulate different quantum-mechanical phases. The probability amplitudes with different evolution phase factors interfere when recombined by the second pulse. Atoms in the  $2^{3}P_{2}$  state are detected after the end of the second microwave pulse.

The probability of finding atoms in the  $2^{3}P_{2}$  state after the second microwave pulse can be derived (for microwave powers well below saturation) from timedependent perturbation theory, and it can be written as

$$P(\Delta\omega) = \left|\frac{VD}{2}\right|^2 \cos^2\left(\frac{\Delta\omega T}{2} + \phi\right) \operatorname{sinc}^2\left(\frac{\Delta\omega D}{2}\right), \qquad (2.4)$$

where  $\Delta \omega = \omega - \omega_0 = 2\pi (f - f_0)$ , V is the matrix element of the transition, and  $\phi = \phi_2 - \phi_1$  is the relative phase between the two microwave pulses.

In a typical SOF experiment, the relative phase between two pulses is toggled between  $\phi_2 - \phi_1 = 0$  and  $\phi_2 - \phi_1 = 180^\circ$ , and the resulting signals are subtracted to obtain an interference signal that is fit to an analytical solution to the SOF model for linecentre determination. Figure 2.27(a) shows the fraction of population expected by Equation 2.4 with T = 300 ns and D = 100 ns. An exponential decay factor of  $e^{-(T+D)\gamma}$ , where  $\gamma = 1/\tau$  with  $\tau = 98$  ns, is included to calculate the population fraction that does not radiatively decay before the end of the second pulse. Both  $\phi = 0^\circ$  and  $\phi = 180^\circ$  interference patterns are shown. In the experiments performed by J. S. Borbely et. al. [27] in 2009, the relative phase between the microwave pulses was toggled between  $0^\circ$  and  $180^\circ$  using a microwave delay line, and the signal at the toggle frequency was recorded to obtain the signal shown in Figure 2.27(b). The width of the central interference fringe is given by 1/(2T).



Figure 2.27: SOF interference signals for T=300 ns and D=100 ns. Signals  $S_0$  and  $S_{180}$  are subtracted to obtain the interference shown in (b).

## 2.11.1.2 FOSOF Technique

The FOSOF technique used in the current experiment is a modified SOF technique in which the frequencies of the two microwave pulses are slightly offset from each other [34]. For the FOSOF technique, two microwave generators are used to prepare the frequency-offset microwave pulses (at frequencies  $f_1 = f + \delta f$  and  $f_2 = f - \delta f$ ). The microwave frequency f is offset by  $\pm \delta f$ . The frequency offset causes the relative phase between the two microwave pulses to vary continuously in time. As a result, the SOF interference continuously cycles between constructive and destructive interference at the frequency  $2\delta f$ . Figure 2.28(a) shows snapshots of the SOF interference for different times. In the figure, time steps of  $0.25/(2\delta f)$  are used (the relative phase changes by  $\pi/2$  in this time step). At time t = 0 in the figure, the two pulses are in phase. As the time progress, the shape of the interference pattern changes continuously, and the  $2^{3}P_{2}$  population at a particular applied microwave frequency changes sinusoidally. Figure 2.28(b) shows this oscillation of  $2^{3}P_{2}$  population as a function of time. The oscillations at three different frequencies are shown. In all three cases, the population oscillates at the frequency  $2\delta f$ , but have different phases depending on the applied microwave frequency. The FOSOF technique measures this phase as a function of applied microwave frequency to determine the resonance linecentre. Since phase is a relative quantity, a stable



Figure 2.28: FOSOF signal progression in time. At time t=0, the two microwave pulses are in phase. As time progresses, the signal oscillates sinusoidally. The oscillations at three different frequencies are shown in (b). The oscillations have the same frequency  $2\delta f$ , but different phases.

reference with a constant phase needs to be supplied for all measurements to obtain phase differences. The reference sine wave is generated by combining the two microwave generator outputs. The power combination process produces a beat note between the two microwaves that oscillates at the frequency difference of  $|f_1 - f_2| = 2\delta f$ . The phase difference between the atomic and beat oscillations as a function of microwave frequency (Figure 2.30) gives the information necessary to determine the linecentre.

One of the major concerns about the FOSOF technique is a phase shift due to the frequency response of the microwave components or due to the detector used in the system. Each microwave component has a reflection coefficient, and the reflection causes interference between forward-going and reflected waves. The interference induces a frequency-dependent distortion in the phase and amplitude of the microwaves. The time constant of the detection system also contributes to a phase offset. To eliminate these effects, two experiments, denoted as experiment I and II, are performed. Figure 2.29 shows the timing diagrams for experiment I and II. In these experiments, the order of the microwave pulses seen by atoms is reversed, i.e., atoms interact with the pulse with frequency  $f + \delta f$  first in experiment I and  $f - \delta f$  first in experiment II. The sign of the FOSOF phase difference is opposite for experiment I and II. Subtraction of observed phase differences from experiments I and II cancels out the phase shifts due to the detector and microwave reflections.



Figure 2.29: FOSOF timing diagrams for experiment I and II. The order of microwave pulses are reversed between experiment I and II. The expected difference in FOSOF phase between experiment I and II is illustrated in Figure 2.30.

Figures 2.30(a), 2.30(b) and 2.30(c) show the FOSOF interference phases at three different microwave frequencies. Phase differences  $\Delta \theta_{\rm I}$  and  $\Delta \theta_{\rm II}$  are extracted in each frequency. Figure 2.30(d) shows the expected phase variation as a function of applied microwave frequency in experiment I and II. The two lines in the figure are subtracted to obtain a true lineshape. Time-dependent perturbation theory (TDPT) predicts a linear phase lineshape  $\Delta \theta = \Delta \omega T$  (where  $\Delta \omega = 2\pi (f - f_0)$ ) that crosses zero phase at the center of the resonance. However, a slight, but important, deviation from this prediction becomes apparent in solving the time-dependent Schrödinger equation for the FOSOF experiment. A brief theoretical framework of SOF and FOSOF using the time-dependent Schrödinger equation and its deviation from the simple TDPT prediction are described in Section 3.2.

There are a few notable advantages in using the FOSOF technique. First, in the TDPT regime, where the amplitude of the microwave field is small, the lineshape is linear and can be fit to a simple straight line to extract the linecentre. Second, cancellation of phase imperfections is possible by using two experiment configurations (I and II), whereas SOF requires four configurations (see [33] for details on the four configurations). Third, the offset frequency  $\delta f$  can be set to a frequency with the minimum noise in the Fourier spectrum of the signal to achieve the best signal-to-noise ratio (refer to Figure 2.15 for the Fourier-transformed FOSOF signal and noise spectrum). Finally, the FOSOF linecentre determination depends solely on the phase extraction from the oscillating signal. Amplitude noise in the signal (the laser frequency noise, acoustic noise, source stability, and so on) does not directly affect this phase measurement.



Figure 2.30: FOSOF phase determination scheme.  $\Delta \theta_{I}$  and  $\Delta \theta_{II}$  are extracted by taking the phase difference between the atomic FOSOF and beat signals. The phase extraction is illustrated in three different frequencies in (a), (b) and (c). The coloured solid and dashed lines indicate the atomic signals for experiment I and II, respectively, and the black dashed line is the beat reference signal. In (d) the TDPT lineshape in experiment I and II are drawn. Points on the lines illustrate the phases determined in (a). Here only 3 microwave frequencies are shown for illustration purposes, whereas the actual FOSOF measurements use a much larger number frequencies.

#### 2.11.2 Microwave System

#### 2.11.2.1 Microwave System Overview

Figure 2.31 illustrates the schematic of the microwave system. As described in Section 2.11.1.2, the FOSOF technique requires two microwave pulses whose frequencies are slightly offset from each other. Wiltron and HP microwave generators (Wiltron68169B and HP83640A) output CW microwaves with a small offset frequency  $f_1 = f + \delta f$  and  $f_2 = f - \delta f$ . The outputs from the two generators are sent to a temperature-stabilized enclosure in which various microwave components are mounted. The system in the enclosure generates the microwave pulses and the reference (beat note) sine wave required for the FOSOF experiment. The details on the enclosure will be described in Section 2.11.2.2. The microwave pulses generated in the temperature-stabilized enclosure are sent to the Alga 100W microwave amplifier. The amplified microwave pulses go through a circulator (JQL 6058545 in Figure 2.31) and the output of the circulator is coupled into the main experiment chamber through a type-N vacuum feedthrough. Inside the vacuum chamber (main experiment chamber of Figure 2.4), this feedthrough is connected to the 14-mm microwave coaxial airline, where atoms interact with the microwave fields (14-mm microwave airline in Figure 2.1). An 18-cm-long, 0.7-cm-diameter type-N coaxial cable is used to connect the vacuum side of the feedthrough and the microwave



Figure 2.31: Microwave system overview

region. One end of the airline is shorted to retro-reflect the microwave power. The reflected microwave power goes back to the circulator and the circulator redirects the reverse power into its third port, and thus protects the amplifier from the reverse power reflected from the short. The redirected reverse microwave power is attenuated by a 40-dB attenuator (Weinschel model 57-40-43). The attenuated microwave pulses go through a 10-dB bi-directional coupler. The power of the coupled outputs are measured using power detectors (Krytor 109A). The microwave pulses from the output port of the coupler is monitored on a digital oscilloscope (Tektronix DPO7354). The oscilloscope traces of the microwave pulses are used for monitoring the microwave pulse timing and simulations that model the atomic signal for the experiment. The power detector readings are used as an independent check of the microwave power, and are compared to the power measured using the oscilloscope.

## 2.11.2.2 Details of the Microwave Switching and FOSOF Beat Reference Generation

Figure 2.32(a) shows a schematic of the microwave system inside the temperaturestabilized enclosure in which microwave components are firmly attached to a temperature-stabilized aluminum breadboard. A 50- $\Omega$  power-resistor chain is used as a heater for temperature stabilization. The system consists of two microwave paths dedicated to switching and to reference-beat-signal generation.

The CW microwave outputs from the two generators are coupled into the enclosure. The power of each CW microwave input is first split by a power splitter (PS in Figure 2.32(a)). One of the outputs from each power splitter goes through a series of 25-dB isolators (ISO in Figure 2.32(a)) and is coupled into a power combiner (PC in Figure 2.32(a)). The power combiner combines the two inputs with the small frequency offset and it outputs a beat signal. A power detector (Kryter109A, PD in Figure 2.32(a)) is used to measure the beat signal. The power detector has a nonlinearity that becomes more significant for a lower power input. The nonlinearity distorts the reference sine wave around the nodes of the beat signal, causing higher harmonics to appear in its Fourier spectrum. A 30-dB attenuator (30dB in Figure 2.32(a)) is used at one of the inputs of the power combiner to offset the beat signal. The offset ensures a nearly linear operation of the power detector.

The other microwave paths from the first pair of power splitters go through high-isolation microwave switches (Mini-Circuits ZASWA-2-50DR) for pulsing (SW1 and SW2 in Figure 2.32(a)). A delay generator (SRS DG645) is used to control the switches. TTL signals from AB and CD outputs of the delay generator are sent to the TTL inputs of SW1 and SW2, respectively, in Figure 2.32(a). These TTL pulses determine the time-separation and duration of the microwave pulses used in the experiment. The pulses produced by SW1 and SW2 are then combined using a



(a) Temperature-stabilized FOSOF microwave switching system. Dashed and solid lines indicate the pulsed and CW microwave paths, respectively. PS:power splitter, PC:power combiner, ISO:25-dB isolator, SW:switch, 30dB:30-dB attenuator, PD:power detector.



(b) Schematic illustration of the microwave switching and FOSOF beat signal generation. The switching path generates a continuous series of microwave pulses whose frequency alternates between  $f + \delta f$  and  $f - \delta f$ . The figure shows the pulse sequence with the pulse separation and duration of 300 ns and 100 ns, respectively. The beat-note envelope oscillation is obtained by using a power detector.

Figure 2.32: Details of the temperature-stabilized switching and FOSOF reference signal generation.



Figure 2.33: Microwave coupling between the switching and beat generation systems. A small fraction of the microwave power used to generate the beat signal couples into the other input port of the power combiner. The microwave power eventually couples into the switching path, giving rise to an oscillation in the pulse amplitude. Dashed lines indicate the undesired coupling of microwaves. PS:power splitter and PC:power combiner.

power combiner. The output of the combiner is a continuous sequence of identical shaped pulses whose frequency alternates between  $f + \delta f$  and  $f - \delta f$  (see Figure 2.32(b)).

A high isolation is required between the switching and beat signal generation paths to avoid microwave coupling between the paths. The microwave coupling scheme is shown in Figure 2.33. Each power combiner/splitter in the system has a typical input/output isolation of 20 dB. A small CW microwave power in the  $f - \delta f$  beat signal generation path can couple into the the  $f + \delta f$  switching path (labelled switching  $f + \delta f$  in Figure 2.33) and vice versa. The coupling induces an interference between the CW  $f \pm \delta f$  and the pulsed  $f \mp \delta f$  microwaves and causes the pulse amplitude to oscillate at the same frequency as the beat signal oscillation. The pulse amplitude oscillation adds a constant phasor onto the FOSOF atomic phasor and causes a frequency-dependent oscillation in the FOSOF phase. The oscillation distorts the FOSOF lineshape and thus introduces a systematic effect. The isolators and attenuator installed in the beat signal generation paths provide 80-dB isolation between the two paths. Including the isolations from the two power combiners that the microwaves have to go through to couple into the switching path, the total isolation between the two systems becomes 120 dB. The 120-dB suppression of microwave coupling makes the lineshape distortion negligibly small, and therefore it can be ignored for the experimental data analysis.

## 2.11.2.3 Details of the Microwave Region

Figure 2.34 shows the microwave-coaxial airline. The rest of the microwave system is shown in Figure 2.31. 14-mm (General Radio GR900 series) microwave components are used for the construction to ensure a good mechanical stability and a low voltage standing-wave ratio (VSWR). Typical VSWR specifications on these components range from 1.0005 to 1.005. Microwave pulses are fed into a type-N-to-14-mm adaptor (GR900-QNJ type-N-to-14-mm adaptor in Figure 2.34). The pulses are then coupled into a 14-mm elbow (GR900-EL elbow in Figure 2.34). The output-end of the elbow is attached to a 15-cm precision airline (GR900-LZ15 15-cm airline in Figure 2.34) with a 0.5-mm-by-5-mm slit where atoms enter the microwave region



Figure 2.34: Details of the microwave region. (a) shows the overview of the microwave region. The helium beam is illustrated with the pink arrow. (b) is the cross-sectional view of the coaxial airline. (c) is the cross-sectional view showing the internal structure of the airline. The main components of the microwave regions are labelled in red.

and interact with the microwave pulses. The other end of the airline is shorted (GR900-WN microwave short in Figure 2.34) at a half-wavelength (6.543 cm) away from the atom-microwave interaction location. The microwaves are reflected from the short, and the interference between the incoming and reflected microwaves creates a standing wave which introduces a magnetic field anti-node at the interaction location (the transition of interest is a magnetic-dipole transition). This reflection effectively quadruples the microwave intensity seen by the atoms. The reflected microwave pulses follow the path of the incoming microwaves and exit from the microwave region. 2-mm holes are machined at the short and elbow for laser pulses to enter and exit the microwave region (Figure 2.34). The laser pulses enter from the short and exit at the elbow. Two laser-access holes machined at the downstream and upstream side of the inner conductor allow for experiments at two different locations in the microwave region to test for possible position-dependent systematic effects (Section 4.4.1).

## 2.11.3 Laser Switching System

As described in Sections 2.5.2, 2.6.1, and 2.6.2, laser pulses are generated by sending pulsed RF signals to acousto-optic modulators (AOMs). Figure 2.35 illustrates the RF system for the laser pulsing. A delay generator (SRS DG645) generates three TTL control signals for switching. The delay generator is externally triggered by a



Figure 2.35: RF system for the AOM laser pulsing. CW RF signals are pulsed using switches and an AOM driver. TTL control signals for the RF switches and AOM driver are generated by the SRS DG645 delay generator which is externally triggered by the delay generator for the microwave switching. The pulsed RF signals are sent to the AOMs for laser pulsing (Sections 2.5.2, 2.6.1, and 2.6.2).

TTL signal from the EF output of the other delay generator used for microwave switching. A fixed-frequency AOM driver (Brimrose FFF-200-B2(50)-F1), which includes a switch and an amplifier, takes the EF output from the delay generator and outputs 1-W RF pulses. The output of the driver is used to pulse the 1532-nm laser (Section 2.6.2). RF pulses for the 1083- and 447-nm lasers are generated by two identical systems (shown in the lower part of Figure 2.35). A USB-controlled RF synthesizer (Windfreak SynthUSBII) outputs a 0-dBm RF signal whose frequency is tuned based on the magnetic field setting of the experiment (Section 2.10.3). The RF signal goes through a low-pass filter for higher harmonics suppression. The filtered signal then goes through two RF switches (Mini-Circuits ZYSW A-2-50DR) connected in series. Both the switches take the same TTL signal from the delay generator (AB and CD outputs for 1083- and 447-nm lasers, respectively). Two switches are used to ensure a high extinction ratio of the pulsed RF signal. The pulsed RF signal is amplified by a 1-W RF amplifier (Mini-Circuits ZHL-2-8-S+) and then is sent to the AOM.

## 2.11.4 Microwave- and Laser-Pulse Timings

Figure 2.36 shows the setup for adjusting and monitoring the experiment timing. Figure 2.37 is the timing diagram of the delay generator outputs for a particular experiment setting. The microwave and laser pulses generated by using two delay



Figure 2.36: Experiment timing monitoring. The microwave pulses generated in the microwave system are sent to the microwave region and the reflected microwave pulses are sent to the channel 1 of the oscilloscope. The overlapped laser pulses are split using dichronic mirrors (DM) after passing through the microwave region and monitored on channel 2 to channel 4 of the oscilloscope. M:mirror, PDs:photodiodes.

generators (SRS DG645 delay generator 1 and 2 in Figure 2.36) are monitored on a digital oscilloscope. The reflected microwave pulses are sent to channel 1 of the oscilloscope. Laser pulses are split using dichroic mirrors (DM in Figure 2.36) after passing through the microwave region. The pulse shape and timing of each laser are monitored on a photodiode. Channels 2 to 4 are dedicated for the laser pulse monitoring. The microwave and laser pulses travel from the interaction location to the measurement location, and the travel time leads to a time delay of the oscilloscope trace. The cable length of each monitoring system is adjusted such that the oscilloscope trace approximately represents the true experiment timing that



Figure 2.37: Microwave and laser pulse timing diagram for T = 400 ns and D = 100 ns experiment. The delay generator 1 outputs the TTL pulses shown in (a). The EF output of this delay generator is used to trigger the delay generator used for pulsing lasers. TTL pulses from delay generator 2 are shown in (b) and (d). The trigger pulse (EF1) in (a) is used to shift the experiment timing from (b) to (d) and vice versa. (c) and (e) show the combined experiment sequence for the experiment I and II, respectively.  $t_D$  indicates the insertion delay.

atoms experience.

The delay generator 1 outputs the TTL pulses shown in Figure 2.37(a). This generator is internally triggered. The combination of AB and CD outputs (AB1 and CD1 in Figure 2.37(a)) produces a continuous series of microwave pulses whose frequency alternates between  $f + \delta f$  and  $f - \delta f$ . The EF output (EF1 in Figure 2.37(a)) of the delay generator 1 generates a pulse whose duration corresponds to the pulse separation T (400 ns in the case of Figure 2.37). This pulse is sent to the external trigger input of the delay generator 2. Once the delay generator 2 acquires the trigger signal, it starts the delay cycle after an insertion delay ( $t_D$  in Figure 2.37(b) and 2.37(d)). The AB, CD, and EF outputs are used to produce the laser pulses for the experiment. Since each of the AOMs used for the laser pulsing has a propagation delay (A time delay caused by the propagation of RF pulses inside the AOM crystal), the delay settings were determined for each experiment timing by adjusting the laser pulses based on the oscilloscope trace of the microwave pulses. The experiment reversal (described in Section 2.11.1.2 and illustrated as a change in pulse timing between Figures 2.37(b) and 2.37(d) that changes the order of the microwave pulses seen by the atoms (atoms see the  $f+\delta f$  pulse first in experiment I and the  $f - \delta f$  pulse first in experiment II) is performed by toggling the trigger edge setting of the delay generator 2. A rising edge trigger setting is used in experiment I and a falling edge trigger setting is used in experiment II. This


Figure 2.38: FOSOF experiment timing parameters. T changes the width of the interference fringe, D changes the spectral width of the microwave pulse. T and D range from 300 to 900 ns and from 50 to 200 ns, respectively. Total of 18 different combinations of T and D are used in the experiment.

experiment reversal method does not involve any change in the microwave system (only of the timing of the laser pulses); therefore, it ensures a stable operation of the microwave components throughout the experiment (the microwave components perform the same tasks at the same rate throughout the experiment).

#### 2.11.5 Experiment Timing Parameters

Figure 2.38 shows the experiment timing parameters that are varied in the current experiment. The experiment timing parameters T and D are denoted as (T,D). Table 2.7 shows all the (T,D) combinations and corresponding delay settings of the delay generators. The major advantage in using the SOF (or FOSOF) technique is the ability to vary the transition lineshape by changing the pulse separation



Figure 2.39: Synchronization of the 10-MHz timebases of instruments.

T and duration D. The (T,D) dependence of the SOF lineshape is described (in the low-power limit) by Equation 2.4. The width of the SOF interference fringe is proportional to 1/(2T), and the width of the sinc envelope of the transition is 1/D. Consistent results in different lineshapes confirm the level of understanding of the measurements. Various (T,D) combinations are investigated in the current experiment.

#### 2.11.6 Synchronization of Instruments

Figure 2.39 shows the timebase synchronization of the instruments used in the experiment. The 10-MHz internal timebase of the Wiltron microwave generator is used as a timebase for the experimental system. The 10-MHz output of the Wiltron generator is daisy-chained with the instruments shown in the figure. Since the oscilloscope only has a 10-MHz input, the output of the digitizer is split into two arms, and one of them is fed into the oscilloscope. The other arm of the digitizer

Timing Parameters		DG645 delay generator 1								DG645 delay generator 2					
Т	D	Trigger Rate [Hz]	А	В	С	D	Е	F	А	В	С	D	Е	F	
300	50	1666666.66667	50	52	350	53	100	300	150	15	0	50	80	80	
300	100	1666666.66667	50	103	350	103	100	300	150	15	50	50	130	80	
300	150	1666666.66667	25	152	325	153	100	300	125	15	75	50	155	80	
375	120	1333333.33333	50	122	425	123	175	375	225	15	220	50	150	80	
400	50	1250000.00000	50	52	450	53	200	400	250	15	200	50	80	80	
400	100	1250000.00000	50	103	450	103	200	400	250	15	250	50	130	80	
400	200	1250000.00000	50	203	450	203	200	400	250	15	350	50	230	80	
450	150	1111111.11111	50	152	500	153	250	450	300	15	400	50	180	80	
500	50	1000000.00000	50	52	550	53	300	500	350	15	400	50	80	80	
500	100	1000000.00000	50	103	550	103	300	500	350	15	450	50	130	80	
500	125	1000000.00000	50	127	550	128	300	500	350	15	475	50	155	80	
600	50	833333.33333	50	52	650	53	400	600	450	15	600	50	80	80	
600	100	833333.33333	50	103	650	103	400	600	450	15	650	50	130	80	
600	150	833333.33333	50	152	650	153	400	600	450	15	700	50	180	80	
600	200	833333.33333	50	203	650	203	500	600	450	15	750	50	230	80	
700	100	714285.71429	50	103	750	103	500	700	550	15	850	50	130	80	
800	100	625000.00000	50	103	850	103	600	800	650	15	1050	50	130	80	
900	100	555555.55556	50	103	950	103	700	900	750	15	1250	50	130	80	

Table 2.7: (T,D) combinations and corresponding timing settings of the two delay generators used in the experiment. T, D, and the delay settings (A to F) are measured in ns. The internal trigger rate of the delay generator 1 is set to 1/(2T). Delay settings A, C, and E are the time measured with respect to the start of the delay cycle. Settings B, D, and F define the TTL pulse duration. Settings shown in the table produce the pulses described in Figure 2.37.

10-MHz output is sent to channel A of a frequency counter (TTi TF960) to monitor the timebase of the Wiltron generator. A rubidium clock (Frequency Electronics, Inc. FE-5680A) is used as an external reference for the frequency counter. A 10-MHz output of a GPS-disciplined clock (Trimble Thunderbolt E) is monitored on channel B of the frequency counter to verify the Rb clock frequency.

## 2.12 Data Acquisition

Figure 2.40 shows the schematic overview of the data acquisition system. The data acquisition system of the experiment can be divided into three groups: the FOSOF atomic and reference beat signals acquisition, the microwave and laser pulse monitoring, and the experimental parameter logging. This section describes each component of the data acquisition system.

#### 2.12.1 FOSOF Atomic and Reference Beat Signals

A 2-channel 16-bit digitizer (Agilent L4532A) is used for the main experimental data acquisition. The FOSOF atomic signal and the reference beat signal from the microwave switching box (Section 2.11.2.2) are fed into the channel 1 and 2 of the digitizer, respectively. The digitizer sample rate is fixed at 10000 samples/s (Sa/s), a sufficiently high sample rate to resolve the signal oscillating at the offset frequency (the typical offset frequency used in the experiment is 280 Hz). Two channels of



Figure 2.40: Data acquisition system. A 2-channel digitizer is used to acquire FOSOF signals. Microwave and laser pulses are monitored on a digital oscilloscope. Other experimental parameters are monitored on two data loggers and a few labjacks. The three dots between the loggers indicate that there are more parameters being logged than the number lines shown in the figure.

the digitizer are synchronized for a simultaneous data acquisition, which ensures no systematic phase delay between channels. To avoid any changes in digitizer performance which may depend on the voltage scale, the scale setting is fixed at  $\pm 4V$  for both channels.

#### 2.12.2 Microwave and Laser Pulses

A digital oscilloscope (Tektronix DPO7354) is used to monitor the microwave and laser pulses. Channel 1 is allocated for the microwave pulses, and channels 2, 3, and 4 are used to monitor 447-nm, 1083-nm, and 1532-nm laser pulses, respectively. When acquiring data for the microwave pulses, only channel 1 is enabled to achieve the maximum sample rate of 40 GSa/s that is required for resolving the 2.3-GHz microwave pulses. 10-GSa/s setting is used for the laser pulse monitoring. The microwave and laser pulse data are transferred to and saved on the computer for every frequency setting used in every data set taken in the experiment. The acquired microwave pulses are used for a microwave power monitoring and the simulation of the experiment.

#### 2.12.3 Experimental Parameter Logging

Two data loggers (Keithley model 2701) and two Labjacks (U3 and U9) are used to log experimental parameters. One of the loggers monitors experimental parameters that are directly related to known systematic effects: the power of the microwave pulses, and the current and voltage used to apply magnetic field. The data logging of these parameters is synchronized with the main data acquisition protocol to ensure that the obtained linecentre is not affected by any outliers associated with a variation in these experimental parameters. The other logger and labjacks constantly logs many parameters (the ambient temperature, current for the metastable helium source, humidity in the lab, pressure in each section of the beamline, etc.). Obtained linecentres are plotted as a function of each parameter to test for possible systematic effects.

# 2.13 Data Processing Prior to the Lineshape Fitting Routine

Figure 2.41 shows a small fraction of the digitizer trace for the FOSOF experiment I and II (the trace length ranges from 5 s to 40 s depending on the experimental parameters). To fit the data with the expected FOSOF lineshape, the phase difference between the FOSOF atomic and reference beat signals needs to be found (indicated as  $\Delta \theta_{\rm I}$  and  $\Delta \theta_{\rm II}$ , where I and II denote experiment I and II). Extraction of the phase and amplitude information of each signal is obtained by taking the sine and cosine inner products (at the offset frequency). For the inner product, each data point of the digitizer trace is multiplied by the sine and cosine functions whose oscillation frequencies correspond to the FOSOF oscillation frequency  $2\delta f$ , and these are summed. The result of the inner product can be represented as  $Re^{i\theta}$ where R and  $\theta$  are the amplitude and phase of the signal, and are found using

$$R = \sqrt{X^2 + Y^2} \tag{2.5}$$

$$\theta = \arctan(\frac{Y}{X}),\tag{2.6}$$

where  $X = R\cos(\theta)$  and  $Y = R\sin(\theta)$  are the real and imaginary parts of  $Re^{i\theta}$ . The method is the same as that used for a lock-in amplifier [52]. The saved digitizer traces can be accessed any time and re-analyzed if necessary; whereas, in a typical lock-in amplifier operation, the information about the raw input signal is lost, and



Figure 2.41: Digitizer trace of the FOSOF signal. A small fraction of the digitizer trace is shown. This figure represents an average of four similar traces.  $\Delta \theta_{\rm I}$  and  $\Delta \theta_{\rm II}$  are used for linecentre determination.

the raw signal becomes inaccessible after the time of data acquisition.

For our analysis, the digitizer trace is typically broken up into fifty segments and the phase of each segment is determined using the inner-product method. The fifty phases are then averaged to obtain the best-estimate value. The standard deviation of the average phase is used to assign an uncertainty to the phase value. Once the phase and its uncertainty are obtained, the phase differences,  $\Delta \theta_{\rm I} = \theta_{\rm beat} - \theta_{\rm I}$  and  $\Delta \theta_{\rm II} = \theta_{\rm beat} - \theta_{\rm II}$ , are calculated. The final FOSOF phase (which eliminates phase lags as described in Section 2.11.1.2)  $\overline{\Delta \theta} = (\Delta \theta_{\rm I} - \Delta \theta_{\rm II})/2$  is then calculated.

As described in Section 2.11.1.2, the FOSOF phase changes linearly with frequency (to first order). Since the described method of phase determination cannot



Figure 2.42: Phase-stitching of the FOSOF phase. (a) and (b) are the FOSOF data without and with the phase-stitching process, respectively. The FOSOF phase cycles between phases  $-2\pi$  and  $2\pi$  radians (a). The data in (b) is used to determine the linecentre.

distinguish between  $\theta$  and  $\theta + 2N\pi$ , the data phase plots (Figure 2.42) show discontinuities. The FOSOF phase is stitched based on the assumption that it grows linearly. Figure 2.42 shows the stitching process. The discontinuities shown in Figure 2.42(a) are removed, and this data is fit to the expected lineshape for linecentre determination.

# **3** Atomic Lineshape and Linecentre

## Determination

This chapter discusses the analytic lineshape of the FOSOF technique obtained by solving the Schrödinger equation. The analytic lineshape is used to fit the FOSOF data for the linecentre determination. Reconstruction of an SOF signal from the FOSOF data is also performed, and the results are fit to the SOF lineshape to test the consistencies between SOF and FOSOF.

## 3.1 Analytic Solution to the FOSOF Lineshape

It is possible to derive an analytic FOSOF lineshape by assuming a continuously varying relative phase between the two microwave pulses. The derivation assumes instant turn-on and turn-off of the microwave pulses and perfect amplitude and phase profiles. Fabjan and Pipkin [53] derive a general SOF lineshape using the time-dependent Schrödinger equation for a two-level system, and their intermediate result is used to derive the FOSOF lineshape. Lombardi and Borbely [33,54] also give

a detailed derivation of the SOF lineshape specifically for the helium  $2^{3}P_{J}$ -to- $2^{3}P_{J'}$ transitions, so only a brief derivation is given in this section. The derivation closely follows Fabjan and Pipkin [53], but different notation is used to be consistent with the content of this thesis.

The two states involved in the SOF transition are  $2^{3}P_{1}$  and  $2^{3}P_{2}$ , and these are represented as  $|1\rangle$  and  $|2\rangle$ , respectively. The Hamiltonian describing the atom-field interaction is

$$H = H_0 + H_D - \boldsymbol{\mu} \cdot \mathbf{B}_0 \cos\left(\omega t + \delta\right), \qquad (3.1)$$

where  $H_0$  gives the energy levels of the two states:

$$H_0 |1\rangle = \hbar \omega_1 |1\rangle, \quad H_0 |2\rangle = \hbar \omega_2 |2\rangle,$$

$$(3.2)$$

and  $H_{\rm D}$  accounts for the decay rate associated with each of the two states:

$$H_{\rm D}|1\rangle = -\frac{1}{2}i\hbar\gamma_1|1\rangle, \quad H_{\rm D}|2\rangle = -\frac{1}{2}i\hbar\gamma_2|2\rangle, \qquad (3.3)$$

where  $\gamma = 1/\tau$  is the radiative decay rate of the state.  $\gamma_1 = \gamma_2 = 1/\tau$  in this particular case since the 2<sup>3</sup>P<sub>1</sub> and 2<sup>3</sup>P<sub>2</sub> states have the same lifetime of  $\tau = 98$  ns.  $\mu$  is the magnetic-dipole-moment operator which is defined to as,

$$\boldsymbol{\mu} = \frac{\mu_{\rm B}}{\hbar} (g_{\rm s} \mathbf{S} + g_{\rm l} \mathbf{L}), \qquad (3.4)$$

where  $\mu_{\rm B}$  is the Bohr magneton,  $g_{\rm s}$  and  $g_{\rm l}$  are the spin and angular-momentum g-factors, respectively, and **S** and **L** are the spin and orbital angular momentum

operators.  $\mathbf{B}_0 \cos(\omega t + \delta)$  represents the microwave magnetic field defined by the oscillating frequency  $\omega$ , the amplitude  $\mathbf{B}_0$ , and the phase  $\delta$ . The polarization of the microwave is oriented in the  $\hat{z}$  direction, so  $\mathbf{B}_0 = \mathbf{B}_0 \hat{z}$ . The two-level system is described by a 2-component wavefunction that is a superposition of two states:

$$|\Psi\rangle = c_1(t) |1\rangle + c_2(t) |2\rangle.$$
 (3.5)

The components of the  $|\Psi\rangle$  give the amplitude of being in state  $|1\rangle$  and  $|2\rangle$ . The time evolution of the system is described by the time-dependent Schrödinger equation:

$$i\hbar\frac{\partial}{\partial t}\left|\Psi\right\rangle = H\left|\Psi\right\rangle. \tag{3.6}$$

Substituting Equation 3.5 into Equation 3.6 with the Hamiltonian of Equation 3.1 yields two coupled equations:

$$i\dot{c}_{1}(t) = \omega_{1}c_{1}(t) - i\frac{1}{2}\gamma c_{1}(t) + 2Vc_{2}(t)\cos\left(\omega t + \delta\right)$$
(3.7)

$$i\dot{c}_{2}(t) = \omega_{2}c_{2}(t) - i\frac{1}{2}\gamma c_{2}(t) + 2Vc_{1}(t)\cos\left(\omega t + \delta\right), \qquad (3.8)$$

where

$$V = - \langle 1 | \boldsymbol{\mu} \cdot \mathbf{B}_{0} | 2 \rangle$$
  
=  $- \frac{\mu_{B}}{2\hbar^{2}} \langle 1 | (g_{s}\mathbf{S} + g_{l}\mathbf{L}) \cdot \mathbf{B}_{0} | 2 \rangle$  (3.9)

is the magnetic-dipole matrix element. The magnetic-dipole matrix elements of the  $2^{3}P_{J}$ -to- $2^{3}P_{J'}$  transitions are evaluated and tabulated in [33, 54].



Figure 3.1: Interaction Timing for the lineshape fitting function

Figure 3.1 shows the timing of the SOF experiment. At time t = 0, all atoms are in state  $|1\rangle$ , and they enter the microwave field  $\mathbf{B}_0 \cos(\omega t)$ , where the phase of this microwave field is assumed to be zero. The atoms then leave the microwave field at time t = D and spend a time  $t_{ff}$  ( $t_{ff} = T - D$ ) in a field-free region. After the field-free region, the atoms are again exposed to a microwave field  $\mathbf{B}_0 \cos(\omega t + \delta)$  for a duration of D. Equations 3.7 and 3.8 need to be integrated with initial conditions for the timing provided by the Figure 3.1 to obtain amplitude of the wavefunction for the SOF experiment. Fabjan and Pipkin give the SOF amplitudes  $c_1(T + D + T)$ and  $c_2(T + D + T)$  at the exit of the second microwave pulse (Equations 19(a) and 19(b) of [53]):

$$c_{1}(D+T+D) = \exp\left[-\gamma(D+T) - i(\omega+\omega_{1}+\omega_{2})D - i\omega_{1}T\right]$$

$$\times\left\{\left(\cos\left(\frac{1}{2}aD\right) + i\frac{\Delta\omega}{a}\sin\left(\frac{1}{2}aD\right)\right)^{2} - \exp\left[-i(\delta+\Delta\omega(T-D))\right]\left(\frac{2V}{a}\right)^{2}\sin^{2}\left(\frac{1}{2}aD\right)\right\},$$

$$(3.10)$$

$$c_{2}(D+T+D) = \exp[-\gamma(D+T) + i(\omega - \omega_{1} - \omega_{2})D - i\omega_{2}T]$$

$$\times \left(-i\frac{2V}{a}\sin\left(\frac{1}{2}aD\right)\right) \left\{\left(\cos\left(\frac{1}{2}aD\right) - i\frac{\Delta\omega}{a}\sin\left(\frac{1}{2}aD\right)\right)\right\}$$

$$+ \exp[i(\delta + \Delta\omega(T-D))] \left(\cos\left(\frac{1}{2}aD\right) + i\frac{\Delta\omega}{a}\sin\left(\frac{1}{2}aD\right)\right)\right\}, \quad (3.11)$$

where  $\Delta \omega = \omega - \omega_0$  is the microwave detuning from the atomic resonance ( $\omega_0 = \omega_1 - \omega_2$ ), and  $a = \sqrt{4V^2 + \Delta \omega^2}$ . In the current experiment, only atoms that make a microwave transition to  $|2\rangle$  are detected and the probability  $|c_2(D + T + D)|^2$ at  $\delta = 0^\circ$  and  $\delta = 180^\circ$  needs to be evaluated and subtracted to obtain the SOF lineshape. It can be shown that the analytic solution to the SOF lineshape can be written as,

$$P_{\text{SOF}}(T, D, V, \Delta \omega) = |c_2(D + T + D)|^2_{\delta = 0^{\circ}} - |c_2(D + T + D)|^2_{\delta = 180^{\circ}}$$
  
$$= \frac{16e^{-\gamma(T+D)}}{(4V^2 + \Delta \omega^2)^2} V^2 \sin^2 \left(\frac{1}{2}D\sqrt{4V^2 + \Delta \omega^2}\right)$$
  
$$\times \{\cos(\Delta \omega(T - D))(4V^2 + \Delta \omega^2)\cos\left(D\sqrt{4V^2 + \Delta \omega^2}\right)$$
  
$$- \Delta \omega \sqrt{4V^2 + \Delta \omega^2}\sin\left(\Delta \omega(T - D)\right)\sin\left(D\sqrt{4V^2 + \Delta \omega^2}\right)\}.$$
  
(3.12)

Equation 3.12 describes the SOF interference pattern inside the envelope function whose width is determined by the width of the applied microwave pulses.

The FOSOF lineshape can be derived from Equation 3.11 by assuming a continuously changing  $\delta = 2\pi (2 \, \delta f \, t)$ . The phase of the resulting sinusoidal variation of signal obtained from Equation 3.11 needs to be determined. Equation 3.11 involves complex numbers, and the phase associated with the real and imaginary components of the equation can be found by adding the arguments of the complex factors:  $\cos(\frac{1}{2}aD) + i\frac{\Delta\omega}{a}\sin(\frac{1}{2}aD)$ , and  $\cos(\frac{1}{2}aD) - i\frac{\Delta\omega}{a}\sin(\frac{1}{2}aD)$ . The factor  $-i\frac{2V}{a}\sin(\frac{1}{2}aD)$  can be ignored since it adds the same phase factor to the two terms. The second term in the argument of the exponential  $e^{\Delta\omega(T-D)}$  is an additional phase factor that needs to be added to the phase. The total phase of Equation 3.11 is found by adding all three phase factors and can be written as

$$\Delta\theta(T, D, V, \Delta\omega) = \Delta\omega(T - D) + 2\tan^{-1}\left[\frac{\Delta\omega\tan\left(\sqrt{4V^2 + \Delta\omega^2}D/2\right)}{\sqrt{4V^2 + \Delta\omega^2}}\right].$$
 (3.13)

Equation 3.13 predicts the variation in phase of the interference cosine of the SOF lineshape. This lineshape slightly deviates from the linear lineshape ( $\Delta \omega T$  in Equation 2.4) predicted by the time-dependent perturbation theory (TDPT) in the limit of  $V \rightarrow 0$ . A detailed description of this deviation is discussed in Section 3.2.

The amplitude of the FOSOF signal as a function of microwave frequency can also be derived by taking the absolute value of the product of the complex terms used to derive Equation 3.13 with  $-i\frac{2V}{a}\sin\left(\frac{1}{2}aD\right)$  term included. The amplitude of the FOSOF signal with the exponential decay factor can be written as,

$$A(T,D,V,\Delta\omega) = \frac{4V^2 e^{-(T+D)\gamma}}{4V^2 + \Delta\omega^2} \sin^2\left(\frac{1}{2}D\sqrt{4V^2 + \Delta\omega^2}\right) \\ \times \left(\cos^2\left(\frac{1}{2}D\sqrt{4V^2 + \Delta\omega^2}\right) + \frac{\Delta\omega^2}{4V^2 + \Delta\omega^2}\sin^2\left(\frac{1}{2}D\sqrt{4V^2 + \Delta\omega^2}\right)\right).$$
(3.14)

The second part of Equation 3.13 is only well defined between the phase values between  $-\pi$  to  $+\pi$  radians. Discontinuities occur at the phases  $-\pi$  and  $+\pi$  radians, and the function value cycles between these two phases. In order to obtain a smooth function, a phase-stitching needs to be performed (similar to the process described in Section 2.13). Figure 3.2 illustrates the function discontinuity and the phase-stitching. In Figure 3.2(a), the second part of Equation 3.13 is plotted. The discontinuity shown in the figure also shows up in the total function plotted in 3.2(b). The stitched phase is shown in Figure 3.2(c). The function used to plot Figure 3.2(c) has the form,

$$\overline{\Delta\theta}(T, D, V, \Delta\omega) = \Delta\omega T + \operatorname{mod}_{2\pi} \left[ \pi + 2 \tan^{-1} \left[ \frac{\Delta\omega \tan\left(\sqrt{4V^2 + \Delta\omega^2}D/2\right)}{\sqrt{4V^2 + \Delta\omega^2}} \right] - \Delta\omega D \right] - \pi,$$
(3.15)



Figure 3.2: Phase-stitching of FOSOF lineshape. (a) shows the discontinuity associated with the second part of Equation 3.13. (b) and (c) are the plots of FOSOF lineshape of Equation 3.13 without and with the phase-stitching, respectively. The gray line in (b) indicates where the stitched phases end up. The lineshape shown in (c) is used to fit the experimental data to determine the linecentres.

where  $\text{mod}_{2\pi}$  indicates the modulus of  $2\pi$  is taken for the second part of the equation. Equation 3.15 is used for plotting a theoretical lineshape, and fitting of the FOSOF data.

## 3.2 Theoretical Lineshapes

The advantage of using the SOF technique is not only the narrowing of the transition linewidth, but also the ability to change the lineshape by adjusting T and D and V, which allows for a study of systematic effects. Various lineshapes associated with different T, D, and V are investigated in the current experiment. Figures 3.3 and 3.4 shows three lineshapes with different T for a fixed D and V. In Figure 3.3, the effect of changing T on the FOSOF lineshape of Equation 3.15 is shown on a single plot.



Figure 3.3: Effect of T on FOSOF theoretical lineshapes. Equation 3.15 with D=100 ns and V=1 rad/s is plotted for three different values of T.

Figure 3.4 summarizes the change in SOF and FOSOF lineshapes. As illustrated at the left of the figure (SOF in Figure 3.4, plotted using Equation 3.12), the width of the interference changes for different T values used. The interference width is given by 1/2T. The FOSOF lineshape, shown in the middle (FOSOF phase in Figure 3.4), is a mostly linear function whose slope is given by  $2\pi T$ . These lineshapes are the same as the ones shown in Figure 3.3. The FOSOF phase deviation from the TDPT prediction (shown at the right of Figure 3.4, labelled as FOSOF-TDPT ) remains constant over the range of T. This is because the deviation only depends on the effective field amplitude that the atoms experience.

Figure 3.5 shows the effect of V on the FOSOF lineshape. Figure 3.5 shows that



Figure 3.4: Theoretical SOF and FOSOF lineshapes for different T. In the figure, parameters D=100 ns and V=1 rad/s are used. Variations in the width of the SOF interference and the FOSOF phase slope are observed. FOSOF-TDPT (i.e., the second term of Equation 3.15) remains the same for different T values.



Figure 3.5: Effect of V on the FOSOF theoretical lineshape (shown here for T=400 ns and D=100 ns). FOSOF-TDPT lineshape (the second term of Equation 3.15) grows as V increases. For V=0 rad/s the TDPT prediction of a linear lineshape is exact.

as V approaches to zero, the TDPT linear lineshape is restored, and the FOSOF-TDPT lineshape is zero. Figure 3.6 illustrates three lineshapes with different Dfor a fixed T and V. D governs the spectral width of the microwave pulse (the width of the envelope of the SOF interference goes as 1/D). Three SOF lineshapes shown at the left of the figure have different widths for different D values. The width of the SOF interference and FOSOF phase slope does not change because Tremains constant. The FOSOF-TDPT lineshapes show that the size of the deviation grows as D increases. The figure also shows that the FOSOF-TDPT difference is maximized around the half width point of the transition.



Figure 3.6: Theoretical SOF and FOSOF lineshapes for different D. The width of the transition (pink solid line in the SOF column) changes for different D. The SOF interference and FOSOF phase slope remains constant for all three cases. The FOSOF-TDPT difference is maximum around the half-width of the transition.

definition	fit parameter	comments
Pulse separation T		floated with the nominal experiment value as an initial guess. Sensitive to phase slope.
Pulse duration	D	fixed with the nominal experiment value
Microwave field amplitude	V	fixed with the best guess of the fractional microwave power
resonant frequency	$f_0$	floated, a quantity to be determined from the fit
microwave frequency	f	function variable

Table 3.1: Summary of fit parameters.

## 3.3 FOSOF Experimental Lineshapes

Figures 3.7 through 3.12 show the experimental FOSOF lineshapes for the 18 timings used in the experiment. Experimental lineshapes for multiple microwave power settings are shown. The plots at the top show the averaged data points (averaged over the full data set considered in this thesis) along with a fit using Equation 3.15. The error bar associated with each data point is too small to be seen on this scale. The middle plot shows the same data points and fit with the TDPT linear prediction  $(2\pi T(f - f_0))$  subtracted. The subtraction scales up the plots at the top by about a factor of 100, and the error bars start to become visible in some of the plots. The fit residuals are shown at the bottom of the figure. Residuals for different power settings are shown separately. Typically, three different microwave power settings are shown. The reduced chi-square of the fits is typically less than 1 (with 30 degrees of freedom).

Table 3.1 shows a summary of fit parameters. The lineshape used is Equation

3.15, with  $2\pi(f - f_0)$  substituted in place of  $\Delta \omega$ . Typically, the pulse separation T and the resonant frequency  $f_0$  are floated. Other parameters (the pulse duration D and the microwave power V) are fixed with the nominal experimental settings. Different sets of floating parameters are used to check the consistency in fit linecentres. Very small (~1 Hz) variations in fit linecentres are observed when different sets of parameters are floated; therefore, the measured linecentres are independent of the floating parameters if the fixed values are chosen properly.



Figure 3.7: FOSOF experimental lineshapes and fits: (T,D)=(300,50) ns, (300,100) ns,(300,150) ns.



Figure 3.8: FOSOF experimental lineshapes and fits: (T,D)=(400,50) ns, (400,100) ns, (400,200) ns.



Figure 3.9: FOSOF experimental lineshapes and fits: (T,D)=(500,50) ns, (500,100) ns, (500,125) ns.



Figure 3.10: FOSOF experimental lineshapes and fits: (T,D)=(600,50) ns, (600,100) ns, (600,150) ns.



Figure 3.11: FOSOF experimental lineshapes and fits: (T,D)=(375,125) ns, (450,150) ns, (600,200) ns.



Figure 3.12: FOSOF experimental lineshapes and fits: (T,D) = (700,100) ns, (800,100) ns, (900,100) ns.

## 3.4 Measured Linecentres

Table A.2 in Appendix-A gives a summary of the linecentres obtained from fits of the experimental data and also gives the applied systematic corrections and their uncertainties (as discussed in Chapter 4). A significant amount of data is collected to test for systematic effects. A detailed description of the systematic corrections and their associated uncertainties is given in Chapter 4. A total of 3608 experiments were performed between April 24 to June 14, 2018. Column one is the run number assigned to each row of the table. Columns two through four show the microwave parameters, the pulse separation T, the pulse duration D, and the microwave power P, used in the experiment. Column five is the magnetic field setting B of the experiment. The sign indicates that the magnetic field direction is reversed from  $+\hat{z}$  to  $-\hat{z}$  direction. Column six is the polarization angle of a quarter-wave plate for optical pumping direction. The combination of the sign of B and polarizer angle determines the  $m_J$  state  $(m_J=+1 \text{ or } -1)$  used in the experiment. Columns seven and eight are the linecentres obtained from fits and the associated fit uncertainties. Columns nine through twelve are the systematic corrections applied to the measured linecentres and their uncertainties. Column thirteen shows linecentres after the systematic corrections are applied. Column fourteen is the total uncertainty obtained by adding all uncertainties in quadrature. Column fifteen gives the normalized weights used to take the weighted average of the data runs. Identifiers are assigned to data runs used for the study of systematic effects, and are shown at column sixteen. Table A.1 shows the definition of each identifier. Numbers in columns seven and thirteen are with respect to the final measured result of 2 291 176 590 Hz.

# 4 Systematic Effects

The excellent signal-to-noise ratio obtained in the current experiment allowed for an extensive study of systematic effects. In this chapter, details on systematic effects and corresponding corrections and uncertainties are discussed. It should be noted that the order of data acquisition is randomized whenever possible to eliminate the possible effects of time-dependent linecentre shifts. However, there was no evidence for such time-dependent shifts in the data set.

## 4.1 DC Zeeman Shifts

The largest systematic correction applied to the measured linecentres comes from the quadratic DC Zeeman shift. The DC magnetic field perturbs the atomic system and shifts the energy levels. To first-order, the  $2^{3}P_{1}(m_{J}=-1)$ -to- $2^{3}P_{2}(m_{J}=-1)$  transition does not have a DC Zeeman shift since the two states shift at the same rate. However, these states shift differently when higher-order effects are taken into account. In second-order, the  $2^{3}P_{1}(m_{J}=-1)$  and  $2^{3}P_{2}(m_{J}=-1)$  states repel each

other at a quadratic rate of  $0.4295 \text{ kHz/G}^2$  [54]. Since the scale of the shift is large, it it necessary to have a precise knowledge of the applied field to apply accurate corrections to the measured linecentres. The magnetic field system is described in Section 2.10. The magnetic field *B* is the combination of applied and residual fields at the location of the experiment. Therefore, *B* can be written as

$$B = \sqrt{(kI + B_0^{\parallel})^2 + (B_0^{\perp})^2}, \qquad (4.1)$$

where I is the current applied to the Helmholtz coils, and k is the current-to-field conversion factor (in Gauss per Ampere) for the main Helmholtz coils, and  $B_0^{\parallel}$  and  $B_0^{\perp}$  are the residual-field components that are parallel and perpendicular to the Helmholtz axis. As described in Section 2.10, the magnetic field at the location of the experiment was measured using a 3-axis gaussmeter. The residual fields  $B_0^{\parallel}$ and  $B_0^{\perp}$  are cancelled to  $\pm 10 \text{ mG}$ . k for the main Helmholtz coils was found to be  $k_{\text{gaussmeter}}=10.866\pm0.010 \text{ G/A}$ . However, the difficulty in positioning the probe exactly at the location of the experiment poses questions about the accuracy of this measurement.

#### 4.1.1 Uncertainty in the Residual Magnetic Field

In the presence of  $B_0^{\parallel}$ , the quadratic Zeeman shift has the form,

$$\Delta \nu_{\rm DC \ Zeeman}(I) = \beta \left( (kI)^2 + 2kIB_0^{\parallel} + B_0^2 \right), \qquad (4.2)$$

where  $\beta = 0.4295 \text{ kHz/G}^2$  is the quadratic Zeeman shift rate. The  $B_0^2 = (B_0^{\perp})^2 + (B_0^{\parallel})^2$  term is negligible since  $|B_0|$  is less than 10 mG, leading to a contribution of < 0.04 Hz. In order to cancel the contribution from the linear term in Equation 4.2, half of the data is taken with positive current and half with negative current. The linear term gets cancelled when linecentres from the two types of data are averaged together.

### 4.1.2 Uncertainty in the Applied Magnetic Field

Precise values of k and I are required to apply appropriate corrections for the quadratic Zeeman shift. The current I is measured to an accuracy of better than 0.002 % by measuring the voltage across a precision shunt resistor (IET Labs, Inc. model DCCS-0.01). Linecentres are determined as a function of applied magnetic field to test the k value obtained with the gaussmeter ( $k_{gaussmeter}=10.866\pm0.010$  G/A). Figure 4.1 shows an example of linecentres obtained versus current in the Helmholtz coils. The data are fit to Equation 4.2 (ignoring the small  $B_0^2$  term), floating parameters k and  $B_0^{\parallel}$ . The residual field parameter  $B_0^{\parallel}$  is found to be  $0.002\pm0.005$  G, which is consistent with zero. The value of k, however, is determined to be slightly different from the value obtained with the gaussmeter method. The parameter k from the fit is  $k_{fit}=10.846\pm0.001$  G/A, and this value is 0.2 % smaller than  $k_{gaussmeter}$ .



Figure 4.1: Magnetic field calibration curve. Panel (a) shows the data fit to Equation 4.2. Panel (b) show the residuals of the fit. The band bounded by the pink lines indicates the result of an additional 0.1% uncertainty in the DC Zeeman correction (column 10 in Table A.2), and the band bounded by the green lines is the final quoted uncertainty of 25 Hz.
and therefore measures the magnetic field at the correct position; therefore it is more reliable. However, if there is a position-dependent variation in k around the experiment region which causes the two values to disagree, then an additional uncertainty needs to be assigned because the position of the excitation inside the microwave region may change slightly depending on the laser alignment.

Table 4.1 shows measured (using averages of the full data set of Table A.2) and predicted Zeeman shifts (based on determinations of k and I) for different currents applied to the Helmholtz coils. The first and second columns show the nominal field setting and corresponding applied current to the Helmholtz coils. Column 3 shows the average measured linecentres at currents given in column 2, and column 4 shows the difference between the linecentre obtained at the smallest current shown in the table  $(I_0)$  and the other currents I. This column indicates the experimentally observed DC Zeeman shifts with respect to  $I_0$ . Linecentres listed in this column are obtained by averaging NR and LB data types in Table A.2 without applying a DC Zeeman correction and without applying the DC Zeeman uncertainty (i.e., subtracting the DC Zeeman correction and uncertainty in columns 9 and 10 from the corrected linecentres in column 13 of Table A.2). Column 5 of Table 4.1 is the predicted DC Zeeman shift based on fields obtained by  $B(I) = k_{\text{fit}}I$ . Percentage difference between the measured and predicted Zeeman shifts (column 6) shows an average difference of 0.086%. The data in column 4 is re-fit to Equation 4.2 for a further

Nominal <i>B</i> [Gauss]	<i>I</i> [A]	$\nu_{\rm avg}(I)$ [Hz]		$\beta((k_{\rm fit}I)^2 - (k_{\rm fit}I_0)^2)$ [Hz]	Difference between col. 4 and col. 5 [%]	$\beta((k_{\text{data}}I)^2 - (k_{\text{data}}I_0)^2)$ [Hz]	Difference between col. 4 and col. 7 [%]
3.175	$I_0 = 0.293806(10)$	2291180950(9)					
4.762	0.439791(5)	2291186356(6)	5406(11)	5411(2)	0.092	5407(2)	0.002
9.524	0.878683(8)	2291215558(11)	34608(14)	34648(7)	0.115	34 620(7)	0.035
19.048	1.757554(19)	2291332546(18)	151596(20)	151709(29)	0.075	151588(29)	0.005
28.572	2.635487(40)	2291527294(22)	346344(24)	346 572(64)	0.066	346297(64)	0.014
33.334	3.075265(49)	2291654035(29)	473085(30)	473 462(87)	0.080	473 087(87)	0.0003

Table 4.1: Comparison between the measured and predicted DC Zeeman shifts. The first column is the field setting. The second column is the current applied to the Helmholtz coils.  $\nu_{avg}(I)$  is the measured linecentres with the applied current. Linecentres shown here are obtained by taking NR and LB data types (refer to Table A.1 for identifiers) in Table A.2 and averaging the linecentres (column 13 in Table A.2) without DC Zeeman correction and uncertainty (columns 9 and 10 in Table A.2) at fields shown in the first column. The values in columns 1 and 2 are also averaged (with the same weights as used for  $\nu_{avg}$ ) for data taken at almost identical field settings. One standard deviation uncertainties are shown in parentheses.  $\nu_{avg}(I) - \nu_{avg}(I_0)$  is the difference between the linecentre obtained with the smallest applied current and linecentre with other applied currents, where  $I_0$  indicates the smallest applied current shown in the first row.  $\beta((k_{fit}I)^2 - (k_{fit}I_0)^2)$  and  $\beta((k_{data}I)^2 - (k_{data}I_0)^2)$  are the predicted DC Zeeman shifts based on fields calculated using  $k_{fit}$  and  $k_{data}$  with respect to field at  $I_0$ . Columns 6 and 8 show the percentage difference between the measured and predicted DC Zeeman shifts using  $k_{fit}$  and  $k_{data}$ .

Parameters	Linecentre $\nu_{\rm exp}$ [Hz]	$\Delta \nu  [\text{Hz}]$
Negative field polarity	2291176593(12)	+3
Positive field polarity	2291176592(13)	+2
B in range 0 to 5 G	2291176584(11)	-6
B in range 5 to 10 G	2291176592(16)	+2
$ \mathbf{B} $ in range $> 10\mathrm{G}$	2291176567(62)	-23

Table 4.2: Summary of measured linecentres with different magnetic field settings. The consistency of results demonstrated in this table eliminates the possibility of having effects larger than the level of precision of the current experiment. The table also shows the results of opposite magnetic field directions.  $\Delta \nu = \nu_{\rm exp} - \nu_{12}$  is the difference between the measured linecentre  $\Delta \nu_{\rm exp}$  and the final measured result of  $\nu_{12} = 2.291176590$  Hz.

adjustment on the value of k. This fit (which is based on the full data set used for the current measurement) suggests  $k_{data}=10.842\pm0.001$  G/A, which agrees to better than 0.1 % with  $k_{fit}$ . Column 7 and 8 shows predicted linecentres based on  $\beta(k_{data}I)^2$ and difference between the measured and predicted linecentres, respectively. Shifts predicted by  $\beta(k_{data}I)^2$  are used to correct all measured linecentres. The observed discrepancy between the  $k_{fit}$  and  $k_{data}$  sets a limit on the knowledge of the applied field, and a conservative 0.1 % uncertainty (slightly larger than the average difference of 0.086 % from the prediction of  $\beta(k_{fit}I)^2$ ) is assigned to the DC Zeeman correciton for all of the experimental runs to account for the position-dependent variation of k. Most of our data are taken at fields smaller than 5 G, where 0.1 % correction uncertainty yields < 10 Hz contribution to the total uncertainty. Agreement between the data taken at low and high fields verifies the 0.1 % understanding of the applied fields, as illustrated in Figure 5.1 and Tables 4.1 and 4.2.

# 4.2 Microwave Power Shifts

Linecentre shifts related to the power of the microwave pulses are discussed in this section. Numerical integration of the time-dependent Schrödinger equation was carried out by Taylor Skinner to model the experiment based on the oscilloscope traces of the microwave pulses used in the experiment, or based on models of possible imperfections in the microwave fields. In particular, systematic effects due to frequency-dependent microwave power variation (Section 4.2.3) and distorted phase and amplitude profiles for the microwave pulses (Section 4.2.4), are extensively modelled. All shifts described in this section follows a linear trend versus microwave power, and vanish at zero microwave power.

## 4.2.1 AC Zeeman Shifts

The oscillating microwave magnetic field introduces AC Zeeman shifts to the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  linecentre. A detailed description of AC Zeeman shifts is given in [54], so only a brief explanation is given here. Figure 4.2 illustrates the microwave magnetic and electric fields inside the coaxial airline. Within the coaxial airline, the microwave magnetic field is, to a good approximation, pointing in the  $\hat{z}$  direction. For our coaxial geometry, the relationship between microwave field and power that atoms



Figure 4.2: Microwave magnetic and electric field lines inside the coaxial airline.

see is given by [55]

$$B_{mw}(r) = 2\mu_0 \left(\frac{a}{r}\right) \left[ \left(\frac{1}{\pi a^2}\right) \sqrt{\frac{\epsilon_0}{\mu_0}} \left(\ln\left(\frac{b}{a}\right)\right)^{-1} P_{mw} \right]^{1/2}, \qquad (4.3)$$

where a is the radius of the inner conductor, b is the radius of the inner wall of the outer conductor, r is the location of the interaction measured from the central axis of the inner conductor,  $\epsilon_0$  is the electric permittivity of vacuum,  $\mu_0$  is the magnetic permeability of vacuum, and  $P_{mw}$  is the microwave power in the coaxial transmission line. The a/r factor is the field reduction factor necessary to account for the decreasing field as a function of distance from the surface of inner conductor. In the current experiment, the microwave is reflected from the short at the end of the microwave region. This gives the factor of 2 in Equation 4.3. The 14-mm coaxial airline geometry (dimensions of the microwave region are given in Section 2.11.2.3) has a=3.102 mm and b=7.144 mm. The interaction of the atoms with the first microwave pulse happens at approximately r=5.123 mm, the average of a and b. The pulse separation T used in the experiment ranges from 300 to 900 ns. With the most probable atomic speed of  $v_{mode}=1100 \text{ m/s}$ , atoms travel a distance of approximately  $v_{mode}T$  during the time T. The average interaction location r is therefore half way between (a + b)/2 and  $(a + b)/2 + v_{mode}T$ . Plugging a, b and r values into Equation 4.3 gives  $B_{mw}$ . For the  $2^{3}P_{1}(m_{J}=\pm1)$ -to- $2^{3}P_{2}(m_{J}=\pm1)$  transitions, the AC Zeeman shift rate is given by [54]

$$\Delta \nu_{\rm AC \ Zeeman} = (+54 \ \text{Hz}) \frac{B_z^2}{\text{G}^2}.$$
(4.4)

The AC Zeeman effect for the case of SOF experiment is suppressed by approximately a factor D/T [33] because the microwaves are on for a fraction of the time defined by the experimental timing parameters T and D. Table 4.3 summarizes the expected AC Zeeman shifts for different experimental timing parameters for the maximum available microwave power of 75 W. The AC Zeeman shifts are  $\leq 100$  Hz, and are even smaller at the typical powers used for the measurements.

Pulse separation $T$ [ns]	Pulse duration $D$ [ns]	Interaction location $r \text{ [mm]}$	$\begin{array}{c} {\rm SOF \ suppression} \\ D/T \end{array}$	Microwave field $B_{mw}$ [Gauss]	AC Zeeman shifts $\Delta \nu_{\rm AC Zeeman}$ [Hz]
300	50	5.486	0.167	1.986	35
300	100	5.486	0.333	1.986	71
300	150	5.486	0.500	1.986	106
375	125	5.577	0.333	1.953	69
400	50	5.607	0.125	1.943	25
400	100	5.607	0.250	1.943	51
400	200	5.607	0.500	1.943	102
450	150	5.668	0.333	1.922	67
500	50	5.728	0.100	1.902	20
500	100	5.728	0.200	1.902	39
500	125	5.728	0.250	1.902	49
600	50	5.849	0.083	1.863	16
600	100	5.849	0.167	1.863	31
600	150	5.849	0.250	1.863	47
600	200	5.849	0.333	1.863	62
700	100	5.970	0.143	1.825	26
800	100	6.091	0.125	1.789	22
900	100	6.212	0.111	1.754	18

Table 4.3: Expected AC Zeeman shifts for different experimental timing parameters for the maximum microwave power of  $75 \,\mathrm{W}$ .

## 4.2.2 AC Stark Shifts

The oscillating electric field of the microwave pulses cause linecentre shifts due to the AC Stark effect. The AC Stark shift rate of the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition is estimated in [54]. A microwave electric field in the  $\hat{z}$  direction causes a shift of

$$\Delta \nu_{\rm AC \; Stark} = (-7.78 \pm 0.57) \, \text{kHz} \, \frac{E_z^2}{(\text{kV/cm})^2}, \tag{4.5}$$

and the electric field in the  $\hat{y}$  direction causes a shift of

$$\Delta \nu_{\rm AC \; Stark} = (-0.6 \pm 1.2) \, \text{kHz} \, \frac{E_y^2}{(\text{kV/cm})^2}. \tag{4.6}$$

As in the case of the AC Zeeman shift, the shift for SOF experiment is suppressed by a factor D/T. As it can be seen from Figure 4.2, the microwave field component  $E_z$ is significantly smaller than  $E_y$  due to the geometry. The geometry restricts the size of  $E_z$  to be < 5% of  $E_y$ ; therefore the shift rate associated with the z-component of the electric field is negligible. The size of the  $E_y^2$  would be significant for the microwave power used in the current experiment. However, the reflection of the microwave pulse from the short located a half wavelength away from the interaction region cancels out the electric field at the location of interaction. That is, there is an electric field node at this position. With the slit width of 5 mm, the maximum electric field (at a position of  $\pm 2.5$  mm from the centre of the slit —i.e., from the position of the node) is suppressed by a factor of < 0.0035. With this suppression, the shift is estimated to be < 1 Hz. There are, however, short periods of time near the beginning and the end of the pulses when the electric field does not get cancelled by the reflection. It takes 0.22 ns for the microwave to return to the interaction location after a reflection off of the short in Figure 2.34. Using a reduction factor of 2(0.22 ns)/T (the factor of 2 is because of the two 0.22-ns periods during which the electric field is not cancelled), the net AC Stark shifts are negligibly small (< 1 Hz).

### 4.2.3 Shifts Due to Frequency-Dependent Microwave-Power Variation

The microwave power seen by the atoms is not perfectly independent of frequency over the frequency range used in the experiment due to the frequency responses of various RF components in the system. The changing microwave power over the frequency range of the experiment causes a lineshape distortion and shifts the linecentre. Simulation of this effect predicts that the linecentre shifts due to the frequency-dependent microwave power is proportional to the applied microwave power. No shifts are seen in the low-power TDPT regime (i.e., the shift extrapolates to zero as  $P_{mw} \rightarrow 0$ ).

In order to achieve the best power flatness versus frequency, the output power level of both the HP and Wiltron microwave generators are adjusted for every frequency used in the experiment. The power of the microwave pulses used in the experiment is monitored using a power detector and an oscilloscope. The power flatness calibration was performed at every power setting used in the experiment. This calibration was performed twice before the start of the data acquisition. The level of power flatness was < 0.05 %/MHz, assuming that the oscilloscope and diode give an accurate measurements of the microwave power. Simulation results with 0.05 %/MHz flatness level shows a shift of 150 Hz (at full power) assuming experimental timing parameters T=300 ns and D=100 ns, with the shift extrapolating to zero at zero power.

Recent (February 2019) investigation of the power flatness using atoms [56] reveals that the power detector reading and oscilloscope traces do not represent the actual power seen by the atoms. Reflections in the microwave system and imperfect isolation in the circulator cause the detector reading to oscillate as a function of applied microwave frequency, even when the atoms experience perfect power flatness. As a result, the quoted 0.05% power-flatness level is underestimated. The effect of imperfect power flatness is eliminated by the extrapolations to zero power, as discussed in Section 4.2.5.

### 4.2.4 Shifts Due to Imperfect Microwave Phase and Amplitude

The most subtle systematic effect arises from distortions of the phase and amplitude of the microwave pulses. The phase distortion is most prominently observed at the beginning and end of the microwave pulses. Sudden switching of microwaves causes the phase during the rise and fall times of the pulses to become shifted compared to the time at which microwaves are fully on. Figure 4.3(a) shows an example of an oscilloscope trace of the microwave pulses for T=400 ns and D=100 ns. Figure 4.3(b) shows an expanded view of one of the pulses in Figure 4.3(a). The plot shows a small increase of the pulse amplitude over the duration of the pulse. Figure 4.4 shows three segments of the microwave pulse of Figure 4.3(b). Figures 4.4(a) and 4.4(c) show the beginning and end of the pulse, respectively. Figure 4.4(b) shows a central fraction of the microwave pulse. The sine wave in pink is a fit to the central part of the microwave pulse shown in Figure 4.4(b). At the beginning and end of the pulse, data points are out of phase with the pink line, showing an indication of phase distortion at these times.

Integration of the Schrödinger equation based on oscilloscope traces of microwave pulses (an example is shown in Figure 4.3) show that the linecentre shift is approximately proportional to the inverse of the pulse separation (1/T), the pulse duration D, and the microwave power P. That is,

$$\Delta \nu \propto D \frac{P}{T},\tag{4.7}$$

where  $\Delta\nu$  denotes the linecentre shift. Experiments with various T, D, P combinations were performed to understand this effect. Since the effect of the microwave phase and amplitude imperfections is expected to vanish at zero microwave power, all measured linecentres are extrapolated to zero power. The data collected with different T, D, and P parameters approximately follow the trend predicted by Equation 4.7 (shown in Figures 4.5 through 4.7). The method and results of the power extrapolation are discussed in Section 4.2.5.



Figure 4.3: Shape of the microwave pulses. (a) shows an oscilloscope trace of T=400 ns and D=100 ns microwave pulses, and (b) shows a pulse in (a) in a blown-up scale. A small amplitude variation is observed.



Figure 4.4: Phase distortion of the microwave pulse. The pink sine wave represents a fit to data shown in (b), and the same fit is shown in both (a) and (c) as a reference. The data in (a) and (c) do not follow the fit during turn-on and -off of the microwave pulse, showing an indication of phase imperfection.

## 4.2.5 Extrapolation of Linecentres to Zero Microwave Power

All systematic effects discussed in earlier sections (AC Zeeman effect, AC Stark effect, frequency-dependent power variation, and microwave phase and amplitude distortions) depend linearly on applied microwave power. Experiments with various T, D, and P combinations are performed, and all measured linecentres are extrapolated to zero microwave power (linecentres are first corrected by the DC Zeeman shifts before the power extrapolation).

For a particular value of D, linecentres are expected to shift linearly with P/T (Equation 4.7). The value of P used is based on an average of power detector readings (described in Sections 2.11.2.1 and 2.12.3). Linecentres with associated P/T are fit to a linear model, floating the slope and y-intercept. Figures 4.5 through 4.7 show such linear fits, and Table 4.4 shows the extrapolation results for different values of D. The extrapolation slopes shown in Table 4.4 follow approximately the trend predicted by Equation 4.7. The values in the final column of Table 4.4 are based on integration of Schrödinger equation using the oscilloscope trace as an input. The measured and simulated P/T slopes do not agree with each other, and this disagreement indicates that the oscilloscope trace is not a true representation of the microwave fields seen by the atoms. Nonetheless, since all of the shifts extrapolate to zero, the extrapolations shown in Figures 4.5 through 4.7 should give



Figure 4.5: Extrapolation of D=50 and D=100 data.



Figure 4.6: Extrapolation of D=125 and D=150 data.



Figure 4.7: Extrapolation of D=200.

the unshifted centres. A validity of this extrapolation demonstrated by the fact that the extrapolated values in column 4 of Table 4.4 agree with each other (to within their uncertainties) despite having very different extrapolation slopes.

All linecentres are corrected to the zero-power value using the slopes shown in Figures 4.5 through 4.7 and in Table 4.4. The uncertainty of the fit slope is included in the correction. The slope correction and its uncertainty (columns 11 and 12 in Table A.2) account for all of the microwave-power-dependent systematic effects described in this chapter. Table 4.5 shows the average of extrapolation results for all 18 timings used in the experiment. Consistency in extrapolated linecentres with

Pulse duration D [ns]	Measured P/T slope $[\text{Hz}/(W/\mu s)]$	Measured $P/T$ slope uncertainty $[Hz/(W/\mu s)]$	Extrapolation frequency [Hz]	Extrapolation uncertainty [Hz]	Simulated $P/T$ slope [Hz/(W/ $\mu$ s)]
50	0.63	0.13	2291176583	20	-1.64
100	2.11	0.05	2291176593	9	-2.45
125	2.54	0.44	2291176607	29	-1.93
150	3.80	0.43	2291176591	25	-3.78
200	6.5	1.4	2291176555	40	-5.35

Table 4.4: Result of microwave power extrapolation

different (T, D) combinations verifies the validity of the power extrapolation.

One concern is that the size of the extrapolation depends on the level of the microwave phase and amplitude distortions. More severe distortions are intentionally introduced to the microwave system to test the variation in the extrapolation. This resulted in an extrapolation with a significantly larger slope for graphs similar to Figure 4.5, but still gave the same value for the linecentre when extrapolated to  $P_{mw} = 0$ , verifying that any effect due to the microwave pulse imperfection (independent of the size of the distortion) is cancelled when the data is extrapolated to zero microwave power.

T [ns]	D [ns]	Linecentre $\nu_{\rm exp}$ [Hz]	$\Delta \nu \; [\text{Hz}]$
300	50	2291176598(44)	+8
300	100	2291176602(13)	+12
300	150	2291176612(24)	+22
375	125	2291176593(35)	+13
400	50	2291176584(40)	-6
400	100	2291176593(15)	+3
400	200	2291176564(35)	-26
450	150	2291176575(27)	-15
500	50	2291176565(46)	-25
500	100	2291176580(19)	-10
500	125	2291176616(27)	+26
600	50	2291176525(61)	-65
600	100	2291176602(30)	+12
600	150	2291176574(39)	-16
600	200	2291176576(68)	-14
700	100	2291176529(22)	-61
800	100	2291176612(50)	+22
900	100	2291176609(83)	+19

Table 4.5: Summary of extrapolation results for various T and D. Extrapolated linecentres are averaged separately for different (T,D) combinations.  $\Delta \nu = \nu_{\rm exp} - \nu_{12}$  is the difference from the final measured result of  $\nu_{12} = 2291176590$  Hz. One standard deviation uncertainties are shown in parentheses.



Figure 4.8: Imperfect polarization. Panel (a) shows the ideal experiment, where only intended transitions are driven. In (b), imperfect 1083-nm laser polarization drives the  $\Delta m_J = -1$  transition. Panel (c) shows a microwave polarization imperfection causing the  $\Delta m_J = -1$  transition. Both situations in (b) and (c) make the effective DC Zeeman shift rate different depending of the level of the polarization imperfection. Panel (d) shows possible transitions when both laser and microwave polarizations are misaligned. There could be a possible interference effect due to a recombination of excitation paths in (d). The dashed lines indicate the unintended transitions.

# 4.3 Imperfect Laser and Microwave Polarization

Figure 4.8(a) shows the ideal experiment where both the 1083-nm laser and microwave drive only intended transitions  $(2^{3}S_{1}(m_{J}=+1)-to-2^{3}P_{1}(m_{J}=+1))$  and  $2^{3}P_{1}(m_{J}=+1)-to-2^{3}P_{2}(m_{J}=+1)$ . When the polarizations of the laser and microwave fields are not perfectly aligned with the quantization axis of atoms (set by the direction of applied magnetic field), unintended transitions ( $\Delta m_{J}=\pm 1$ ) are also weakly driven, and these transitions could cause systematic shifts of linecentres. This section describes the effects due to the imperfect polarizations of the laser and microwave fields.

### 4.3.1 Imperfect 1083-nm laser polarization

Figure 4.8(b) shows the possible transitions driven by the 1083-nm laser whose polarization is not perfectly aligned with the quantization axis of the atoms. Imperfect 1083-nm laser polarization excites atoms in the  $2^{3}S_{1}(m_{J}=+1)$  state to both the  $2^{3}P_{1}(m_{J}=0)$  and  $2^{3}P_{1}(m_{J}=+1)$  states prior to the FOSOF experiment sequence. The microwave then drives both the  $2^{3}P_{1}(m_{J}=0)$ -to- $2^{3}P_{2}(m_{J}=0)$  and  $2^{3}P_{1}(m_{J}=+1)$ -to- $2^{3}P_{2}(m_{J}=+1)$  transitions. These two microwave transitions have different quadratic Zeeman shift rates (0.5283 kHz/G<sup>2</sup> and 0.4295 kHz/G<sup>2</sup>, respectively [33,54]), and thus the effective DC Zeeman shift depends on the fractional population in  $2^{3}P_{1}(m_{J}=0)$  (due to the unintended laser excitation). In order to ensure a well-defined DC Zeeman shift, a high purity in the 1083-nm laser polarization is required.

The polarization of the laser is checked by the method described in Section 2.8. A large magnetic field is applied around the experiment region and the strengths of possible transitions are observed while scanning the 1083-nm laser tuned to the  $2^{3}S_{1}$ -to- $2^{3}P_{1}$  transition. The 1083-nm laser power and pulse duration are increased (by a factor of 10) to exaggerate the effect of the wrong polarization. Figure 4.9 shows an averaged oscilloscope trace of the ionization signal during such a frequency scan of the 1083-nm laser. It shows a slight sign of a left-over population in  $m_{J}=-1$ 



Figure 4.9: 1083-nm laser polarization test. The inset shows possible transitions. The arrows indicate the positions at which transitions are expected to appear. A small sign of a  $2^{3}S_{1}(m_{J}=-1)$ -to- $2^{3}P_{1}(m_{J}=-1)$  transition is seen on the plot, but the unintended  $\Delta m_{J}=\pm 1$  transitions are not seen on this scale.

state from optical pumping, but no sign of wrong polarization is observed (multiple peaks at different locations are expected when the polarization is imperfect, refer to Figures 2.17 and 2.18). To test this further, an AOM was used to tune the laser frequency, and the size of the FOSOF amplitude was measured at frequencies where transitions due to the wrong polarization are expected. The amplitude of these signals was measured to an accuracy of 0.1% of the main FOSOF amplitude, and no sign of unintended transitions were detected.

For a typical experiment, the applied magnetic field is 5 G, causing the intended and unintended transitions to be separated by 10 MHz. The spectral width of the 15-ns 1083-nm laser pulse is 67 MHz, so both transitions are within the spectral width. Assuming 0.1% as the highest limit of the polarization component driving the unintended transitions, 0.09% relative population between the  $2^{3}P_{1}(m_{J}=+1)$ and  $2^{3}P_{1}(m_{J}=0)$  states is expected at 5-G field (since the power of the laser pulse drops by 10% at 10 MHz away from resonance). The effect of the 0.09% relative population to the quadratic Zeeman shift rate is small. Comparison of linecentres between low and high fields shows no inconsistency (Table 4.2), which further indicates that there is no effect due to imperfect laser polarization.

#### 4.3.2 Imperfect Microwave Polarization

Figure 4.8(c) shows possible transitions in the case of imperfect microwave polarization. The microwaves drive the  $\Delta m_J = -1$  transition  $(2^3 P_1(m_J = +1)-to-2^3 P_2(m_J = 0))$ transition) with its unintended polarization component. The signal due to the unintended transition causes a linecentre shift. Due to the curvature of the microwave magnetic field inside the coaxial airline (refer to Figure 4.2), the unintended polarization component is always present.

In [33], Borbely discusses the method of observing the effect due to the neighbouring transitions, by tuning the size of the applied magnetic field such that the SOF signals from the neighbouring transitions are either in phase or 90 degrees out of phase with the main SOF signal. When two signals are in phase, the addition of the signals causes no shift in linecentre. Signals that are 90 degrees out of phase maximize the effect of neighbouring transition. Comparison between the two experiments sets a limit on the size of possible shifts. In this experiment, the same method was used to test for possible effects, and no inconsistency was found between linecentres obtained in the two types of experiments. Also, the effect of neighbouring transition is expected to be smaller for larger magnetic fields. For a larger magnetic field, the neighbouring  $\Delta m_J = \pm 1$  transitions become more off-resonant (due to the first-order Zeeman effect) from the intended transition, suppressing the signal due to the unintended transition. The consistency of linecentres obtained at different magnetic fields supports the fact that imperfect microwave field polarization was not an issue in the present measurement.

### 4.3.3 Imperfect Laser and Microwave Polarization

Figure 4.8(d) shows the situation where both the laser and microwave have imperfect polarization components. In this situation, atoms starting from the  $2^{3}S_{1}(m_{J}=+1)$ are excited to both  $2^{3}P_{1}(m_{J}=+1)$  and  $2^{3}P_{1}(m_{J}=0)$  states. Imperfect microwave polarization drives  $\Delta m_{J}=\pm 1$  and  $\Delta m_{J}=0$  transitions. In this situation, in addition to the linecentre shift due to the effects discussed in earlier sections, a quantummechanical interference due to recombination of excitation paths could be significant. This effect is also expected to be strongly dependent on the applied magnetic field. A large applied magnetic field suppresses the recombination channel, and, again, the consistency of linecentres at different magnetic fields indicates that the effect is not significant for the present work.

# 4.3.4 Conclusion on Effects due to Imperfect Laser and Microwave Polarizations

All effects described in this section are strongly dependent on the size of applied magnetic field, and they are most directly tested by comparing measured linecentres at different applied fields. Table 4.2 shows the summary of experimental results for different magnetic field settings. Consistency of linecentres demonstrated in Table 4.2 verifies that the effects due to imperfect polarizations are smaller than the level of precision of the current experiment. The effect of imperfect polarization would be expected to change sign for the  $m_J=+1$  experiment (such as shown in Figure 4.8) and the analogous  $m_J=-1$  experiment. Linecentres from the  $m_J=+1$  and  $m_J=-1$ experiments show a difference of  $(+8\pm17)$  Hz. The difference is consistent with zero, and it indicates that the size of any potential polarization related shifts are smaller than the final quoted uncertainty of 25 Hz for the current work.

# 4.4 Effect of Microwave Fields on Rydberg Atoms

There is a concern for possible linecentre shifts due to  $18^{3}P_{2}$  Rydberg atoms being influenced by the microwave fields. During the travel from the  $2^{3}P$ -to $18^{3}P$  excitation location to the ionizer, the Rydberg atoms are exposed to multiple microwave pulses. A particular concern is that the microwaves drive high-*n* Rydberg transitions due to the 0.22-ns pulse of microwave electric field discussed in Section 4.2.2. The matrix elements of electric dipole Rydberg transitions are large, and this causes a large power broadening of transitions. This broadening, along with the spectral width of 4.5 GHz due to the 0.22-ns duration of these pulses, allows transitions to be driven even when the applied microwave frequency is far off-resonance from the Rydberg transitions. Since these microwave pulses are in the FOSOF microwave configuration (alternating between  $f + \delta f$  and  $f - \delta f$ ), it is imaginable that the microwave transitions between Rydberg states could cause sinusoidally changing signals and add an additional phase onto the main FOSOF signal. The added phase could lead to a systematic shift. The effect of additional microwave pulses on the Rydberg atoms (and therefore on the detected ion signal) is investigated by performing three different experiments.

### 4.4.1 Downstream- vs. Upstream-Experiment Location

One test for microwave pulses affecting Rydberg atoms, is to change the position of the laser excitations within the microwave region. Figure 4.10 shows the two locations used for this test. During the travel between the excitation location to the ionizer, Rydberg atoms experience multiple microwave pulses. Table 4.6 summarizes



Figure 4.10: Upstream and downstream interaction locations.

the expected average number of microwave pulses that atoms experience during the travel. From the geometry of the 14-mm coaxial airline described in Sections 2.11.2.3 and 4.2.1, atoms spend average time of  $1.81 \,\mu$ s and  $11.1 \,\mu$ s after being excited to the Rydberg state at the downstream and upstream locations, respectively. The number of pulses seen by the atoms during the travel decreases for larger value of T due to a lower duty cycle. When atoms are excited at the upstream location, the atoms see a significantly larger number of pulses during the flight (as seen on Table 4.6). Experiments are performed at the upstream location with the timing parameters  $T=300 \,\mathrm{ns}$ , and  $D=100 \,\mathrm{ns}$ , and the result is compared to the result of identical experiment performed at the downstream location. The test revealed no inconsistency between data taken at the downstream and upstream locations, with

	Pulse duration $D$ [ns]	Number of pulses $N_{downstream}$	Number of pulses $N_{upstream}$
300	100	4.5	27.7
400	100	3.6	22.2
500	100	3.0	18.5
600	100	2.6	15.9
700	100	2.3	13.9
800	100	2.0	12.3
900	100	1.8	11.1

Table 4.6: Average number of microwave pulses experienced by the atoms for different pulse separations T for experiments taking place at the downstream and upstream locations.

a difference between the linecentres of  $(3\pm 9)$ Hz.

## 4.4.2 Detection States

The 1532-nm diode laser driving the  $4^{3}$ D-to- $18^{3}$ P transition has a wide tuning range, and can be tuned to the  $4^{3}$ D-to- $18^{3}$ F transition. The  $18^{3}$ F state can be used instead of  $18^{3}$ P state as a detection state to test for a detection-state-dependent effect. The  $18^{3}$ P and  $18^{3}$ F states behave differently (including having different resonant frequencies for driving allowed transitions) when exposed to DC or AC electric field. The  $18^{3}$ F state is more susceptible to the external DC electric field; whereas, the  $18^{3}$ P state, because of its larger energy defect, does not shift (or mix with other states) as readily. A comparison between measurements using the  $18^{3}$ F and  $18^{3}$ P state shows a linecentre difference of  $(28\pm 24)$  Hz. The level of consistency between



Figure 4.11: Low duty cycle experiment timing. The coloured rectangles represent the laser pulses (1083-, 447-, 1532-nm lasers), and the rectangles with labels  $f + \delta f$  and  $f + \delta f$  represent the microwave pulses. Experiment reversal is done by switching microwave pulse timings, and it causes a phase offset between two experiments, leading to a systematic shift.

the  $18^{3}$ P and  $18^{3}$ F data adds to our confidence that the interaction between the microwaves and the Rydberg atoms does not cause a shift.

# 4.4.3 Low Duty Cycle Experiments

Low duty cycle experiments (as shown in Figure 4.11) are performed as another test for the possible effect of microwave pulses on the Rydberg atoms. Reducing the duty cycle temporally separates subsequent experiments further apart, and reduces the number of microwave pulses seen by the Rydberg atoms. It is possible to set the duty cycle such that all atoms are completely cleared from the microwave region before the subsequent experiment cycle starts. This ensures that the linecentres obtained are not influenced by the additional microwave pulses.

Figure 4.11 illustrates the timing of the low duty-cycle experiment for the FOSOF experiment I and II. Unlike the normal operation of the FOSOF experiment where the laser pulse timings are shifted to switch between experiment I and II, timing of microwave pulses also must be switched for the low duty-cycle experiments. This type of experiment reversal is not ideal since it causes the microwave switches to operate differently for experiments I and II. The result is that experiments I and II no longer form a perfect reversal and there is a net phase shift in the average FOSOF signal from the two experiments. The effect of imperfect experiment reversal is tested by mixing the CW output of the microwave generator with the microwave pulses used in the experiment. The interference between two signals generates a sine wave which mimics a FOSOF signal, and its phase with respect to the FOSOF beat reference signal is monitored during the experiment reversal. It was found that the experiment reversals at lower duty cycles do not lead to a perfect cancellation of phase shifts, and consequently, the measured linecentres at low duty cycles are inconsistent with linecentres measured at normal duty cycle. It was, however, possible to correct the linecentre obtained at a particular duty cycle by the phase offset observed from the beating the pulses with CW microwaves (as described above) during this test. Correcting for the observed phase shifts, a consistency in linecentres was restored. The consistency was tested to a precision of 100 Hz. The precision of the performed test is not at the level of the current experiment; however, the origin of the systematic effect due to imperfect experiment reversal at low-duty cycle is well understood, and this test complements the tests of Sections 4.4.1 and 4.4.2.

### 4.4.4 Conclusion for the Effect of Microwave Fields on Rydberg Atoms

Three different experiments described in this section test the possible systematic effect due to the Rydberg atoms being influenced by the additional microwave pulses. A comparison between downstream/upstream experiments along with the consistency demonstrated in Section 4.2.5 for different pulse separations rules out the possibility of additional pulses affecting the linecentres. All other tests are also consistent with Rydberg atoms playing no significant role in the current measurement.

## 4.5 Laser Light Shifts

Overlap between laser pulses and microwave pulses during the experiment cycle could lead to a linecentre shift due to a light shift (AC Stark shift due to the electric fields of the laser light). The 1083- and 447-nm lasers driving  $2^{3}S_{1}$ -to- $2^{3}P_{1}$ and  $2^{3}P_{2}$ -to- $2^{3}D_{3}$ , respectively, could shift the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition if the laser light and microwaves temporally overlap. Overlap of the 1532-nm laser with the microwave pulse is less of a concern because this laser is not directly related to transitions involving  $2^{3}P_{1}$  and  $2^{3}P_{2}$  states. Experiments with different laser-pulse timings and laser powers were performed to test for the possible effect of light shifts, as described below.

## 4.5.1 Experiments with Varied Laser Pulse Timings

Figure 4.12 shows the timing diagrams of three experiments performed to test the effect due to the overlap between the laser pulses and microwave pulses. Laser pulse timings are changed in each of the experiments shown in the figure. In Figure 4.12(a), the 1083-nm laser pulse is shifted by 30 ns earlier in time, separating it further away in time from the microwave pulse. AOM pulsing has a ringing effect caused by the RF pulse reflections inside the AOM crystal. This effect leaves an unsuppressed laser power for some time even after the pulse is turned off [33]. By separating the pulse further from the microwave pulse, any effect associated with the overlap of the tail of the 1083-nm laser can be suppressed.



Figure 4.12: Experiments with varied laser pulses timings. The rectangles represent the laser and microwave pulses used for the experiment. 1083-nm laser pulse (laser A), 447-nm laser pulse (laser B), and 1532-nm laser pulse (laser C) are represented as the red, blue, and green rectangles, respectively. The purple rectangles represent the microwave pulses.

Figure 4.12(b) shows another experiment timing where the detection laser pulses are shifted by 30 ns later in time, again making them further away from the microwave pulse. Since the 447-nm laser pulse starts after the second microwave pulse, and the time between the laser pulse and next microwave pulse (the first pulse of the next experiment cycle) is over 100 ns (even further for larger pulse separation settings), the ringing effect is not a concern in this case. The overlap of the rising edge of the 447-nm detection laser with the falling-edge of the second microwave pulse is tested with this experiment.

Figure 4.12(c) shows the experiment that tests the overlap of 1532-nm laser with

the microwave pulses. In this experiment, the 1532-nm laser simply runs in the CW mode. The laser overlaps with both microwave pulses. If there is any effect on the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition due to the 1532-nm laser, the effect is greatly exaggerated in this experiment.

### 4.5.2 Experiments with Different Laser Powers

An AOM spatially separates the undiffracted and first-order diffracted paths, making the overlap of the two paths very unlikely. However, if there is an imperfect separation of the two paths, it causes a small laser power to be always present during the experiment, which could induce a light shift. In the previous section (Section 4.5.1), experiments to test the laser-microwave overlap are discussed. These experiments, however, do not test the light shift due to the presence of the unintended CW laser power during the experiment. In order to test for this effect, the 1083and 447-nm laser powers are reduced to 10 % and 12.5 % of the typical operating power, respectively. Two experiments were performed separately to avoid significant reduction of signal-to-noise ratio. In one experiment, 1083-nm laser power is reduced, leaving the 447-nm laser power unchanged. In the other experiment, the 447-nm laser power is reduced, and the 1083-nm laser power is unchanged.

Experiment	Linecentre $\nu_{\rm exp}$ [Hz]	$\Delta \nu \; [\text{Hz}]$
447-nm laser $+30$ ns	2291176566(34)	-24
1083-nm laser - $30$ ns	2291176568(33)	-22
1532-nm laser CW	2291176583(24)	-7
10% 1083-nm laser power	2291176603(22)	+13
12.5%447-nm laser power	2291176572(38)	-18

Table 4.7: Summary of experimental results testing laser light shifts.  $\Delta \nu = \nu_{\rm exp} - \nu_{12}$  is the difference between the measured linecentre  $\nu_{\rm exp}$  and the final measured result of  $\nu_{12} = 2\,291\,176\,590\,\text{Hz}$ . One standard deviation uncertainties are shown in parentheses.

## 4.5.3 Conclusion for Laser Light Shifts

Five different experiments are performed to test for light shifts. Table 4.7 summarizes the results of the five experiments. Results from the three timing experiments reveal no inconsistencies in measured linecentres. The differences in measured linecentres with respect to the final measured result of 2 291 176 590 Hz are  $(-22\pm33)$  Hz,  $(-24\pm34)$  Hz, and  $(-7\pm24)$  Hz for experiments with varied 1083-nm laser pulse timing, varied 447-nm laser pulse timing, and CW-mode 1532-nm laser, respectively. Comparison of the experimental results with different laser powers showed differences of  $(+13\pm22)$  Hz and  $(-18\pm38)$  Hz for the reduced 1083- and 447-nm laser powers, respectively. These differences are consistent with zero. The (unlikely) possibility of having any light-shift-related systematic effect is suppressed to the level of agreement demonstrated in these experiments.
## 4.6 First-Order Doppler Shifts

In the present experiment, the microwave propagation directions intersect perpendicularly with an atomic beam. Imperfect alignment of the microwave region with respect to the atomic beam axis leads to a shift in linecentre due to the first-order Doppler shift. The Doppler shift can be written as

$$\Delta \nu_{\text{Doppler}} = \nu_0 \beta \Delta \theta, \qquad (4.8)$$

where  $\nu_0$  is the frequency of the microwave,  $\Delta\nu_{\text{Doppler}}$  is the shift in frequency,  $\beta = \frac{v}{c}$ where v is the average speed of the atoms, c is the speed of light in vacuum, and  $\Delta\theta$  is the angle at which the atoms intersect with the microwave (where  $\Delta\theta = 0$  is defined by the atomic and microwave propagation directions being perpendicular). The entire system is aligned using a surveyor's scope, and the maximum deviation from the perfect alignment angle is very conservatively estimated to be less than 5 mrad (including the size of the slit at the microwave region and its distance from the helium source). The shift due to the first-order Doppler effect in this experiment is expected to be small because of the slow atomic speed (1100 m/s) and the small microwave frequency. The upper limit of the first-order Doppler shift is 42 Hz using Equation 4.8. However, a reflection of the microwave from the short ensures that the effect on the measured linecentres is much smaller than this 42-Hz limit for the present experiment. Even with the assumption of a 1% power difference between the forward and reverse going microwaves, the 42 Hz estimate becomes 0.42 Hz, and is completely negligible.

## 4.7 Time-Base Correction

The time base of the Wiltron microwave generator is used to synchronize instruments for the experiment. The 10-MHz clock output of the Wiltron generator is daisy chained to other instruments that require clock synchronization and monitored at the end of the chain using a frequency counter (TTi960) referenced to a Rb frequency standard (FE-5680A). The frequency of the Rb clock is checked against a GPS disciplined clock (Trimble Thunderbolt E) on a weekly basis, to ensure that there is no frequency drift of the Rb clock over time. The Rb clock frequency stayed extremely stable over the course of data acquisition. The clock frequency of the Wiltron generator, monitored over the entire data acquisition, is shown in Figure 4.13. The time-base correction is calculated by the fractional deviation of the generator clock frequency from the 10 MHz Rb clock frequency,

$$\Delta \nu_{\text{time base}} = \frac{10 \text{MHz(Wiltron)} - 10 \text{MHz}}{10 \text{MHz}} \times 2.291 \text{GHz.}$$
(4.9)

The typical time-base correction applied to the measured linecentre is 4.5 kHz. The clock frequency drifted by maximum 0.015 ppm over the period of data acquisition which corresponds to the time-base correction drift of 30 Hz. Since the time base



Figure 4.13: Wiltron clock frequency drift

is measured very accurately, the corrections are also known very accurately, and the uncertainties in these corrections are very small compared to the 25-Hz final uncertainty of our measurement.

# 4.8 Analysis-Related Systematic Effects

To test for possible analysis-related systematic effects, the data analysis was repeated with different data restrictions. Additionally, SOF signals were reconstructed using FOSOF data, and the entire data set was re-analyzed based on SOF fits. Details on results based on different analysis parameters are discussed in this section.

#### 4.8.1 Saturation Restriction *PD*<sup>2</sup>: Linearity of Power Extrapolation

The linecentre shifts discussed in Section 4.2 become more significant for higher powers. The shifts discussed in that section were linear in power; however, a nonlinear behaviour in linecentre shifts was observed for powers approaching the saturation of the transition. To avoid the effects of this nonlinearity only the linecentres taken at the lowest powers are included in the analysis. Additionally, the maximum power  $P_{\text{max}}$  included is varied to ensure that no systematic shifts are present due to the nonlinearity in the extrapolation of the linecentres to zero power. The criteria for choosing  $P_{\text{max}}$  is based on the saturation parameter  $PD^2$ , which determines the degree of the transition for a particular combination of P and D. The maximum value of  $PD^2$  used in the experiment was  $0.9 \text{ W}\mu\text{s}^2$ . The entire data analysis was repeated with different  $P_{\text{max}}D^2$  restriction (0.9, 0.75, 0.6, 0.45, and  $0.3 \,\mathrm{W}\mu\mathrm{s}^2$ ) to check the linearity of the extrapolation. The analysis results with different  $P_{\text{max}}D^2$  restrictions are compared in Table 4.8. The consistent results in the table verifies that the extrapolation is not affected by the nonlinearity for the powers used in the analysis.

Saturation restriction $PD^2$ [W $\mu$ s <sup>2</sup> ]	Linecentre $\nu_{\rm exp}$ [Hz]	$\Delta \nu  [\text{Hz}]$
0.3	2291176588(21)	-2
0.45	2291176592(16)	+3
0.6	2291176602(13)	+12
0.75	2291176590(11)	0
0.9	2291176590(11)	0

Table 4.8: Summary of analysis results from different saturation restrictions  $P_{\text{max}}D^2$ .  $\Delta \nu = \nu_{\text{exp}} - \nu_{12}$  is the difference between the measured linecentre and the final measured result of  $\nu_{12} = 2291176590$  Hz. The result from the analysis using  $P_{\text{max}}D^2=0.75$  Wµs<sup>2</sup> was used to quote the final measured result, so the difference to  $\Delta \nu$  is zero. The saturation restriction used for quoting the final measured result (0.75 Wµs<sup>2</sup>) is highlighted in gray.

#### 4.8.2 Frequency Range of the FOSOF Fits

The envelope width  $(\frac{1}{D})$  of the FOSOF signal (see Figure 3.4) was used to set the frequency range used in data acquisition. Data were typically collected over the range between  $(f_0 - 1/(2D) - 2.5)$  MHz and  $(f_0 + 1/(2D) + 2.5)$  MHz. Different frequency ranges (full range,  $|f - f_0| < \frac{1}{2D}$ ,  $|f - f_0| < \frac{1}{4D}$ , and  $|f - f_0| < \frac{1}{8D}$ ) are used to fit the collected data, and obtained linecentres are analyzed. Figure 4.14 shows FOSOF data at different powers and corresponding fits. The frequency ranges

Pulse duration [ns]	Full range [MHz]	1/(2D) range [MHz]	1/(4D) range [MHz]	1/(8D) range [MHz]
50	25	20	12.5	10
100	15	5	2.5	1.25
125	13	4	2	1
150	11.7	3.3	1.7	0.8
200	10	2.5	1.25	0.625

Table 4.9: Frequency range used for fitting the data. The frequency ranges vary from 0.625 to 25 MHz.

Fit range	Linecentre $\nu_{\rm exp}$ [Hz]	$\Delta \nu \; [\text{Hz}]$
Full range	2291176590(12)	0
1/(2D)	2291176590(11)	0
1/(4D)	2291176615(14)	+25
1/(8D)	2291176595(16)	+6

Table 4.10: Analysis results with different fit ranges.  $\Delta \nu = \nu_{\exp} - \nu_{12}$  is the difference from the final measured result of  $\nu_{12} = 2.291\,176\,590$  Hz. The analysis range of 1/2D is used to quote the final measured result and is highlighted in gray. The results shown are from a reanalysis of the entire data set used in this work.

used for each analysis are indicated with gray bands. Table 4.9 summarizes the frequency ranges used for fitting. Results obtained from different fitting ranges are compared in Table 4.10. The results reveal no significant inconsistency amongst the analysis results.

#### 4.8.3 SOF Reconstruction Using FOSOF Data

The amplitude of the FOSOF signal along with corresponding phase information can be used to reconstruct SOF signals from the FOSOF experiment data. To do this, the FOSOF amplitude is multiplied by the cosine of  $\overline{\Delta \theta}$ . Simulations were performed for both the SOF and FOSOF experiments, and a small deviation between the two types of measurement was found. A small offset in the linecentre extrapolation (to zero microwave power) was predicted for the case of the SOF experiment, whereas the FOSOF linecentres extrapolate exactly to the atomic resonance ( $f_0$ ) in these simulations. The SOF signal for the current measurement was reconstructed from



Figure 4.14: Illustration of fit ranges used for data analysis. The figure shows a full range fit to a (T,D)=(400,100) ns data. The gray bands indicate the different fit ranges used in the analysis. The different powers are unresolved in panel (a)

each FOSOF data run and was re-fit with the SOF lineshape of Equation 3.12. Obtained linecentres are extrapolated to zero microwave power. The averaged linecentre slightly deviates from the result of FOSOF experiment. Two values differ (when averaged over the entire data set) by  $(60\pm42)$  Hz, where the uncertainty is dominated by the SOF average linecentre.

## 4.9 Other Tests for Possible Systematic Effects

As described in Section 2.12, various experimental parameters are monitored over the course of data acquisition. Most of the logged parameters are not expected to be related to any systematic effects. However, if a correlation between the measured linecentres and logged parameter were found, further systematic studies would be required. Table 4.11 shows linecentre differences and their associated uncertainties for different logged parameters, and also shows the parameter ranges. Linecentres as a function of each parameter given in the table are fit to a linear model, and the difference from the minimum parameter value to the maximum parameter value is determined. In all cases, no significant shifts are found.

The source operation parameters are tested by changing the driving current and temperature. When the current is changed, the source operates differently (the atomic flux changes, and the relative production efficiencies of UV photons, singletand triplet-metastable helium atoms also changes). The source temperature tests

Parameter	$\Delta$ [Hz]	Uncertainty [Hz]	Minimum value	Maximum value
Source current	-4	12	$10.0\mathrm{mA}$	25.0 mA
Source temperature	+24	53	$-158^{\circ}\mathrm{C}$	$+30^{\circ}\mathrm{C}$
Chamber pressure	-7	53	$3 \times 10^{-9}  \mathrm{torr}$	$6.7 \times 10^{-8} \mathrm{torr}$
Offset frequency	+45	23	$-2800\mathrm{Hz}$	$+2800\mathrm{Hz}$
2DMOT	-22	33	OFF	ON
$m_J$ state	+8	17	-1	+1
$B_x$ -coil current	+3	10	$-16.3\mathrm{mA}$	$-11.0\mathrm{mA}$
$B_y$ -coil current	+3	11	$57.2\mathrm{mA}$	$60.8\mathrm{mA}$
$B_z$ -coil current	+7	11	$144.1\mathrm{mA}$	$147.5\mathrm{mA}$
Ambient temperature	-18	16	$26.1\mathrm{C}^\circ$	$31.9\mathrm{C}^\circ$
Run start time	+1	9	$0 \mathrm{day}$	$43.6\mathrm{days}$

Table 4.11: Table of linecentre comparisons for tests of other systematic effects.  $\Delta$  denotes the difference in linecentres between the miminum and maximum values of parameters.

for atomic-speed-dependent effects.

Currents to all background magnetic field cancelling coils  $(B_x, B_y \text{ and } B_z \text{ in}$ Table 4.11) are monitored. A variation in linecentres with these coil currents tests for laser- and microwave-polarization effects.

Ambient temperature could cause small variation in electrical length of the microwave system, causing instability in microwave system operation. This may cause shifts discussed in Section 4.2.5. If there is any time-dependent effect such as magnetization of system components close to the experiment region and degradation of microwave components over time, it should show up in the run start time parameter. No significant deviations in linecentres are found from the comparisons (shown in Table 4.11).

#### 4.9.1 Offset-Frequency Correction

The two microwave generators used in the current experiment have different frequency resolutions. The Wiltron microwave generator has a resolution of 0.1 Hz, whereas the HP generator frequency can only be set in steps of 1 kHz. Because of this limitation, the frequency f is nominally set by the HP generator, and the offset frequency  $f + 2\delta f$  is set by the Wiltron generator (as opposed to setting the two frequencies symmetrically to  $f - \delta f$  and  $f + \delta f$ , as was described in 2.11.1.2). Therefore, the offset frequency  $\delta f$  needs to be added to the measured linecentres in order to obtain the true FOSOF resonance position. The typical offset frequency used in the experiment is  $2\delta f = 280$  Hz. Linecentres with offset frequencies ranging from -2.8 kHz to +2.8 kHz are also used to test for any possible systematic effects. Consistent linecentres are observed within the range of offset frequencies, eliminating the possibility of offset-frequency-dependent shifts, as shown in Table 4.11.

#### 4.9.2 Pressure Shifts

The typical operating vacuum pressure inside the main experiment chamber is  $3 \times 10^{-9}$  torr and is dominated by the helium gas load from the metastable helium source. To set a limit for the size of a possible pressure shift, the pressure was increased to  $6.7 \times 10^{-8}$  torr and the linecentre was measured at that pressure. Since

atoms may behave differently when colliding with gas molecules other than helium, it was important to keep the experimental environment as similar as possible to the normal operating environment in performing this experiment. Therefore, the pressure was increased by slowing down the turbo pump at the main experiment chamber instead of leaking gas into the chamber using a leak valve. This method ensures that the fractional composition of the residual gas is unchanged when the pressure is increased. The measured linecentres at the two pressures showed a difference of  $(-7\pm53)$  Hz, which is consistent with zero. Since the pressure shift is expected to grow linearly with pressure, the limit on the pressure shift at  $3 \times 10^{-9}$  torr (where the main data were taken) is 3 Hz.

#### 4.9.3 Atomic Beam Intensity

The test for the pressure shift (Section 4.9.2) only concerns collisions of helium atoms with the background gas. In the current experiment, a 2DMOT is used to intensify the atomic beam. A high density of atoms could, though unlikely, cause a systematic shift due to collisions of atoms within the beam. Atoms within the beam collide with others due to the transverse and longitudinal velocity spread. To test for this possible systematic effect, linecentres are measured with or without operation of the 2DMOT. Results from the two experiments shows a difference of  $(-22\pm33)$  Hz. Another test performed with different source driving current (which reduces the atomic flux by a factor of 2) also shows no sign of linecentre shift, with a difference of  $(-3\pm12)$  Hz.

#### 4.9.4 Microwave Amplitude Variation due to Travelling Atoms

During the experiment cycle, atoms travel a small distance inside the coaxial airline. As described in Section 4.2.1, the amplitude of the field varies as 1/|r| (r is measured from the central axis of the coaxial airline). Atoms see different pulse amplitudes for the two microwave pulses due to the difference in positions at which atoms experience the first and second microwave pulses. Figure 4.15(a) illustrates the 1/|r| field variation inside the coaxial airline, and Figures 4.15(b) and 4.15(c) show the pulse amplitudes seen by the atoms as a function of time for the upstream and downstream locations. The variation is as large as 20 % for the largest pulse separation T used in the current experiment.

No shift was expected from the field amplitude imbalance. The consistency of experimental results with different pulse separations T (demonstrated in Section 4.2.5) verifies that this effect does not contribute to a shift in linecentres. The experiment described in Section 4.4.1 also tests for this effect because atoms travel closer to (upstream) or further from (downstream) the inner conductor so that the field imbalance is reversed, as seen in Figures 4.15(b) and 4.15(c).



Figure 4.15: Microwave field strength variation inside the coaxial airline. (a) shows the field variation inside the coaxial airline as a function of distance. The pink arrow indicates the helium atoms moving to the right of the figure. (b) and (c) show the field strength variation seen by the atoms during one experiment cycle with (T,D)=(500,100) ns for upstream and downstream experiment locations, respectively.

# 5 Conclusion

The  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  fine-structure interval in atomic helium was measured using the frequency-offset separated-oscillatory-fields (FOSOF) technique. This work was the first demonstration of the FOSOF technique. An outstanding signal-to-noise ratio was achieved by employing a two-dimensional magneto-optical trap and a Stark-ionization detection scheme (described in Chapter 2). Collected data were fit to an analytic solution derived in Chapter 3. The quality of the fit confirmed that the experimental data were well described by the theoretical prediction (Figures 3.7 through 3.12). The excellent signal-to-noise ratio allowed for a very extensive study of systematic effects. A wide range of experimental parameters was investigated. A systematic effect pertaining to the microwave pulse imperfection was found during the experiment (Section 4.2.4), and was dealt with by extrapolating our measurements to zero microwave power (Section 4.2.5). A significant quantity of data was necessary to understand the systematic effects described in Chapter 4.

Table 5.1 shows the summary of measured linecentres with different experimental

Experimental Parameter	Parameter Detail	Linecentre $\nu_{exp}$ [Hz]	$\Delta \nu$ [Hz]	Section
Magnetic Field Direction	$\hat{z}$ $\hat{z}$	$2\ 291\ 176\ 593(12) \\ 2\ 291\ 176\ 592(13)$	$^{+3}_{+2}$	4.1
Magnetic Field Magnitude	B  < 5 $5 \le  B  \le 10$  B  > 10	$2\ 291\ 176\ 596(11)\ 2\ 291\ 176\ 592(16)\ 2\ 291\ 176\ 567(62)$	$-6 \\ +2 \\ -23$	4.1, 4.3
Timing Parameter $(T,D)$	$\begin{array}{c} (300, 50)\\ (300, 100)\\ (300, 150)\\ (375, 125)\\ (400, 50)\\ (400, 50)\\ (400, 200)\\ (450, 150)\\ (500, 50)\\ (500, 100)\\ (500, 125)\\ (600, 50)\\ (600, 100)\\ (600, 150)\\ (600, 200)\\ (700, 100)\\ (800, 100)\\ (900, 100) \end{array}$	$\begin{array}{c} 2\ 291\ 176\ 582(44)\\ 2\ 291\ 176\ 602(13)\\ 2\ 291\ 176\ 612(24)\\ 2\ 291\ 176\ 593(35)\\ 2\ 291\ 176\ 593(35)\\ 2\ 291\ 176\ 593(15)\\ 2\ 291\ 176\ 593(15)\\ 2\ 291\ 176\ 565(46)\\ 2\ 291\ 176\ 565(46)\\ 2\ 291\ 176\ 565(46)\\ 2\ 291\ 176\ 565(46)\\ 2\ 291\ 176\ 525(61)\\ 2\ 291\ 176\ 525(61)\\ 2\ 291\ 176\ 574(68)\\ 2\ 291\ 176\ 574(68)\\ 2\ 291\ 176\ 574(68)\\ 2\ 291\ 176\ 529(22)\\ 2\ 291\ 176\ 612(50)\\ 2\ 291\ 176\ 609(83)\\ \end{array}$	$\begin{array}{r} +8\\ +12\\ +22\\ +3\\ -6\\ +3\\ -26\\ -15\\ -25\\ -10\\ +26\\ -65\\ +12\\ -16\\ -14\\ -61\\ +22\\ +19\end{array}$	4.2.5
Average of $T$ Parameters	300 400 500 600	$\begin{array}{c} 2\ 291\ 176\ 577(13)\\ 2\ 291\ 176\ 592(15)\\ 2\ 291\ 176\ 591(17)\\ 2\ 291\ 176\ 589(26) \end{array}$	+13 +2 +1 -1	4.2.5
Average of $D$ Parameters	$50 \\ 100 \\ 125 \\ 150 \\ 200$	$\begin{array}{c} 2\ 291\ 176\ 591(38)\\ 2\ 291\ 176\ 590(12)\\ 2\ 291\ 176\ 607(25)\\ 2\ 291\ 176\ 600(20)\\ 2\ 291\ 176\ 563(35) \end{array}$	-1 + 0.2 + 17 + 10 - 27	4.2.5
Saturation Restriction $PD^2$	> 0.30 > 0.45 > 0.60 > 0.75 > 0.90	$\begin{array}{c} 2\ 291\ 176\ 592(21)\\ 2\ 291\ 176\ 592(16)\\ 2\ 291\ 176\ 602(13)\\ 2\ 291\ 176\ 590(11)\\ 2\ 291\ 176\ 590(11)\\ \end{array}$	-2 +2 +12 -0 +0.1	4.8.1
Detection $m_J$ State	$\begin{array}{l} m_J = +1 \\ m_J = -1 \end{array}$	$2\ 291\ 176\ 594(12) \\ 2\ 291\ 176\ 586(13)$	$^{+4}_{-4}$	4.3.3
Analysis Range	Full Range $ f - f_0  < 1/2D$ $ f - f_0  < 1/4D$ $ f - f_0  < 1/8D$	$\begin{array}{c} 2\ 291\ 176\ 590(12)\\ 2\ 291\ 176\ 590(11)\\ 2\ 291\ 176\ 615(13)\\ 2\ 291\ 176\ 595(16)\\ \end{array}$	$0 \\ 0 \\ +25 \\ +5$	4.8.2
Laser Parameters	447-nm laser timing 1083-nm laser timing Low 1083-nm laser power Low 447-nm laser power CW 1532-nm laser	$\begin{array}{c} 2\ 291\ 176\ 566(34)\\ 2\ 291\ 176\ 568(33)\\ 2\ 291\ 176\ 603(22)\\ 2\ 291\ 176\ 572(38)\\ 2\ 291\ 176\ 583(24) \end{array}$	$-24 \\ -22 \\ +13 \\ -18 \\ -7$	4.5
Atomic Beam Intensity	2DMOT OFF	2291176617(36)	+27	4.9.3
Rydberg State Detection	18F	2291176625(29)	+35	4.4

Table 5.1: Summary of experimental parameters.  $\Delta \nu = \nu_{\rm exp} - \nu_{12}$  is the difference between the measured linecentre  $\nu_{\rm exp}$  and the final measured result of  $\nu_{12} = 2\,291\,176\,590\,\text{Hz}$ . One standard deviation uncertainties are shown in parentheses.



Figure 5.1: Summary of experiment parameters. (a) shows the measured linecentres with different magnetic fields. (b) through (d) are the measured linecentres with different timing parameters of the experiment. (e) and (g) are the linecentres resulting from analysis with different data restrictions. (h) shows the linecentres with different laser parameters. (f) and (i) show auxiliary data with different optical pumping and detection states, as well as the effect of turning off the 2DMOT. From the variations seen on the plot, a conservative 25-Hz uncertainty (gray band) is assigned to the final measured result of 2 291 176 590 Hz.

parameters. Figure 5.1 shows the plot of the measured linecentres listed in Table 5.1. The gray band is the 25-Hz uncertainty band for the current measurement. Excellent consistency amongst various experimental parameters is demonstrated.

A weighted average of all data presented in Table A.2 using the normalized weights in column 15 gives the final measured result. The final result of this work is  $2\,291\,176\,590(25)$  Hz. A conservative estimate of 25 Hz was assigned to the final measured result by observing the spread of measured linecentres obtained with different experimental parameters shown in Figure 5.1. Even though the final result quotes an uncertainty of 25 Hz, a total statistical uncertainty of < 2 Hz was achieved. This measurement is completely limited by the systematic uncertainty, and there is a possibility of improving the precision by another order of magnitude if all systematic effects are well understood.

Figure 5.2 shows the statistical distributions of linecentres. The histogram was obtained by taking the differences between the individual linecentres and the final measured result and dividing this difference (column 13 of Table A.2) by the total uncertainty (column 14 of Table A.2) of the individual measurement. The histogram shows an excellent agreement with a normal distribution.

Table 5.2 shows recent measurements of the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition. Major systematic corrections are applied to laser spectroscopy results due to newly discovered quantum interference effects [57]. Figure 5.3 shows the comparison of the theoretical



Figure 5.2: Statistical distribution of linecentres.

Research group	Experiment type	Quoted value [Hz]	Corrected values [Hz]	Correction type
Shiner, et al. [31]	Laser Spectroscopy	2 291 176 900(1000)	2 291 177 100(1000)	Quantum interference [57]
Gabrielse, et al. [30]	Laser Spectroscopy	2291175590(510)	2291176790(1100)	Quantum interference [59]
Hessels, et al. [27]	Microwave Spectroscopy	2291177530(350)	2291176655(660)	Reanalysis based on $P/T$ [19]
Hu, et al. [58]	Laser Spectroscopy	2291177690(360)		
Hu, et al. [29]	Laser Spectroscopy	2291177560(190)		
This work [46]	Microwave Spectroscopy	2291176590(25)		

Table 5.2: Recent measurements of the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition with new systematic corrections. For the most recent results of the combined  $\nu_{02}$  transition, refer to [29] and [60]

calculation and experimental measurements of the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition. Our result is slightly smaller (1.5 times the estimated theoretical uncertainty) than the best theoretical prediction. It disagrees with recent laser measurements by Hu, et al. [29, 58] by 4.9 and 2.9 times their uncertainties. The SOF measurement by Hessels, et al. [27] has been reanalyzed based on the P/T linecentre extrapolation discussed in Section 4.2.5 [19]. The reanalyzed result agrees with the present measurement. This measurement is the most precise measurement to date of a helium fine-structure interval, and represents a major advance in this precision. This work sets the stage for a new level of accuracy for this fine structure, which, when combined with more precise theory, could provide <1 ppb tests of the physics and constants relevant to the interval—including a precise determination of the fine-structure constant, the most precise test of multi-electron QED, and tests for physics beyond the Standard Model.



Figure 5.3: Comparison of recent measurements of the  $2^{3}P_{1}$ -to- $2^{3}P_{2}$  transition. The blue points indicate values quoted by the research groups. The purple points are the results with quantum interference correction included. The black point is the reanalyzed result of [27] based on P/T extrapolation discussed in Section 4.2.5. The green point indicates the theoretical calculation of [26]. The red point is the current work. The plotted values are also given in Table 5.2.

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# A Table of Data Runs

Identifier	Acronym	Description
NR	Normal Run	Normal experiment running parameter
LB	Large B	B  > 10 applied to the experiment
$\mathbf{PR}$	Power Restriction	Data with $PD^2 > 0.9$
PRLB	Power Restriction Large B	Data with $PD^2 > 0.9$ and $ B  > 10$ applied to the experiment
FDET	F DETection	18F detection experiment
CWLC	CW Laser C	CW 1532-nm laser experiment
LLAP	Low Laser A Power	Reduced 1083-nm laser power
LLBP	Low Laser B Power	Reduced 447-nm laser power
LAT	Laser A Timing	Varied 1083-nm laser timing
LBT	Laser B Timing	Varied 447-nm laser timing
MOT0	MOT OFF	2DMOT turned off
UP	UPstream	Experiment performed at upstream location
UPLB	UPstream Large B	Experiment performed at upstream location with large B applied

Table A.1: Data identifier table. The table describes the interpretation of the last column in Table A.2.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Run Number N <sub>run</sub>	Pulse Separation $T$ [ns]	Pulse Duration $D$ [ns]	Microwave Power P [W]	Magnetic Field B [Gauss]	Polarizer Angle $\theta_{\rm pol}$ [degree]	Fit Linecentre $\nu_{\rm fit}~[{\rm Hz}]$	Fit Uncertainty $\Delta  u_{\mathrm{fit}}$ [Hz]	DC Zeeman Correction DC <sub>B</sub> [Hz]	Zeeman Uncertainty $\Delta DC_{B} \; [Hz]$	Slope Correction SC [Hz]	Slope Uncertainty $\Delta SC$ [Hz]	Corrected Linecentre $\nu_0$ [Hz]	Total uncertainty $\Delta \nu_0$ [Hz]	Weights wts. [%]	Data Type
123345567890111133455678901122222222222222222222222222222222222	$\begin{array}{c} 3000\\$	$\begin{array}{c} 1000\\$	$\begin{smallmatrix} 15\\ 52\\ 52\\ 52\\ 22\\ 37\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52$	$\begin{array}{c} 4,762\\ 4,762\\ 4,762\\ 4,762\\ -3,81\\ -3,$		$\begin{array}{c} 100699\\ 101051\\ 10151\\ 10151\\ 10284\\ 10117\\ 10284\\ 10117\\ 10284\\ 10017\\ 10028\\ 99200\\ 99200\\ 99200\\ 99200\\ 99200\\ 99200\\ 99900\\ 99900\\ 99900\\ 99900\\ 62270\\ 6424\\ 6343\\ 6313\\ 6313\\ 6333\\ 6333\\ 6333\\ 10030\\ 99906\\ 99906\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 99905\\ 6535\\ 6336\\ 6375\\ 6336\\ 99390\\ 6535\\ 6336\\ 99390\\ 6535\\ 6336\\ 99390\\ 6535\\ 6336\\ 99390\\ 6535\\ 6336\\ 99390\\ 6535\\ 6336\\ 99390\\ 6535\\ 6336\\ 9930\\ 75542\\ 75542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 755542\\ 7$	$\begin{array}{c} 110\\ 891\\ 138\\ 681\\ 1561\\ 858\\ 474\\ 858\\ 474\\ 105\\ 5533\\ 12401\\ 1213\\ 23010\\ 12259\\ 8868\\ 66663\\ 1213\\ 1220\\ 112\\ 98868\\ 66663\\ 1213\\ 1220\\ 112\\ 1220\\ 112\\ 12200\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220\\ 1220$	$\begin{array}{c} 97656\\ -97655\\ -97655\\ -977658\\ -977558\\ -977558\\ -977558\\ -977558\\ -97757\\ -977578\\ -97758\\ -97768\\ -97788\\$	$\begin{array}{c} 8755488888888888999999999999999999999999$	$\begin{array}{c} 981\\37286\\82754\\42953133\\42998\\2420959\\313333333333333333333333333333333333$	$\begin{array}{c} 236239463384160152668111666622226604730083746669222111156662222269439928666626751991166638666626751991166638666626751991166638666626751991166638666666666666666666666666666666$	$\begin{array}{c} 206\\ -352\\ -1249\\ -1249\\ -763\\ -89\\ -763\\ -499\\ -355\\ -65\\ -577\\ -499\\ -355\\ -552\\ -2029\\ -15\\ -2029\\ -155\\ -15\\ -1$	$\substack{111\\894}{1371}\\46824\\1048\\8599\\475\\8859\\475\\8859\\475\\8859\\475\\8859\\475\\8859\\475\\8859\\475\\885\\6637\\108\\886\\86667\\1321\\198\\886\\667\\1321\\198\\1157\\337\\297\\237\\1366\\297\\853\\475\\159\\1169\\699\\885\\855\\455\\557\\159\\1169\\1696\\853\\855\\557\\159\\1169\\169\\653\\855\\855\\557\\159\\1169\\169\\655\\853\\855\\557\\159\\1169\\169\\655\\853\\855\\557\\159\\1169\\169\\169\\169\\169\\169\\169\\169\\169\\1$	$\begin{smallmatrix} 0.32 \\ 0.003 \\ 0.004 \\ 0.004 \\ 0.004 \\ 0.0050 \\ 0.004 \\ 0.0050 \\ 0.004 \\ 0.0050 \\ 0.004 \\ 0.0050 \\ 0.004 \\ 0.0050 \\ 0.004 \\ 0.0050 \\ 0.000$	NR NNRRNNNNNNNNNNNNNNNNNNNNNNNNNNNNNNN

Table A.2: Table of data runs. Each row is a weighted average of repeated runs. Experiment type is specified in Data Type column. Uncertainties are highlighted in gray. Columns 7 and 13 are with respect to the final measured result of  $2\,291\,176\,590\,\text{Hz}$ 

Table A.2 Continued from previous page

run	[ns]	[ns]	[m]	[Gauss]	ool [deg.]	it [Hz]	ν <sub>fit</sub> [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	[Hz] (	$\nu_0 \; [{ m Hz}]$	ts. [%]	ata Type
$\underset{N}{\operatorname{unn}}_{N}$	$\begin{bmatrix} \mathrm{su} \end{bmatrix} L \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	$ \begin{bmatrix} \mathrm{su} \end{bmatrix} \ Q \\ 1050000000000000000000000000000000000$	$ \begin{bmatrix} M \end{bmatrix} a \\ 455525755555555555555555555555555555555$	$\begin{bmatrix} 88n \text{ me} \mathbf{S} \end{bmatrix} = \begin{bmatrix} 222377555577555777555777777777777777777$	log       θ       000000000000000000000000000000000000	[NH]         98505           988505         946900           445141         45584           44522         21057           22555         21958           90046         912210           915221757         21958           90046         912210           915221757         21958           90046         912210           915255         91948           90046         912210           915255         91948           90046         912210           919403         4098711           499841         1499403           409871         219688           4199403         314135           222602         221907           219834         4199403           4193434         410817           219668         411934           410817         222602           21801         222228           40620         411427           410620         411447           410666         4122769           411447         22002           221661         22228           406619         414447           220763 <t< td=""><td><math display="block"> \begin{bmatrix} \mathbf{r}_{H} \end{bmatrix} \overset{\mathbf{t}_{H}}{\mathbf{t}_{J}} \mathbf{v}_{J} \\ \mathbf{x}_{J} \\ \mathbf{x}_{</math></td><td><math display="block">\begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \ ^{\mathbf{R}}_{\mathbf{D}\mathbf{O}\mathbf{O}} \\ = 97659 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 43358 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 2199768 \\ + 21997660 \\ + 2199768 \\ + 21997660 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 219978 \\ + 219</math></td><td><math display="block"> \begin{array}{c} {}_{[\mathbf{H}\mathbf{I}]}^{\mathbf{H}} = &amp; \nabla O \\ &amp; 9.88444444444444222222222222222222222222</math></td><td><math display="block"> \begin{smallmatrix} [\mathbf{s}\mathbf{H}] &amp; \mathbf{OS} \\ \hline 164443223334400\\ 3228334400\\ 322832412940\\ 169112925665880\\ 12950256672388\\ 10022125292565\\ 11336800\\ 1292125292565\\ 11336800\\ 129212529\\ 100713888\\ 400173888\\ 4001873888\\ 4001873888\\ 4001873888\\ 122661830\\ 1873888\\ 4001873888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 100578888888\\ 10057888888\\ 100578</math></td><td>[zH] OSV 4465554466555044091133277552244474202088412682155102763244200637282834492200604221000000000000000000000000000000</td><td><math display="block">\begin{bmatrix} \mathbf{PH} \end{bmatrix} \begin{bmatrix} <b>0</b>_{\mathcal{H}} \\ -198 \\ -102 \\ -2246 \\ -104 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -204 \\ -203 \\ -204 \\</math></td><td><math display="block"> \begin{bmatrix} \mathbf{\bar{z}H} \end{bmatrix}_{04\nabla} \\ 1385738409 \\ 1198784009 \\ 1198784009 \\ 1198784009 \\ 119878400000000000000000000000000000000000</math></td><td><math display="block"> \begin{array}{c} &amp; &amp; \\ &amp; &amp; </math></td><td>Data Туро Data Туро Data Туро</td></t<>	$ \begin{bmatrix} \mathbf{r}_{H} \end{bmatrix} \overset{\mathbf{t}_{H}}{\mathbf{t}_{J}} \mathbf{v}_{J} \\ \mathbf{x}_{J} \\ \mathbf{x}_{$	$\begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \ ^{\mathbf{R}}_{\mathbf{D}\mathbf{O}\mathbf{O}} \\ = 97659 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 433558 \\ + 43358 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 21997660 \\ + 2199768 \\ + 21997660 \\ + 2199768 \\ + 21997660 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 2199768 \\ + 219978 \\ + 219$	$ \begin{array}{c} {}_{[\mathbf{H}\mathbf{I}]}^{\mathbf{H}} = & \nabla O \\ & 9.88444444444444222222222222222222222222$	$ \begin{smallmatrix} [\mathbf{s}\mathbf{H}] & \mathbf{OS} \\ \hline 164443223334400\\ 3228334400\\ 322832412940\\ 169112925665880\\ 12950256672388\\ 10022125292565\\ 11336800\\ 1292125292565\\ 11336800\\ 129212529\\ 100713888\\ 400173888\\ 4001873888\\ 4001873888\\ 4001873888\\ 122661830\\ 1873888\\ 4001873888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 1005788888\\ 100578888888\\ 10057888888\\ 100578$	[zH] OSV 4465554466555044091133277552244474202088412682155102763244200637282834492200604221000000000000000000000000000000	$\begin{bmatrix} \mathbf{PH} \end{bmatrix} \begin{bmatrix} 0_{\mathcal{H}} \\ -198 \\ -102 \\ -2246 \\ -104 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -2246 \\ -1042 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -203 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -204 \\ -203 \\ -204 \\ -203 \\ -204 \\ -204 \\ -203 \\ -204 \\$	$ \begin{bmatrix} \mathbf{\bar{z}H} \end{bmatrix}_{04\nabla} \\ 1385738409 \\ 1198784009 \\ 1198784009 \\ 1198784009 \\ 119878400000000000000000000000000000000000$	$ \begin{array}{c} & & \\ & & $	Data Туро Data Туро Data Туро
$\begin{array}{r} 2378\\ 2378\\ 2340\\ 2412\\ 2442\\ 2442\\ 2442\\ 2446\\ 2446\\ 2448\\ 2446\\ 2448\\ 2450\\ 2512\\ 255\\ 2558\\ 2558\\ 2558\\ 2558\\ 2558\\ 2662\\ 2664\\ 2668\\ $	$\begin{array}{c} 3000\\ 5000\\ 6000\\ 5000\\$	$\begin{array}{c} 350\\ 1500\\ 1500\\ 500\\ 500\\ 1500\\ 500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1255\\ 125$	$\begin{array}{c} & & & & & & \\ & & & & & & \\ & & & & & $	39.7.622 -7.1433 -7.1443 -7.1443 -7.1443 -7.1443 -9.7.623 -9.7.1623 -9.7.1623 -9.7.1623 -9.7.1623 -9.7.1623 -7.622 -7.	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 411097\\ 411487\\ 222452\\ 22002\\ 21754\\ 41041\\ 40757\\ 22903\\ 41041\\ 21947\\ 40763\\ 21947\\ 2293\\ 41045\\ 21935\\ 2293\\ 41112\\ 25737\\ 25445\\ 25745\\ 25745\\ 25745\\ 25745\\ 25745\\ 25745\\ 25241\\ 25242\\ 25052\\ 25456\\ 25243\\ 25244\\ 25265\\ 25244\\ 25265\\ 25244\\ 25265\\ 25244\\ 25265\\ 25244\\ 25265\\ 25243\\ 25265\\ 252810\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25281\\ 25265\\ 25281\\ 25265\\ 25281\\ 25281\\ 25265\\ 25281\\ 25281\\ 25265\\ 25281\\ 25281\\ 25281\\ 25265\\ 25281\\ $	$\begin{smallmatrix} 1/74\\ 2/16\\ 2/$	$\begin{array}{r} -409061\\ -40960\\ -21969\\ -21969\\ -21969\\ -21969\\ -21979\\ -40961\\ -40948\\ -40964\\ -21979\\ -40958\\ -40948\\ -21979\\ -40948\\ -21966\\ -25005\\ -25005\\ -25006\\ -24996\\ -25006\\ -24994\\ -25006\\ -24994\\ -25006\\ -24994\\ -25005\\ -24994\\ -25005\\ -24994\\ -25005\\ -24995\\ -24993\\ -25006\\ -24993\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25005\\ -25006\\ -25006\\ -25005\\ -25006$	$\begin{array}{c} 411\\ 222\\ 241\\ 40.9\\ 412\\ 40.9\\ 40.9\\ 225\\ 255\\ 255\\ 255\\ 255\\ 255\\ 255\\ 25$	$\begin{array}{c} 383\\840\\105\\105\\107\\207\\285\\143\\43\\391\\3443\\391\\3443\\345\\443\\345\\443\\345\\443\\345\\443\\242\\421\\192\\921\\1929\\561\\\end{array}$	$\begin{smallmatrix} 16\\16\\14\\22\\1\\21\\21\\21\\21\\21\\21\\21\\21\\21\\21\\21\\2$	$\begin{array}{c} 1356\\ 4442\\ 190\\ -7\\ -243\\ -294\\ -294\\ -295\\ -155\\ -236\\ -195\\ -190\\ -395\\ -190\\ -395\\ -190\\ -395\\ -190\\ -395\\ -190\\ -366\\ -56\\ 197\\ -56\\ 197\\ -56\\ 197\\ -56\\ 197\\ -56\\ 197\\ -56\\ -56\\ 197\\ -56\\ -56\\ -56\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -35\\ -56\\ -56\\ -35\\ -56\\ -56\\ -56\\ -35\\ -56\\ -56\\ -56\\ -56\\ -56\\ -56\\ -56\\ -5$	$\begin{array}{c} 1797\\ 1797\\ 2175\\ 55526\\ 3008\\ 2502\\ 3008\\ 2502\\ 3008\\ 1008\\ 999\\ 1273\\ 1233\\ 1128\\ 866\\ 896\\ 8133\\ 1123\\ 118\\ 1009\\ 1311\\ 2308\\ \end{array}$	$\begin{array}{c} 0.00\\$	NRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR

Table A.2 Continued from previous page

$\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{i$	run
$\begin{array}{c} \mathbf{S} \\ 6000 \\ 60$	[ns]
$\begin{array}{c} 7 \\ 2000 \\ 1500 $	[ns]
$\begin{array}{c} 7\\ 15\\ 15\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 22.5\\ 74.25\\ 75.5\\ 75.5\\ 74.25\\ 74.25\\ 75.5\\ 74.25\\ $	[w]
$\begin{array}{c} 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ 7\\ $	[Gauss]
$\begin{array}{c} g\\ 2600\\ 2660\\ 26$	ool [deg.]
$\begin{array}{c} 2\\ 25213\\ 255062\\ 255079\\ 26187\\ 25062\\ 255307\\ 25079\\ 26187\\ 261$	at [Hz]
$\begin{smallmatrix} 7 \\ 240 \\ 357 \\ 357 \\ 357 \\ 357 \\ 357 \\ 357 \\ 357 \\ 357 \\ 357 \\ 359 \\ 269 \\ 299 \\ 206 \\ 299 \\ 206 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 \\ 299 \\ 456 $	ν <sub>fit</sub> [Hz]
$\begin{array}{c} \mathbf{I} \\ \hline \mathbf{I} \hline \mathbf{I} \\ \hline \mathbf{I} \hline \mathbf{I} \\ \hline $	C <sub>B</sub> [Hz]
$\begin{smallmatrix} 7 \\ 225 $	DC <sub>B</sub> [Hz]
$\begin{smallmatrix} 0_1 \\ 151 \\ 150 \\ 471 \\ 645 \\ 803 \\ 802 \\ 803 \\ 802 \\ 805 \\ 5563 \\ 484 \\ 805 \\ 488 \\ 804 \\ 481 \\ 805 \\ 488 \\ 804 \\ 481 \\ 805 \\ 480 \\ 804 \\ 481 \\ 805 \\ 480 \\ 804 \\ 481 \\ 805 \\ 480 \\ 480 \\ 481 \\ 805 \\ 480 \\ 480 \\ 481 \\ 480 \\ 4$	C [Hz]
$\begin{smallmatrix} 7 \\ 31 \\ 317 \\ 821 \\$	SC [Hz]
$\begin{array}{c} 3\\ 53\\ -82\\ -82\\ -82\\ -82\\ -82\\ -82\\ -82\\ -82$	[Hz] (
$\begin{smallmatrix} 7 \\ 243 \\ 359 \\ 359 \\ 359 \\ 2369 \\ 282 \\ 282 \\ 282 \\ 282 \\ 282 \\ 287 \\ 319 \\ 1335 \\ 464 \\ 347 \\ 345 \\ 326 \\ 339 \\ 441 \\ 439 \\ 119 \\ 132 \\ 258 \\ 164 \\ 119 \\ 226 \\ 111 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 121 \\ 110 \\ 449 \\ 512 \\ 313 \\ 402 \\ 121 \\ 101 \\ 449 \\ 512 \\ 313 \\ 402 \\ 121 \\ 101 \\ 449 \\ 512 \\ 2510 \\ 127 \\ 1$	ν0 [Hz]
$\begin{array}{c} & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & $	ts. [%]
I NRERRERERERERERERERERERERERERERERERERER	ata Type

Table A.2 Continued from previous page

Vrun	[ [ns]	[su] O	[M]	3 [Gauss]	) <sub>pol</sub> [deg.]	'fit [Hz]	$\Delta \nu_{\rm fit}  [{ m Hz}]$	OC <sub>B</sub> [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	ASC [Hz]	<sup>0</sup> [Hz]	Δν <sub>0</sub> [Hz]	vts. [%]	)ata Type
$\begin{array}{c} 3771\\ 33774\\ 33774\\ 33774\\ 33774\\ 33776\\ 33774\\ 33776\\ 33778\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33776\\ 33778\\ 33778\\ 3378\\ 3396\\ 3398\\ 33990\\ 33993\\ 33996\\ 33996\\ 33996\\ 33996\\ 33996\\ 33996\\ 33996\\ 33996\\ 3398\\ 33996\\ $	$\begin{array}{c} 450\\ 450\\ 800\\ 800\\ 800\\ 800\\ 800\\ 800\\ 800\\ 8$	$\begin{array}{c} 150\\ 150\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\$	$\substack{\begin{array}{c}30\\30\\74,25\\74,2$	$\begin{array}{c} 3.1757\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1752\\ 3.1755\\ 5.244\\ 4.76222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.762222\\ 4.7622222\\ 4.7622222\\ 4.76222222\\ 4.76222222\\ 4.762222$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 4573\\ 4478\\ 9984\\ 4478\\ 99862\\ 910345\\ 96937\\ 99379\\ 99036\\ 96033\\ 99006\\ 39008\\ 3908\\ 39008\\$	$\begin{array}{c} 1702\\ 1223\\ 2296\\ 4038\\ 3379\\ 2296\\$	$\begin{array}{r} -4362\\ -4362\\ -9759\\ -9759\\ -9760\\ -9759\\ -9760\\ -9759\\ -9769\\ -97769\\ -97769\\ -97769\\ -97769\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9770\\ -9769\\ -38986\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4356\\ -4355\\ -4366\\ -4355\\ -4356\\ -4366\\ -4355\\ -4366\\ -4355\\ -4366\\ -4366\\ -4355\\ -4366\\ -4366\\ -4355\\ -4366\\ -436\\ -4366\\ -4366\\ -436\\ -4$	$\begin{array}{c} 4.4\\ 4.48\\ 9.98\\ 8.89\\ 9.98\\ 8.89\\ 9.98\\ 9.99\\ $	$\begin{array}{c} 399\\ 2412\\ 2122\\ 2133\\ $	$\begin{array}{c} 775555555555555555555555627711603644963739033373679639360023385525212443240662551337888111720684022777767222448822920222944822920222944832292022944832920229448329202294483292920229448329292022944832929202294483292920222944832929202294489292022944892920229448929202299448929202299448929202294489292022944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944892920229944929202299448929202299449292022994492920229944892920229944892920229944892920229944892920229944892920229944929202299449292022994489292022994489292022994489292022994489292022994489292022994489292022994489292022994489292022994489292022994492920229944929202299449292022994492929292$	$\begin{array}{c} -29\\ -124\\ 373\\ -2753\\ -766\\ 280\\ -346\\ -188\\ -99\\ -127\\ -366\\ -280\\ -380\\ -366\\ -188\\ -99\\ -266\\ -199\\ -266\\ -199\\ -266\\ -199\\ -275\\ -135\\ -366\\ -280\\ -380\\ -380\\ -438\\ -312\\ -438\\ -312\\ -438\\ -312\\ -438\\ -312\\ -251\\ -344\\ -312\\ -251\\ -387\\ -344\\ -312\\ -251\\ -387\\ -344\\ -312\\ -288\\ -388\\ -388\\ -388\\ -223\\ -223\\ -268\\ -288\\ -55\\ -80\\ -288\\ -55\\ -80\\ -288\\ -288\\ -56\\ -288\\ -2$	$\begin{array}{c} 1253\\ 2229\\ 4038\\ 33782\\ 6266\\ 2222\\ 2222\\ 2066\\ 1111\\ 1156\\ 002\\ 0083\\ 33782\\ 6266\\ 1111\\ 1256\\ 002\\ 2222\\ 206\\ 1111\\ 1256\\ 002\\ 206\\ 111\\ 1256\\ 002\\ 206\\ 111\\ 1276\\ 112\\ 276\\ 112\\ 276\\ 112\\ 276\\ 112\\ 276\\ 112\\ 276\\ 112\\ 276\\ 112\\ 276\\ 122\\ 276\\ 112\\ 276\\ 122\\ 276\\ 112\\ 276\\ 122\\ 122\\ 276\\ 122\\ 122\\ 122\\ 122\\ 122\\ 122\\ 122\\ 12$	$\begin{array}{c} 0.00\\ 0.00\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.00\\$	ŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔŔ

Table A.2 Continued from previous page
$N_{ m run}$	$T \; [ns]$	D [ns]	P [W]	B [Gauss]	$\theta_{\rm pol}~[{\rm deg.}]$	$ u_{\rm fit}  [{\rm Hz}] $	$\Delta \nu_{\rm fit} \; [{ m Hz}]$	DC <sub>B</sub> [Hz]	$\Delta DC_{B}$ [Hz]	SC [Hz]	$\Delta SC [Hz]$	$ u_0  [\mathrm{Hz}] $	$\Delta \nu_0 \; [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{l} 468\\ 4701\\ 4723\\ 4774\\ 4775\\ 4774\\ 4784\\ 4883\\ 4884\\ 4884\\ 4884\\ 4885\\ 4884\\ 4885\\ 55001\\ 25003\\ 4499\\ 55012\\ 5503\\ 5555\\ 555$	$\begin{array}{r} 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300$	$\begin{array}{l} 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 1000\\ 2000\\$		$\begin{array}{r} -4.762\\ -5.24\\ -9.524\\ -4.762\\ $	$\begin{array}{c} 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\$	$\begin{array}{l} 10168\\ 10078\\ 10025\\ 10078\\ 10023\\ 100113\\ 10023\\ 100113\\ 10010\\ 9982\\ 10025\\ 100005\\ 100005\\ 100005$	$\begin{array}{c} 771\\ 1703\\ 679\\ 790\\ 901\\ 762\\ 1483\\ 919\\ 900\\ 543\\ 889\\ 900\\ 543\\ 813\\ 133\\ 1591\\ 2659\\ 2723\\ 3811\\ 1591\\ 2659\\ 2723\\ 3811\\ 2595\\ 4272\\ 3811\\ 2595\\ 4272\\ 3811\\ 2595\\ 4272\\ 3811\\ 2595\\ 4272\\ 3883\\ 2751\\ 2327\\ 8889\\ 2751\\ 2327\\ 8889\\ 2751\\ 2327\\ 8889\\ 2751\\ 2325\\ 4967\\ 1712\\ 1712\\ $	$\begin{array}{c} -9759\\ -9771\\ -9775\\ -9775\\ -9775\\ -9775\\ -9775\\ -9770\\ -9775\\ -9770\\ -9776\\ -9770\\ -9776\\ -9776\\ -9769\\ -9769\\ -9769\\ -9769\\ -9769\\ -9769\\ -9776\\ -9776\\ -9776\\ -9776\\ -9776\\ -9776\\ -9776\\ -9769\\ -98966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -9757\\ -9759\\ -975$	88888888888888888888888888888888888888	$\begin{array}{c} 410\\ 3 \\ 443\\ 496\\ 8\\ 202\\ 149\\ 8\\ 253\\ 2\\ 514\\ 6\\ 49\\ 8\\ 95\\ 22\\ 514\\ 6\\ 49\\ 9\\ 8\\ 9\\ 22\\ 514\\ 6\\ 49\\ 9\\ 104\\ 1\\ 104\\ 9\\ 49\\ 9\\ 104\\ 1\\ 105\\ 104\\ 9\\ 104\\ 105\\ 105\\ 104\\ 105\\ 104\\ 105\\ 105\\ 105\\ 105\\ 105\\ 105\\ 105\\ 105$	$\begin{array}{c} 10 \\ 9 \\ 11 \\ 12 \\ 9 \\ 511 \\ 47 \\ 15 \\ 40 \\ 66 \\ 62 \\ 22 \\ 22 \\ 233 \\ 10 \\ 333 \\ 39 \\ 91 \\ 111 \\ 14 \\ 41 \\ 111 \\ 111 \\ 15 \\ 52 \\ 22 \\ 25 \\ 55 \\ 81 \\ 84 \\ 48 \\ 8 \\ 8 \\ \end{array}$	$\begin{array}{c} -19\\ 129\\ 129\\ 128\\ -10\\ 129\\ -223\\ -19\\ -37\\ -37\\ -38\\ -193\\ -37\\ -38\\ -193\\ -37\\ -38\\ -193\\ -37\\ -38\\ -188\\ -188\\ -188\\ -188\\ -188\\ -188\\ -275\\ -338\\ -188\\ -188\\ -275\\ -338\\ -188\\ -275\\ -388\\ -188\\ -275\\ -388\\ -188\\ -275\\ -388\\ -102\\ -275\\ -264\\ -298\\ -275\\ -275\\ -264\\ -298\\ -275\\ -264\\ -298\\ -275\\ -264\\ -298\\ -275\\ -264\\ -298\\ -264\\ -298\\ -264\\ -275\\ -282\\ -298\\ -1600\\ -816\\ -225\\ -2995\\ -295\\ -295\\ -295\\ -295\\ -295\\ -295\\ -295\\ $	$\begin{array}{c} 792\\ 792\\ 1711\\ 6791\\ 902\\ 777\\ 8149\\ 992\\ 11480\\ 832\\ 991\\ 1480\\ 832\\ 2659\\ 2723\\ 327232\\ 32723\\ 32723\\ 32723\\ 32723\\ 32723\\ 327232\\ 32723\\ 32723\\ 3$	$\begin{array}{c} 0.02\\ 0.10\\ 0.10\\ 0.10\\ 0.10\\ 0.10\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.21\\ 0.21\\ 0.21\\ 0.21\\ 0.21\\ 0.21\\ 0.21\\ 0.21\\ 0.20\\ 0.22\\ 0.00\\$	NRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR

Table A.2 Continued from previous page

un	[us]	[ns]	[m]	[Gauss]	ool [deg.]	it [Hz]	$ u_{\mathrm{fit}}  [\mathrm{Hz}] $	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	[Hz]	SC [Hz]	[Hz]	ν <sub>0</sub> [Hz]	ts. [%]	ata Type
$\substack{\textbf{111}\\ \textbf{2}\\ \textbf{566}\\ 5667\\ 5689\\ 5770\\ 5723\\ 5773\\ 5778\\ 5778\\ 5778\\ 5779\\ 5801\\ 5823\\ 5845\\ 5883\\ 5885\\ 5885\\ 5885\\ 5885\\ 5885\\ 5885\\ 5985\\ 5983\\ 5992\\ 5933\\ 5985\\ 5985\\ 5985\\ 5985\\ 5985\\ 5996\\ 6001\\ 6003\\ 6005\\ 6003\\ 6005\\ 6008\\ 6008$	$\begin{bmatrix} \text{st} \\ 5000$	$ \begin{bmatrix} \mathrm{su} \\ \mathrm{su} \end{bmatrix} Q \\ \begin{array}{c} 550 \\ 1000 \\ 1$	$ \begin{bmatrix} M \end{bmatrix}_{\mathbf{d}'} \begin{bmatrix} 600 & 67.5 \\ 660 & 67.5 \\ 774.25 & 774.25 \\ 774.25 & 774.25 \\ 522.5 & 552.5 \\ 522.5 & 567.5 \\ 300 & 222.5 \\ 522.5 & 552.5 \\ 300 & 222.5 \\ 522.5 & 300 \\ 74.25 & 300 \\ 74.25 & 52.5 \\ 774.25 & 600 \\ 74.25 & 52.5 \\ 774.25 & 52.5 \\ 774.25 & 600 \\ 774.25 & 52.5 \\ 774.25$	$ \begin{bmatrix} g \\ g \\ -g \\ -g \\ -g \\ -g \\ -g \\ -g \\$	$\left  \begin{array}{c} \left  \theta^{\rm bol} \right  \\ \left $	$\begin{bmatrix} \mathbf{\bar{z}} \\ $	$ \begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \ ^{19} \mathbf{A} \nabla \\ \begin{array}{c} 4785 \\ 3021 \\ 22750 \\ 6067 \\ 6662 \\ 3343 \\ 005 \\ 66662 \\ 3343 \\ 005 \\ 66662 \\ 3343 \\ 005 \\ 66662 \\ 3343 \\ 005 \\ 6662 \\ 3343 \\ 005 \\ 6662 \\ 3343 \\ 005 \\ 0$	$\begin{array}{c} P_{G} P_{G}$	DDCB (Hz) 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0	$ \begin{smallmatrix} \mathbf{\bar{r}} \mathbf{H} \\ \mathbf{U} \mathbf{S} \\ \mathbf{S} $	[FH] OSV 166778865555511112244777333222244444882221188777121165	$ \begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \overset{0}{\mathbf{z}} \\ \overset{-649}{\mathbf{z}} \\ \overset{-381}{\mathbf{z}} \\ \overset{-312}{\mathbf{z}} \\ \overset{-312}{\mathbf{z}} \\ \overset{-312}{\mathbf{z}} \\ \overset{-312}{\mathbf{z}} \\ \overset{-341}{\mathbf{z}} \\ \overset{-344}{\mathbf{z}} \\ \overset{-344}{\mathbf{z}} \\ \overset{-346}{\mathbf{z}} \\ \overset{-3265}{\mathbf{z}} \\ \overset{-3263}{\mathbf{z}} \\ \overset{-326}{\mathbf{z}} \\ \overset{-326}{\mathbf$	$ \begin{bmatrix} z_{H} \end{bmatrix} \begin{smallmatrix} 0_{A} \nabla \\ 4808 \\ 3022 \\ 2750 \\ 6068 \\ 7457 \\ 5760 \\ 0273 \\ 33450 \\ 75760 \\ 018 \\ 6078 \\ 33450 \\ 1866 \\ 4932 \\ 2482 \\ 4823 \\ 3684 \\ 4823 \\ 3684 \\ 4823 \\ 3684 \\ 3880 \\ 1866 \\ 186$	[%]           .stm           0.000           0.002           0.002           0.000           0.002           0.002           0.001           0.002           0.002           0.002           0.001           0.001           0.001           0.002           0.002           0.002           0.002           0.002           0.002           0.002           0.002           0.003           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.000           0.001           0.002           0.002	Data Type ИМИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИИ
$\begin{array}{c} 608\\ 609\\ 610\\ 611\\ 611\\ 612\\ 616\\ 615\\ 616\\ 615\\ 616\\ 620\\ 622\\ 622\\ 622\\ 622\\ 622\\ 622\\ 62$	$\begin{array}{c} 500\\ 500\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300\\$	$\begin{array}{c} 1000\\ 1000\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 1500\\ 500\\ $	$\begin{array}{c} 52.5\\ 60\\ 15\\ 22.5\\ 52.5\\ 3.75\\ 52.5\\ 3.75\\ 4.5\\ 4.5\\ 4.5\\ 4.5\\ 3.75\\ 4.5\\ 3.75\\ 4.5\\ 3.75\\ 4.25\\ 22.5\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 3.75\\ 52.5\\ 3.7.5\\ 52.5\\ 3.7.5\\ 52.5\\ 3.7.5\\ 52.5\\ 3.7.5\\ 52.5\\ 3.7.5\\ 52.5\\ 52.5\\ 3.7.5\\ 52.$	$\begin{array}{c} 1,762\\ 4,762\\ 4,762\\ -4,762\\ -3,175\\ -3,175\\ 3,175\\ 3,175\\ 3,175\\ -3,17$	$\begin{array}{c} 170\\ 170\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 26$	$\begin{array}{l} 1025.4\\ 1025.4\\ 9851\\ 9851\\ 4364\\ 4578\\ 5207\\ 4378\\ 45207\\ 4378\\ 45207\\ 4512\\$	$\begin{array}{c} 382\\ 382\\ 667\\ 125\\ 98\\ 147\\ 76\\ 72\\ 16\\ 76\\ 94\\ 676\\ 72\\ 76\\ 76\\ 76\\ 76\\ 76\\ 76\\ 76\\ 76\\ 76\\ 76$	$\begin{array}{r} -9767\\ -97767\\ -97766\\ -97766\\ -43524\\ -4354\\ -4354\\ -4354\\ -4356\\ -4356\\ -43559\\ -43559\\ -43559\\ -43559\\ -43559\\ -43554\\ -4355\\ -35976\\ -389979\\ -389976\\ -389978$	$\begin{array}{c} 9.8\\ 8.8\\ 8.4\\ 4.4\\ 4.4\\ 4.4\\ 4.4\\ 4.4\\ 4$	$\begin{array}{c} 224\\ 224\\ 516\\ 224\\ 516\\ 224\\ 516\\ 224\\ 516\\ 224\\ 516\\ 224\\ 516\\ 226\\ 226\\ 226\\ 226\\ 226\\ 226\\ 226\\ 2$	$\begin{smallmatrix}5&1\\80\\9&29\\9&69\\4&39\\9&59\\9&59\\14\\0&334\\499\\824\\4&24\\1005\\149\\235\\139\\6\\327\\1395\\331\\6\\357\\335\\24\\6\\24\\124\\132\\15\\5\\22\\22\\15\\5\\22\\22\\15\\5\\22\\22\\15\\5\\22\\22\\22\\15\\5\\22\\22\\22\\22\\22\\22\\22\\22\\22\\22\\22\\22\\$	$\begin{array}{c} 263\\ 263\\ 194\\ -162\\ -38\\ -226\\ 0\\ 137\\ 139\\ -316\\ -5$	$\begin{array}{c} 3825\\$	$\begin{array}{c} 0.02\\ 0.01\\ 0.00\\$	NR NP NN PP NP PR RR

Table A.2 Continued from previous page

$\sum_{i=1}^{n} \frac{664}{6656} + \frac{667}{6679} + \frac{667}{6699} + \frac{667}{6699} + \frac{667}{6699} + \frac{667}{7007} + \frac{667}{$	<i>r</i> un
$ \begin{array}{c} 5\\ 5000\\ 5$	[ns]
$\begin{array}{c} r \\ 100 \\ 1$	[ns]
$\begin{array}{c} 7\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 75.5\\ 300\\ 600\\ 30\\ 37.5\\ 74.25\\ 52.5\\ 74.25\\ 7$	[M]
$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	3 [Gauss]
$\begin{smallmatrix} G \\ 2600 \\ 260 \\ 2600 \\$	pol [deg.]
$\begin{array}{c} 2\\ 9846\\ 99948\\ 9997\\ 38703\\ 38703\\ 38703\\ 38705\\ 9948\\ 9963\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10058\\ 10049\\ 10037\\ 100380\\ 10056\\ 38991\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38991\\ 38955\\ 38951\\ 38955\\ 38951\\ 38954\\ 10048\\ 100262\\ 4576\\ $	fit [Hz]
7 133 151 148 242 2294 300 163 1993 1994 267 253 211 178 1896 267 253 211 178 1896 267 253 211 178 1896 1657 187 1990 1667 187 200 1888 2765 201 1785 1890 1657 187 200 1888 2765 201 1888 2765 2045 187 200 1888 2705 187 200 1888 2705 200 201 1785 200 1888 200 1888 200 1888 200 201 1785 200 1888 200 201 1785 200 1888 200 201 1785 200 1888 200 201 1785 200 1888 200 201 200 200 200 200 200 200 200 200	νν <sub>fit</sub> [Hz]
1 -9762 -9762 -9763 -9763 -9763 -9763 -9763 -9763 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9763 -9762 -9762 -9764 -9766 -9766 -9762 -9762 -9762 -9764 -9766 -9762 -9763 -9762 -9763 -9762 -9763 -9763 -9763 -9763 -9763 -9763 -9764 -9762 -9764 -9762 -9763 -9762 -9763 -9763 -9763 -9762 -9764 -9762 -9764 -9762 -9763 -9762 -9763 -9762 -9762 -9763 -9762 -9764 -9762 -9763 -9762 -9763 -9762 -9762 -9763 -97762 -9763 -9762 -9764 -9766	DC <sub>B</sub> [Hz]
$7 \\ 9.88889999888888888888888888888888888$	DC <sub>B</sub> [Hz]
$\begin{array}{c} 5\\ 92\\ 331\\ 333\\ 333\\ 927\\ 7125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 125\\ 127\\ 7198\\ 127\\ 7198\\ 127\\ 7198\\ 127\\ 7198\\ 127\\ 7198\\ 128\\ 127\\ 7198\\ 128\\ 127\\ 7198\\ 128\\ 127\\ 7198\\ 128\\ \mathbf$	C [Hz]
$7 \\ 288688111333666645556611155886663322555111811444772177106655546222648841122366300296769766888321101983445451133134526122641266666666666666666666666666666$	SC [Hz]
$\begin{array}{c} -& -& -& -& -& -& -& -& -& -& -& -& -& $	0 [Hz]
7 133 152 149 141 152 143 152 143 152 143 152 143 152 143 152 145 152 143 152 145 152 152 152 152 152 152 152 152 152 15	240 [Hz]
$\begin{array}{c} \mathbf{P} \\ 0 \\ $	rts. [%]
1 NRRBRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR	)ata Type

	Table A.2	Continued	from	previous	page
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un1 <sub>A7</sub> 623 663 665 667	T [ns] T [ns]	[su] <u>Q</u> 100 100 100 100	$\begin{bmatrix} M \\ 52.5 \\ 67.5 \\ 7.5 \\ 45 \\ 74.25 \\ 74.25 \end{bmatrix}$	[ssneg] g -4.762 -4.762 -4.762 -4.762 -4.762 -4.762	$\begin{bmatrix} -1000 \\ -1$	[¤H] 10009 10281 10886 10200 9743	$\begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \stackrel{\text{ty}}{\overset{\text{ty}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}{\overset{\text{T}}}}{\overset{\text{T}}}{\overset{\text{T}}}}{\overset{\text{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}}{\overset{T}}{\overset{T}}}{}$	DC <sup>B</sup> [H <sup>z</sup> ] 9761-9761- 9760-9760 97600-9760	secence secence SDCB [Hz]	[ <b>z</b> H] OS 185245 211 1562 2122	ZSC [Hz] OSV	[zH] 07 63 275 1104 -289	[zH] 0 <sup>∧</sup> ∇ 276 233 488 291 1892	[%]	ZZZZZZ JZZZZZZ JZZZZZZ JZZZZZZ Data Type
$68 \\ 669 \\ 771 \\ 772 \\ 774 \\ 775 \\ 777 \\ 779 \\ 801 \\ 823 \\ 845 \\ 886 \\ 889 \\ 901 \\ 889 \\ 901 \\ 880 \\ 889 \\ 901 \\ 880 \\$	$\begin{array}{c} 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600$	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{smallmatrix} 15\\ 15\\ 37.5\\ 22.5\\ 7.5\\ 60\\ 37.25\\ 74.25\\ 74.25\\ 15\\ 67.5\\ 67.5\\ 52.5\\ 22.5\\ 22.5\\ 22.5\\ 37$	$\begin{array}{r} 4.762\\ 4.762\\ 4.762\\ 4.762\\ -4.762\\ -4.762\\ -4.762\\ -4.762\\ -4.762\\ -9.524\\ -9.$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 10398\\ 10066\\ 10133\\ 9560\\ 9739\\ 10390\\ 9843\\ 10601\\ 10326\\ 39111\\ 39189\\ 39085\\ 39090\\ 399085\\ 399085\\ 399085\\ 399085\\ 389066\\ 38938\\ 388866\\ 388886\\ 3888918\\ 38918\\ 389170\\ 391770\\ \end{array}$	$\begin{array}{r} 464\\ 237\\ 229\\ 454\\ 219\\ 435\\ 312\\ 355\\ 243\\ 355\\ 243\\ 109\\ 1202\\ 120\\ 120\\ 120\\ 147\\ 103\\ 91\\ 458\\ 97\\ 136\\ 204\\ 187\\ 130\end{array}$	$\begin{array}{r} -9770\\ -9771\\ -9759\\ -9771\\ -9759\\ -9771\\ -9771\\ -9778\\ -9772\\ -9759\\ -9771\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38966\\ -38996\\ -3$	9.8 9.8 9.8 9.8 9.8 9.8 9.8 9.8 9.8 3.9	$\begin{array}{r} 47\\ 212\\ 46\\ 127\\ 20\\ 209\\ 1266\\ 268\\ 16\\ 81\\ 164\\ 92\\ 92\\ 66\\ 88\\ 26\\ 25\\ 36\\ 46\\ 46\end{array}$	$     \begin{array}{c}       1 \\       5 \\       1 \\       3 \\       2 \\       0 \\       5 \\       3 \\       6 \\       6 \\       3 \\       2 \\       9 \\       18 \\       1 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       1 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       1 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       1 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       1 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       13 \\       5 \\       5 \\       7 \\       9 \\       18 \\       13 \\       5 \\       5 \\       7 \\       9 \\       10 \\      $	$\begin{array}{c} 582\\ 833\\ -284\\ -284\\ -575\\ 287\\ 128\\ -575\\ 287\\ 140\\ 89\\ -122\\ -129\\ -126\\ -127\\ -129\\ -136\\ -260\\ -115\\ -260\\ -115\\ -260\\ -115\\ -260\\ -1128\\ -260\\ -260\\ -1128\\ -260\\$	$\begin{array}{r} 465\\ 237\\ 229\\ 454\\ 219\\ 435\\ 312\\ 283\\ 117\\ 206\\ 128\\ 100\\ 105\\ 142\\ 208\\ 191\\ 136\\ 191\\ 136\end{array}$	$\begin{array}{c} 0.02\\ 0.04\\ 0.08\\ 0.02\\ 0.09\\ 0.03\\ 0.03\\ 0.03\\ 0.03\\ 0.00\\$	NRRRRRRRRRRRRRRRRRRRR NNNNNNNNNNNNNNNN
91 92345 999901 00000000000000000000000000000000000	$\begin{array}{c} 500\\ 5500\\ $	$\begin{array}{c} 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ 100\\ 100\\ 100\\ $	$\begin{smallmatrix}&45\\52.5\\455\\60\\3,0\\7.5\\22.5\\52.5\\52.5\\52.5\\7.5\\22.5\\7.5\\3,0\\3,0\\3,0\\3,0\\5\\22.5\\3,0\\5\\22.5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\3,0\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5$	$\begin{array}{r} 9.524\\ 9.524\\ 9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -4.762\\ 4.762\\ -4.$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 38945\\ 38971\\ 39187\\ 39187\\ 39106\\ 39175\\ 38374\\ 10016\\ 9841\\ 9725\\ 9877\\ 10029\\ 99840\\ 9944\\ 10128\\ 10001\\ 9905\\ 10013\\ 9801\\ 10005\\ 9864\\ 10091 \end{array}$	$149\\103\\66\\1113\\200\\95\\128\\95\\128\\92\\145\\92\\145\\92\\145\\92\\133\\238\\68\\127\\133\\238\\98\\98\\98\\98\\98\\98\\98\\98\\98\\98\\98\\98\\98$	-38996 -38998 -389967 -38967 -38967 -38968 -9773 -9773 -9775 -9775 -9775 -97773 -97754 -97773 -97757 -97756 -97773 -9773	39 399 399 339 399 399 399 9.88	$\begin{array}{c} 578\\ 688\\ 1033\\ 580\\ 366\\ 2804\\ 853\\ 2134\\ 244\\ 1155\\ 1147\\ 1804\\ 8534\\ 1469\\ 179\\ 281\end{array}$	$11\\20\\11\\6\\7\\1\\7\\21\\5\\5\\1\\3\\3\\4\\4\\2\\1\\1\\4\\4\\7$	$\begin{array}{c} -108\\ -95\\ 84\\ -119\\ 25\\ 171\\ -632\\ -22\\ -16\\ -101\\ -92\\ -41\\ 192\\ 208\\ 49\\ -235\\ 205\\ 205\\ 205\\ 21\\ 103\\ -71\\ 103\\ -71\\ 37\end{array}$	$155 \\ 111 \\ 79 \\ 112 \\ 204 \\ 389 \\ 96 \\ 83 \\ 129 \\ 80 \\ 71 \\ 103 \\ 92 \\ 84 \\ 69 \\ 127 \\ 133 \\ 238 \\ 92 \\ 92 \\ 98 \\ 70 \\ 100 $	$\begin{array}{c} 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.27\\ 0.40\\ 0.23\\ 0.35\\ 0.44\\ 0.64\\ 0.26\\ 0.25\\ 0.040\\ 0.37\\ 0.37\\ \end{array}$	NRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR
545678901234567890123455	$\begin{array}{c} 600\\ 600\\ 700\\ 700\\ 700\\ 600\\ 700\\ 600\\ 700\\ 600\\ 700\\ 600\\ 450\\ 450\\ 450\\ 450\\ 450\\ 450\\ 450\\ 600\\ 450\\ 450\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 6$	$\begin{array}{c} 100\\ 200\\ 200\\ 100\\ 100\\ 200\\ 100\\ 200\\ 100\\ 200\\ 100\\ 200\\ 150\\ 150\\ 150\\ 150\\ 150\\ 150\\ 150\\ 1$	$\begin{array}{c} 18.75\\ 3.75\\ 67.5\\ 37.5\\ 18.75\\ 18.75\\ 11.25\\ 67.5\\ 11.25\\ 37.5\\ 11.25\\ 37.5\\ 11.25\\ 1$	$\begin{array}{c} -7.143\\ -7.143\\ -4.762\\ 4.762\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -7.143\\ -3.175\\ -3.175\\ -3.175\\ -3.175\\ -9.524\\ 3.175\\ -9.524\\ 3.175\\ -9.524\\ -3.175\end{array}$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 22104\\ 20317\\ 10092\\ 10293\\ 9884\\ 22104\\ 10647\\ 21765\\ 21765\\ 22877\\ 22877\\ 10057\\ 22140\\ 38876\\ 4543\\ 389028\\ 4433\\ 389028\\ 4433\\ 389028\\ 4433\\ 389028\\ 4433\\ 389028\\ 38790\\ 3946\\ 3946\end{array}$	$\begin{array}{c} 252\\ 1020\\ 230\\ 406\\ 1234\\ 261\\ 355\\ 254\\ 879\\ 496\\ 140\\ 140\\ 202\\ 1310\\ 395\\ 202\\ 395\\ 206\\ 395\\ 393\\ 393\\ 3223 \end{array}$	$\begin{array}{c} -21967\\ -21969\\ -9760\\ -9772\\ -9772\\ -21984\\ -9760\\ -21968\\ -9772\\ -21982\\ -9760\\ -21982\\ -9760\\ -21985\\ -38969\\ -4355\\ -4353\\ -38969\\ -4356\\ -4363\\ -38992\\ -4363\\ -38964\\ -4363\\ -38956\\ -4356\\ -4356\end{array}$	$\begin{array}{c} 22\\ 22\\ 22\\ 9.8\\ 9.8\\ 9.8\\ 22\\ 9.8\\ 22\\ 9.8\\ 22\\ 9.8\\ 22\\ 9.8\\ 22\\ 39\\ 4.4\\ 4.4\\ 4.4\\ 4.4\\ 39\\ 30\\ 4.4\\ 4.4\\ 34\\ 34\\ 4.4\\ 34\\ 34\\ 4.4\\ 34\\ 34\\ 4.4\\ 34\\ 34\\ 34\\ 34\\ 4.4\\ 34\\ 34\\ 34\\ 34\\ 34\\ 34\\ 34\\ 34\\ 34\\ 3$	$\begin{array}{c} 184\\ 309\\ 209\\ 234\\ 186\\ 235\\ 106\\ 209\\ 109\\ 100\\ 100\\ 100\\ 142\\ 81\\ 142\\ 68\\ 49\\ 142\\ 68\\ 49\\ 142\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 5$	37 65 36 38 6225 21 3228 169 109 3311 109 311 6	$\begin{array}{c} -47\\ -1682\\ 123\\ 412\\ -121\\ -66\\ 652\\ -309\\ -195\\ 791\\ 188\\ 49\\ -133\\ 45\\ -72\\ 145\\ -726\\ -14\\ 49\\ -133\\ 45\\ -726\\ -14\\ 404\\ -325\\ -235\\ -235\\ -462\end{array}$	$\begin{array}{c} 256\\ 1020\\ 231\\ 407\\ 1238\\ 262\\ 357\\ 254\\ 496\\ 438\\ 343\\ 141\\ 202\\ 132\\ 397\\ 202\\ 132\\ 397\\ 206\\ 395\\ 395\\ 224 \end{array}$	$\begin{array}{c} 0.00\\ 0.00\\ 0.05\\ 0.02\\ 0.07\\ 0.00\\ 0.03\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.00\\ 0.12\\ 0.08\\ 0.00\\ 0.00\\ 0.11\\ 0.06\\ 0.00\\ 0.13\\ \end{array}$	RRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR
678901234567890123456789	$\begin{array}{c} 600\\ 600\\ 450\\ 450\\ 450\\ 450\\ 450\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 700\\ 7$	$\begin{array}{c} 50\\ 50\\ 50\\ 150\\ 150\\ 150\\ 150\\ 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ 100\\ 10$	$\begin{array}{c} 52.5\\ 1.5\\ 45.5\\ 26.25\\ 26.25\\ 26.25\\ 26.25\\ 26.25\\ 3.75\\ 67.5\\ 37.5\\ 37.5\\ 26.25\\ 74.$	$\begin{array}{c} 9.524\\ -9.524\\ -9.524\\ -9.524\\ 3.175\\ -3.175\\ -3.175\\ -3.524\\ -9.524\\ 9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -9.524\\ -4.762\\ -4.762\\ -9.524\\ -7.143\\ -7.143\\ -7.143\\ -7.162\\ -9.524\\ -7.143\\ -7.143\\ -7.762\\ -9.524\\ -7.143\\ -7.762\\ -9.524\\ -7.143\\ -7.762\\ -9.524\\ -7.143\\ -7.762\\ -9.524\\ -7.762\\ -7$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 88920\\ 39962\\ 39962\\ 458697\\ 458697\\ 4603\\ 4575\\ 4603\\ 38405\\ 38405\\ 39241\\ 388405\\ 39241\\ 39242\\ 38564\\ 39222\\ 3877\\ 10115\\ 10407\\ 10125\\ 10125\\ 10125\\ 39511\\ 39511\\ 39512\\ 38972\\ 10053\\ 38972\\ 10064\\ \end{array}$	$\begin{array}{r} \hline 299\\ \hline 798\\ 322\\ 204\\ 102\\ 123\\ 378\\ 329\\ 730\\ 218\\ 325\\ 470\\ 231\\ 106\\ 206\\ 102\\ 106\\ 102\\ 106\\ 102\\ 105\\ 1130\\ 115\\ 251\\ 430\\ 160\\ \end{array}$	$\begin{array}{r} -389.89\\ -389.71\\ -389.71\\ -389.70\\ -43.64\\ -43.66\\ -43.63\\ -43.89.90\\ -389.94\\ -389.94\\ -389.94\\ -389.90\\ -389.90\\ -389.91\\ -389.91\\ -9.770\\ -9.770\\ -9.770\\ -9.770\\ -9.7761\\ -9.761\\ -9.761\\ -9.761\\ -9.759\\ -9.759\\ -9.759\\ -9.759\end{array}$	39 39 39 4.4 4.4 4.4 4.4 4.4 39	$59 \\ 139 \\ 49 \\ 524 \\ 205 \\ 244 \\ 78 \\ 220 \\ 422 \\ 236 \\ 320 \\ 2356 \\ 320 \\ 325 \\ 325 \\ 911 \\ 1225 \\ 69 \\ 274 $	$11\\310\\623\\33\\15\\35\\15\\4\\8\\4\\13\\8\\6\\6\\8\\18\\6\\3\\1\\14\\7$	$\begin{array}{c} -128\\ 678\\ -323\\ 170\\ 105\\ -344\\ -189\\ -599\\ -428\\ 315\\ -304\\ 1109\\ 414\\ 454\\ -737\\ 177\\ 177\\ -91\\ -90\\ 31\end{array}$	$\begin{array}{r} \overline{302}\\ \overline{302}\\ 799\\ 324\\ 204\\ 105\\ 125\\ 378\\ 242\\ 731\\ 222\\ 328\\ 472\\ 2328\\ 107\\ 200\\ 1096\\ 103\\ 338\\ 1130\\ 115\\ 251\\ 432\\ 4161 \end{array}$	$\begin{array}{c} 0.00\\ 0.00\\ 0.00\\ 0.15\\ 0.00\\$	NRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR

	Table A.2	Continued	from	previous	page
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$N_{ m run}$	T [ns]	D [ns]	P [W]	B [Gauss]	<pre> θpol [deg.] </pre>	v <sub>fit</sub> [Hz]	$\Delta  u_{ m fit}  [ m Hz]$	DC <sub>B</sub> [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	∆SC [Hz]	v0 [Hz]	$\Delta  u_0  [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{c} 860\\ 8661\\ 8662\\ 8663\\ 8664\\ 8668\\ 8668\\ 8669\\ 871\\ 8732\\ 8772\\ 8773\\ 8775\\ 8776\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8778\\ 8879\\ 8891\\ 8892\\ 8892\\ 8893\\ 8894\\ 8895\\ 8892\\ 8892\\ 8893\\ 8894\\ 8895\\ 8896\\ 8997\\ 9901\\ 9902\\ 9903\\ 9904\\ 9905\\ 9907\\ 9908\\ 8996\\ 9907\\ 9907\\ 9908\\ 8996\\ 9907\\ 9907\\ 9908\\ 8996\\ 9909\\ 9901\\ 9907\\ 9908\\ 8996\\ 9909\\ 9901\\ 9907\\ 9908\\ 8996\\ 9909\\ 9901\\ 9907\\ 9908\\ 8996\\ 9909\\ 9901\\ 9902\\ 9903\\ 9904\\ 9905\\ 9907\\ 9908\\ 9909\\ 9907\\ 9908\\ 8996\\ 9909\\ 9901\\ 9907\\ 9908\\ 8996\\ 9907\\ 9908\\ 9909\\ 9907\\ 9908\\ 9900\\ 9900\\ 9$	$\begin{array}{c} 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600\\ 600$	$\begin{array}{c} 100\\ 100\\ 100\\ 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ 50\\ $	$\begin{array}{c} 67.5\\ 77.5\\ 64.5\\ 77.5\\ 74.15\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.55\\$	$\begin{array}{c} -4.762\\ -4.762\\ 9.524\\ -9.5256\\ -9.5356\\ -9.5357\\ -9.5556\\ -9.5556\\ -9.5357\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5357\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ -9.5556\\ $	$\begin{array}{c} 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\$	$\begin{array}{r} 9978\\ 99978\\ 99978\\ 99977\\ 39630\\ 38858\\ 4172\\ 39230\\ 38858\\ 4172\\ 39230\\ 38858\\ 4172\\ 39230\\ 39297\\ 9108\\ 10411\\ 38734\\ 02445\\ 10411\\ 38736\\ 10411\\ 38736\\ 10411\\ 38736\\ 10411\\ 38736\\ 10411\\ 38736\\ 10411\\ 38736\\ 10411\\ 39760\\ 39297\\ 39297\\ 39257\\ 39297\\ 32784\\ 156152\\ 12568\\ 32850\\ 119262\\ 328501\\ 12568\\ 328502\\ 12568\\ 328502\\ 12568\\ 328502\\ 12568\\ 328502\\ 12568\\ 328502\\ 12568\\ 328502\\ 12568\\ 328502\\ 125281\\ 12568\\ 32973\\ 32784\\ 125942\\ 25281\\ 125729\\ 32784\\ 12393\\ 32784\\ 12351\\ 155729\\ 32982\\ 45610\\ 1196387\\ 741\\ 32982\\ 455610\\ 1196387\\ 7525\\ 68873\\ 1196387\\ 1196387\\ 125942\\ 25942\\ 25942\\ 15574\\ 1196387\\ 1196387\\ 1196387\\ 1196387\\ 125942\\ 25942\\ 15574\\ 1196387\\ 1196387\\ 125942\\ 25942\\ 155841\\ 1568429\\ 77809\\ 99633\\ 7809\\ 9963\\ 7809\\ 99633\\ 7809$	$\begin{array}{c} 2333\\ 5431\\ 5738\\ 2728\\ 3631\\ 2728\\ 3633\\ 6319\\ 3420\\ 6600\\ 2202\\ 2282\\ 2070\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2207\\ 1255\\ 2033\\ 2035\\$	$\begin{array}{r} -9760\\ -9760\\ -9760\\ -38989\\ -38969\\ -38969\\ -38969\\ -38969\\ -38969\\ -9772\\ -9773\\ -38989\\ -9772\\ -9773\\ -38968\\ -9772\\ -9773\\ -38968\\ -9772\\ -9773\\ -38968\\ -38968\\ -38996\\ -38996\\ -38996\\ -38996\\ -38996\\ -38996\\ -38996\\ -38996\\ -38996\\ -38995\\ -7916\\ -38966\\ -38995\\ -7916\\ -38966\\ -38995\\ -7916\\ -38966\\ -38995\\ -34365\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -155928\\ -33265\\ -2459\\ -2459\\ -2459\\ -2459\\ -24596\\ -2459\\ -24596\\ -2459\\ -24596\\ -2459\\ -2459\\ -24596\\ -2459\\ -2459\\ -32788\\ -45835\\ -25782\\ -2459\\ -32788\\ -45835\\ -25782\\ -2459\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -4588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -108269\\ -32788\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\ -2588\\$	$\begin{array}{r} 9.8\\ 9.8\\ 3.9\\ 3.9\\ 3.9\\ 3.9\\ 3.9\\ 3.9\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 9.8\\ 3.9\\ 1.5\\ 1.5\\ 1.5\\ 1.5\\ 1.5\\ 1.5\\ 1.5\\ 1.5$	$\begin{array}{c} 248\\ 21\\ 279\\ 579\\ 522\\ 499\\ 2236\\ 117\\ 69\\ 243\\ 140\\ 2841\\ 1054\\ 181\\ 149\\ 1054\\ 1056\\ 1$	$\begin{smallmatrix} 6 & 0 & 6 \\ 16 & 0 & 6 \\ 10 & 16 & 6 & 4 \\ 10 & 3 & 0 & 6 & 3 & 6 \\ 3 & 3 & 3 & 5 & 7 & 8 & 8 \\ 12 & 4 & 6 & 4 & 20 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 4 & 2 & 4 & 5 & 3 & 18 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 4 & 2 & 4 & 5 & 3 & 18 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 4 & 2 & 4 & 5 & 3 & 18 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 1 & 2 & 2 & 4 & 5 & 3 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 1 & 2 & 2 & 4 & 5 & 3 \\ 1 & 1 & 16 & 19 & 20 & 2 \\ 1 & 2 & 16 & 2 & 2 & 2 \\ 1 & 2 & 2 & 5 & 2 & 4 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 2 & 16 \\ 2 & 2 & 2 & 1$	$\begin{array}{c} -30\\ -370\\ $	$\begin{array}{c} 2333\\ 5434\\ 5752\\ 2729\\ 3703\\ 36329\\ 3440\\ 66612\\ 2285\\ 2260\\ 1261\\ 20221\\ 1202\\ 2211\\ 1202\\ 2221\\ 1244\\ 1259\\ 2260\\ 1261\\ 202221\\ 1244\\ 1259\\ 2260\\ 1261\\ 202221\\ 1264\\ 1255\\ 2260\\ 1261\\ 202222\\ 211\\ 202222\\ 211\\ 202222\\ 211\\ 202222\\ 2033\\ 2167\\ 202222\\ 2033\\ 2167\\ 202222\\ 2162\\ 2162\\ 202222\\ 2162\\ 2162\\ 202222\\ 216$	$\begin{array}{c} 0.04\\ 0.02\\ 0.00\\$	RRRRRRRRRRRRRRRRRRRRRRRRRBBBBRRBBBBRRBBBB

$N_{ m run}$	$T \; [\mathrm{ns}]$	D [ns]	P [W]	B [Gauss]	$\theta_{\mathrm{pol}} ~[\mathrm{deg.}]$	$ u_{ m fit}$ [Hz]	$\Delta \nu_{\rm fit}   [{\rm Hz}]$	$DC_{B}$ [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	$\Delta SC [Hz]$	ν0 [Hz]	$\Delta \nu_0 \; [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{l} 958\\ 959\\ 960\\ 961\\ 962\\ 963\\ 966\\ 9967\\ 9968\\ 9969\\ 9970\\ 9971\\ 9972\\ 9973\\ 9974\\ 9975\\ 9977\\ 9978\\ 9980\\ $	$\begin{array}{c} 400\\ 500\\ 500\\ 400\\ 500\\ 500\\ 500\\ 400\\ 4$	$\begin{array}{c} 1000\\ 1025\\ 1000\\ 1255\\ 1000\\ 1000\\ 1000\\ 500\\ 1000\\ $	$\begin{array}{c} 32.5\\ 32.5\\ 30\\ 22.5\\ 37.6\\ 0\\ 15\\ 7.25\\ 7.1.25$	$\begin{array}{l} {}^{+}.357\\ 3.333\\ -19.048\\ 4.167\\ -3.333\\ -19.048\\ 19.048\\ 19.048\\ -5.357\\ -10.119\\ 3.968\\ 19.048\\ -5.357\\ -33.334\\ -14.286\\ -19.048\\ -28.572\\ -2.381\\ -19.048\\ -2.5556\\ -19.048\\ -2.2778\\ -2.2381\\ -15.875\\ -2.268\\ -2.278\\ -2.288\\ -2.288\\ -2.278\\ -2.288\\ -$	$\begin{array}{c} 1700\\ 1700\\ 1700\\ 1700\\ 1700\\ 1700\\ 1700\\ 1700\\ 1700\\ 22660\\ 22660\\ 22660\\ 22660\\ 22660\\ 22660\\ 22660\\ 22660\\ 22660\\ 2260$	$\begin{array}{r} 12359\\ 44977\\ 155870\\ 77725\\ 4508\\ 156390\\ 156074\\ 12514\\ 43912\\ 64949\\ 156193\\ 108405\\ 108003\\ 477897\\ 477871\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 478014\\ 156448\\ 351126\\ 351250\\ 25869\\ 1083046\\ 125506\\ 12520\\ 12628\\ 126$	$\begin{array}{c} 1269\\ 1253\\ 1269\\ 1557\\ 1956\\ 1864\\ 1339\\ 1877\\ 2078\\ 8770\\ 666\\ 651\\ 156\\ 665\\ 146\\ 665\\ 146\\ 665\\ 1456\\ 665\\ 1456\\ 665\\ 1456\\ 166\\ 166\\ 166\\ 166\\ 166\\ 166\\ 166\\ 1$	$\begin{array}{r} -12366\\ -4787\\ -155926\\ -47787\\ -155972\\ -155972\\ -155981\\ -12354\\ -44000\\ -6798\\ -155972\\ -108272\\ -108310\\ -6798\\ -155974\\ -108272\\ -108310\\ -477397\\ -477422\\ -877739\\ -477415\\ -87773\\ -87772\\ -87774\\ -87774\\ -87774\\ -350615\\ -9763\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108306\\ -2465\\ -108336\\ -2468\\ -155929\\ -13268\\ -32769\\ -332769\\ -332769\\ -47905\\ -33769\\ -47905\\ -33769\\ -47905\\ -33769\\ -47905\\ -33769\\ -47905\\ -33785\\ -33785\\ -33785\\ -33785\\ -33785\\ -33785\\ -33785\\ -33785\\ -33785\\ -4786\\ -47866\\ -155959\\ -155929\\ -33288\\ -33785\\ -4786\\ -155959\\ -155926\\ -12364\\ -47866\\ -155959\\ -155926\\ -12364\\ -47866\\ -155959\\ -33288\\ -33785\\ -4786\\ -155959\\ -33288\\ -33785\\ -4786\\ -155959\\ -155926\\ -155$	$\begin{array}{c} 12.4\\ 4.4\\ 155.9\\ 7.5\\ 7.4\\ 8.6\\ 156.9\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 126.4\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 108.3\\ 155.9\\ 155.9\\ 155.9\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 32.8\\ 108.3\\ 32.8\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 108.3\\ 32.8\\ 108.3\\ 10$	$\begin{array}{c} 1514\\ 1501\\ 151\\ 104\\ 1501\\ 1051\\ 102\\ 102\\ 102\\ 102\\ 102\\ 102\\ 102\\ 10$	$\begin{smallmatrix} 48 & 4 & 4 \\ 18 & 4 & 0 \\ 20 & 9 & 29 \\ 21 & 9 & 9 \\ 21 & 29 & 21 \\ 21 & 21 & 21 \\ 21 & 21 & 21 \\ 21 & 21 &$	$\begin{array}{c} ^{+157} \\ ^{+86} \\ ^{-206} \\ ^{-202} \\ ^{-3745} \\ ^{-109} \\ ^{-108} \\ ^{-1128} \\ ^{-3765} \\ ^{-109} \\ ^{-1128} \\ ^{-3765} \\ ^{-111} \\ ^{-387} \\ ^{-38$	$\begin{array}{c} 1279\\ 218\\ 1279\\ 218\\ 1410\\ 1286\\ 484\\ 4111\\ 1286\\ 484\\ 4111\\ 1168\\ 3560\\ 651\\ 1765\\ 2357\\ 165\\ 257\\ 1285\\ 216\\ 219\\ 218\\ 216\\ 219\\ 218\\ 216\\ 219\\ 2125\\ 2157\\ 218\\ 216\\ 219\\ 216\\ 219\\ 2125\\ 216\\ 219\\ 212\\ 219\\ 216\\ 219\\ 210\\ 210\\ 210\\ 210\\ 210\\ 210\\ 210\\ 210$	$\begin{array}{c} 0.08\\ 0.08\\ 0.001\\ 0.001\\ 0.001\\ 0.001\\ 0.001\\ 0.000\\ 0.00$	KRBRRBRBRBRBBBBBBBBBBBBBBBBBBBBBBBBBBB

un1 17 557	5000 5000 5000	[su] Q 125 125	[M] <u>d</u>	-3.333 -3.324 -3.524	$\begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	[zH] <sup>1</sup> H] <sup>1</sup> H] <sup>1</sup> H <sup>1</sup> H	253776 25776	DC <sup>B</sup> [H <sup>Z</sup> ] DC <sup>-4779</sup> -999904	DCB [Hz]	[¤H] DS 104	ASC [Hz]	[zH] 07 -137 1132	[zH] 0 <sup>∧</sup> √ 2555 2175	0000 wts. [%]	Data Type
159 160 161 162 163 164 166 166 166 166 166 166 172 173 175 177 175 177 177 177 177 177	$\begin{array}{c} 400\\ 300\\ 300\\ 300\\ 400\\ 400\\ 300\\ 300\\$	$\begin{array}{c} 2000\\ 1000\\ 500\\ 1000\\ 1500\\ 1500\\ 1000\\ 1000\\ 1500\\ 1000\\ 1500\\ 1000\\ $	$\begin{smallmatrix}&15\\22.5\\37.5\\7.5\\7.5\\7.5\\15\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.5\\22.5\\7.2\\2.5\\7.1\\25\\71.25\\71$	$\begin{array}{c} 7.738\\ 5.556\\ 10.317\\ 5.556\\ 6.548\\ 19.048\\ -3.968\\ 3.968\\ 3.968\\ 3.908\\ 3.908\\ 3.908\\ 3.908\\ 3.908\\ 3.908\\ -4.167\\ 9.048\\ 19.048\\ -4.167\\ 9.048\\ -4.167\\ 9.524\\ 9.524\\ 9.524\\ 9.524\\ 9.524\\ -4.762\\ -4.762\\ \end{array}$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 20098\\ 13507\\ 45750\\ 13404\\ 18451\\ 6878\\ 156046\\ 13345\\ 156032\\ 156365\\ 7074\\ 7012\\ 155906\\ 156003\\ 7717\\ 32918\\ 155987\\ 7611\\ 34323\\ 45998\\ 3950\\ 19350\\ 19350\\ 39475\\ 39475\\ 39400\\ 39475\\ 39400\\ 10276\\ 10276\\ 10276\\ 10276\\ 10306\end{array}$	$\begin{array}{c} 139\\ 104\\ 110\\ 274\\ 130\\ 274\\ 130\\ 274\\ 130\\ 207\\ 132\\ 105\\ 122\\ 123\\ 102\\ 152\\ 123\\ 102\\ 152\\ 126\\ 359\\ 74\\ 135\\ 126\\ 359\\ 74\\ 135\\ 140\\ 49\\ 544\\ 754\\ 445\\ 754\\ 552\\ 552\\ 552\\ 552\\ 552\\ 552\\ 552\\ 5$	$\begin{array}{r} -25799\\ -13280\\ -13280\\ -13280\\ -18472\\ -43998\\ -6788\\ -135968\\ -135968\\ -135968\\ -155971\\ -155924\\ -55973\\ -255973\\ -155974\\ -155974\\ -155974\\ -155974\\ -155974\\ -155974\\ -32785\\ -6799\\ -119335\\ -7481\\ -34999\\ -38993\\ -38993\\ -38993\\ -9760\\$	$\begin{array}{c} 23.8\\ 23.3\\ 45.8\\ 44\\ 6.8\\ 156\\ 13.3\\ 18.5\\ 44\\ 6.8\\ 156\\ 155.9\\ 156.9\\ 166.8\\ 119.3\\ 7.5\\ 32.86\\ 168\\ 19.3\\ 7.5\\ 34.3\\ 45.8\\ 319\\ 339\\ 39\\ 39\\ 39\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.$	$\begin{array}{c} 219\\ 219\\ 105\\ 81\\ 95\\ 105\\ 801\\ 801\\ 94\\ 103\\ 801\\ 94\\ 103\\ 801\\ 103\\ 801\\ 103\\ 801\\ 101\\ 101\\ 101\\ 101\\ 105\\ 105\\ 105\\ 1$	$\substack{44\\16\\21\\29\\16\\2\\2\\3\\9\\18\\1\\20\\3\\21\\4\\20\\20\\12\\12\\12\\12\\12\\12\\12\\12\\12\\12\\12\\12\\12\\$	$\substack{812\\812}\\812\\-162\\-300\\-126\\181\\100\\-2\\-333\\328\\198\\198\\198\\-71\\133\\-22\\-71\\133\\-86\\-90\\-222\\-126\\-86\\-322\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-90\\-222\\-18\\-18\\-90\\-222\\-18\\-18\\-18\\-18\\-18\\-18\\-18\\-18\\-18\\-18$	$\begin{array}{c} 148\\ 105\\ 1206\\ 276\\ 155\\ 131\\ 199\\ 1259\\ 134\\ 1267\\ 213\\ 101\\ 227\\ 123\\ 101\\ 1220\\ 1237\\ 143\\ 149\\ 64\\ 685\\ 885\\ 665\\ 77\\ 256\end{array}$	$\begin{array}{c} 0.00\\ 0.06\\ 0.00\\ 0.01\\ 0.01\\ 0.00\\$	NN LNRBRBRBRRBRRBRRBRRBRRRR LINN LINN LEBRRBRRBRRBRRRRR LINN LINN NN LINN NNN NNN NNN NNN NNN NN
3839011234456678990012344560789001123445	300         300         300	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 71.25\\ 71$	$\begin{array}{r} -23.81\\ -23.81\\ -9.524\\ -9.524\\ -9.524\\ 23.81\\ 23.81\\ 23.81\\ 14.286\\ 14.286\\ 14.286\\ 14.286\\ 14.286\\ 14.286\\ 28.572\\ 28.572\\ 28.572\\ 28.572\\ 28.572\\ 28.572\\ 28.572\\ 28.572\\ -4.762\\ -4$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{r} 244045\\ 244125\\ 244125\\ 244125\\ 39607\\ 399607\\ 399604\\ 244260\\ 244186\\ 244186\\ 244186\\ 244186\\ 244091\\ 88324\\ 88364\\ 88286\\ 10242\\ 100242\\ 10038\\ 351262\\ 351196\\ 477993\\ 851262\\ 351196\\ 477993$	$\begin{array}{c} 708\\ 888\\ 559\\ 560\\ 556\\ 557\\ 563\\ 344\\ 759\\ 522\\ 555\\ 877\\ 415\\ 781\\ 782\\ 812\\ 81\\ 381 \end{array}$	$\begin{array}{r} -243528\\ -243553\\ -243553\\ -38978\\ -38978\\ -38977\\ -38967\\ -243601\\ -243607\\ -243602\\ -87809\\ -87809\\ -87809\\ -87802\\ -9773\\ -9771\\ -9771\\ -9771\\ -350653\\ -350694\\ -477481\\ -9774\\ -350653\\ -350680\\ -477481\\ -9772\\ -9772\\ -9772\\ -9772\\ -9758\\ -9755\\ -9756\end{array}$	$\begin{array}{c} 243.5\\ 243.6\\ 243.6\\ 39\\ 39\\ 243.6\\ 243.6\\ 243.6\\ 243.6\\ 87.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9$	$\begin{array}{c} 500\\ 5000\\ 5000\\ 5000\\ 4998\\ 4988\\ 4988\\ 4988\\ 4988\\ 4988\\ 4988\\ 4988\\ 4989\\ 4999\\ 5000\\ 5004\\ 5003\\ 5004\\ 5003\\ 5004\\ 1881\\ 1812\\ 182\\ 182\\ 182\\ 182\\ 182\\ 1$	$\begin{array}{c} 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\$	$\begin{array}{c} 17\\ 72\\ -17\\ 129\\ -23\\ 139\\ 160\\ 80\\ -8\\ 18\\ 66\\ -14\\ -29\\ -47\\ 109\\ 112\\ 15\\ 8\\ -27\\ 69\\ 109\\ 112\\ 15\\ 8\\ -27\\ 69\\ 109\\ -174\\ 101\\ -173\\ -173\end{array}$	$\begin{array}{c} 2543\\ 259\\ 69\\ 721\\ 2511\\ 249\\ 250\\ 1006\\ 1006\\ 375\\ 359\\ 355\\ 481\\ 483\\ 355\\ 481\\ 483\\ 877\\ 5445\\ 415\\ 7828\\ 1261\\ 381\\ \end{array}$	$\begin{array}{c} 0.00\\$	LBBRRRBBBBRRRRBBBBBRRRRR LLBBRRRRBBBBRRRRRRR LLLBBBRRRRRRRR
6789012345678901234567890122	900 900 900 900 900 900 900 900 900 900	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 74.25\\ 74$	$\begin{array}{c} 4.762\\ -4.762\\ $	$\begin{array}{c} 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\$	$\begin{array}{r} 9865\\ 9864\\ 10059\\ 9379\\ 11310\\ 10477\\ 10420\\ 9335\\ 8277\\ 9632\\ 10888\\ 9911\\ 8872\\ 9673\\ 10517\\ 9875\\ 9617\\ 10132\\ 10305\\ 10047\\ 10030\\ 10255\\ 10047\\ 10030\\ 10255\\ 11309\\ 99955\\ 95549\\ 95549\\ 9519\\ 95545\end{array}$	$\begin{array}{r} 8425\\ 804\\ 496\\ 734\\ 396\\ 2359\\ 450\\ 405\\ 405\\ 405\\ 405\\ 405\\ 405\\ 405$	$\begin{array}{r} -9772\\ -9757\\ -9757\\ -9772\\ -9772\\ -9772\\ -9772\\ -9772\\ -9772\\ -9777\\ -9777\\ -9777\\ -9777\\ -9777\\ -9770\\ -9760\\ -9770\\ -9$	9.88 9.88 9.88 9.88 9.88 9.88 9.98 9.98	$183 \\ 183 \\ 183 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 184 \\ 205 \\ 206 \\ 207 \\ 207 \\ 207 \\ 207 \\ 183 \\ 183 \\ 184 \\ 205 \\ 206 \\ 207 $	444444444444445555555554444	$\begin{array}{r} -89\\ -76\\ 103\\ -561\\ 1354\\ 521\\ 480\\ -619\\ -4619\\ -4619\\ -4619\\ -309\\ 947\\ -45\\ -1071\\ -271\\ -273\\ -349\\ -349\\ -358\\ 1341\\ 1\\ -396\\ -437\\ -586\\ -586\\$	$\begin{array}{r} 8425\\ 8047\\ 7344\\ 3977\\ 23597\\ 44530\\ 44530\\ 44530\\ 44530\\ 4450\\ 455711\\ 3177\\ 3383\\ 3426\\ 4682\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 4462\\ 8337\\ 8332\\ 8337\\ 8332\\ 8332\\ 8337\\ 8332\\ 8332\\ 8337\\ 8332$	$\begin{array}{c} 0.01\\ 0.02\\ 0.01\\ 0.02\\ 0.01\\ 0.02\\ 0.01\\ 0.02\\ 0.00\\ 0.02\\ 0.00\\ 0.02\\ 0.00\\ 0.02\\ 0.01\\ 0.01\\ 0.01\\ 0.01\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.02\\ 0.03\\ 0.01\\$	NRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR
54567890123	800 800 800 300 300 300 300 300 300 300	$     \begin{array}{r}       100\\       100\\       100\\       100\\       100\\       100\\       100\\       100\\       100\\       100      $	74.25 74.25 74.25 67.5 67.5 67.5 15 15 15 15 60	$^{+1.762}_{-4.762}$ $^{-4.762}_{-4.762}$ $^{-4.762}_{-4.762}$ $^{-4.762}_{-4.762}$ $^{-4.762}_{-4.762}$ $^{-4.762}_{-4.762}$	$260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 \\ 260 $	9503 9504 9706 9402 10033 10028 10291 10251 9822 9965 10051	$     \begin{array}{r}       176 \\       326 \\       383 \\       401 \\       165 \\       157 \\       154 \\       198 \\       196 \\       266 \\       148 \\     \end{array} $	-9713 -9758 -9759 -9760 -9723 -9723 -9723 -9724 -9724 -9724 -9723 -9723	9.8 9.8 9.8 9.7 9.7 9.7 9.7 9.7 9.7 9.7 9.7	$204 \\ 204 \\ 205 \\ 206 \\ 461 \\ 462 \\ 463 \\ 91 \\ 90 \\ 90 \\ 401$	$     \begin{array}{c}       35 \\       55 \\       55 \\       11 \\       11 \\       22 \\       22 \\       10 \\     \end{array} $	-459 -258 -563 -151 -157 105 437 9 152 -73	$     \begin{array}{r}       176 \\       326 \\       383 \\       401 \\       166 \\       158 \\       154 \\       198 \\       196 \\       266 \\       148 \\     \end{array} $	$\begin{array}{c} 0.01\\ 0.02\\ 0.02\\ 0.02\\ 0.00\\$	NR NR UP UP UP UP UP UP UP

$N_{ m run}$	$T \ [ns]$	D [ns]	P [W]	B [Gauss]	<pre> θpol [deg.] </pre>	vfit [Hz]	$\Delta \nu_{\rm fit}   [{ m Hz}]$	DC <sub>B</sub> [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	ΔSC [Hz]	۰۰0 [Hz]	$\Delta  u_0  [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{c}1154\\1155\\1156\\1157\\1158\\1156\\1166\\1166\\1166\\1166\\1166\\1166$	300 300 300 300 300 300 300 300	$\begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$		$\begin{array}{c} -4.762\\ -4.762\\ -4.762\\ -14.286\\ -14.286\\ 14.286\\ -14.286\\ $	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	9918 101952 877206 88147 87206 88147 87206 88147 87206 88147 87206 87206 8702 87027	$\begin{array}{c} 1422\\ 1233\\ 2244\\ 2458\\ 1950\\ 2472\\ 2998\\ 2476\\ 4999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2170\\ 2999\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2090\\ 2000\\$	$\begin{array}{c} -9723\\ -9723\\ -87524\\ -87656\\ -876524\\ -87656\\ -876524\\ -87656\\ -97223\\ -87524\\ -87656\\ -9766\\ -9766\\ -97623\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -87524\\ -9766\\ -9723\\ -9766\\ -9723\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9766\\ -9762\\ -9766\\ -9766\\ -9762\\ -9766\\ -9766\\ -9762\\ -9766\\ -9762\\ -9766\\ -9762\\ -9766\\ -9762\\ -9722\\$	$\begin{array}{c} 77555577768888555555555555555555555888877778888777777$	$\begin{array}{c} 404\\ 404\\ 4048\\ 2248\\ 459\\ 991\\ 1400\\ 1452\\ 8459\\ 441\\ 1489\\ 45509\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 4065\\ 5097\\ 5006\\ 5097\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5007\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5007\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5006\\ 5007\\ 5006\\ 5006\\ 5006\\ 5007\\ 5006\\ 500$	10666611111222233331111111111122200000011111555888222255566688811100777777222222555555551111166663333777788883337777333377773333777733337777333377773333	$\begin{array}{c} -209\\ -658\\ -209\\ -475\\ -368\\ -475\\ -368\\ -265\\ -261\\ -2869\\ -265$	$\begin{array}{c} 1433\\ 22603\\ 22124\\ 1903\\ 2322\\ 1245\\ 23371\\ 235229\\ 1235\\ 2292\\ 23371\\ 1235\\ 2292\\ 2355\\ 2295\\ 1223\\ 2295\\ 2222\\ 2295\\ 2222\\ 2295\\ 2222\\ 2295\\ 2222\\ 2295\\ 2222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 22222\\ 2255\\ 2255\\ 222222\\ 2255\\ 2255\\ 222222\\ 2255\\ 2255\\ 222222\\ 2255\\ 2255\\ 22222222$	$\begin{array}{c} 0.00\\ 0.0$	PPABBBBBB UUUUUUUUUUUUUUUUUUUUUUUUUUUUUU

ц	ns]	[su]	[m	Gauss]	l [deg.]	[Hz]	fit [Hz]	B [Hz]	C <sub>B</sub> [Hz]	[Hz]	C [Hz]	[Hz]	0 [Hz]	. [%]	ta Type
$N_{ m r1}$	T	D	Ρ.	B [	$\theta_{\mathrm{po}}$	νfit	$\Delta \nu$	DC	ΔD	sC	$\Delta_{\rm S}$	ν <sub>0</sub>	$\Delta_{\nu}$	wts	Da
$\begin{array}{c} 12523\\ 1255\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1256\\ 1266$	3000 3000 3000 3000 3000 3000 3000 300	$\begin{array}{c} 1000\\$	$\begin{array}{c} (4.25)\\$	$\begin{array}{c} -4.762\\$	$\begin{array}{c} 2600\\ 2700\\$	$\begin{array}{c} 10252\\ 10015\\ 10014\\ 10714\\ 87470\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 99507\\ 10140\\ 10325\\ 243599\\ 244117\\ 3516260\\ 156395\\ 243599\\ 244117\\ 3516260\\ 10547\\ 351134\\ 350475\\ 10547\\ 351134\\ 10154\\ 350475\\ 10154\\ 350475\\ 10154\\ 350475\\ 10154\\ 350475\\ 10154\\ 350475\\ 10154\\ 10154\\ 10154\\ 10154\\ 10195\\ 99772\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99772\\ 99739\\ 99772\\ 997739\\ 99763\\ 99772\\ 997739\\ 99763\\ 99772\\ 99772\\ 99739\\ 99763\\ 99772\\ 99772\\ 99739\\ 99772\\ 99739\\ 99772\\ 99772\\ 99739\\ 99772\\ 99772\\ 99772\\ 99739\\ 99772\\ 99772\\ 99772\\ 99772\\ 99773\\ 99772\\ 9977$	$\begin{array}{c} 1865\\ 1665\\ 1665\\ 3351\\ 3326\\ 63064\\ 3561\\ 3564\\ 3560\\ 2238\\ 1980\\ 1980\\ 1283\\ 1681\\ 14217\\ 161\\ 1392\\ 1503\\ 1684\\ 192\\ 2252\\ 1025\\ 1272\\ 1652\\ 2790\\ 1393\\ 1684\\ 192\\ 2254\\ 1651\\ 22790\\ 1393\\ 1025\\ 1222\\ 12222\\ 1222\\ 1222\\ 1222\\ 1222\\ 1222\\ 1222\\ 12222\\ 1222\\ 1222\\ 1222\\ 122$	-9/21 9722 -9722 -9722 -9722 -9722 -87519 -9765 -9765 -9765 -9765 -9764 -9764 -9764 -9764 -9764 -9764 -39983 -9723 -9764 -243946 -39983 -9772 -242934 -243946 -39983 -87649 -243946 -39983 -87655 -87655 -87655 -87655 -87655 -87655 -87655 -87655 -87655 -9722 -9723 -97723 -97765 -9723 -97765 -9723 -97765 -9722 -9723 -9765 -9722 -97723 -9765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765 -97723 -97765	$\begin{array}{c} 9.7775558888777788885767991999999999999999999999999999999999$	$\begin{array}{r} 4992\\ 5091\\ 990\\ 492\\ 446\\ 3350\\ 2444\\ 496\\ 5003\\ 2244\\ 496\\ 5003\\ 5002\\ 2503\\ 5003\\ 5002\\ 2933\\ 5002\\ 5003\\ 5002\\ 2933\\ 5002\\ 2933\\ 5003\\ 5002\\ 2933\\ 5002\\ 2933\\ 5003\\ 5002\\ 2933\\ 4032\\ 2944\\ 4556\\ 4556\\ 4553\\ 4556\\ 4553\\ 402\\ 2943\\ 4026\\ 4556\\ 2933\\ 4002\\ 2944\\ 4550\\ 2933\\ 4002\\ 2944\\ 4012\\ 2934\\ 4012\\ 2934\\ 4011\\ 1399\\ 2934\\ 4011\\ 1399\\ 2934\\ 4011\\ 1399\\ 2934\\ 4011\\ 1399\\ 2934\\ 4011\\ 1399\\ 2934\\ 4011\\ 1910\\ 1945\\ 5002\\ 5002\\ 5002\\ 5002\\ 2932\\ 2410\\ 1900\\ 1900\\ 2929\\ 2410\\ 1910\\ 1910\\ 1910\\ 1910\\ 1910\\ 1910\\ 1902\\ 2025\\ 5002\\ 2932\\ 2410\\ 2409\\ 1899\\ 3979\\ 3979\\ 3979\\ 3979\\ 3979\\ 3970\\$	1222221111888866661221212121212121212121	$\begin{array}{c} 328\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -208\\ -209\\ -289\\ -203\\ -289\\ -299\\ -119\\ -1400\\ -400\\ -400\\ -400\\ -400\\ -400\\ -282\\ -292\\ -282\\$	$\begin{array}{c} 1866\\ 1866\\ 1662\\ 3308\\ 3308\\ 33054\\ 3610\\ 2408\\ 199\\ 2533\\ 190\\ 1217\\ 1209\\ 286\\ 1388\\ 1399\\ 2303\\ 2187\\ 2935\\ 1406\\ 1036\\ 1333\\ 1467\\ 1608\\ 2419\\ 1036\\ 1333\\ 1467\\ 1618\\ 1333\\ 1467\\ 1618\\ 1427\\ 2935\\ 1406\\ 1333\\ 1467\\ 1618\\ 1427\\ 2935\\ 1618\\ 173\\ 1618\\ 1427\\ 2106\\ 1218\\ 1618\\ 1100\\ 1214\\ 1966\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 2106\\ 1309\\ 1553\\ 1982\\ 2263\\ 1100\\ 1214\\ 1965\\ 1288\\ 12$	0.000 0.0000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	UPPPBEB UUDPPDUUDPPPBB UUDPDUUDPPPBB UUDDUUDPPPBB UUDDUUDUUDPPBBB UUDDUUDUUDPPBBBBBBBBBB

$l_{run}$	' [ns]	[us]	[M]	3 [Gauss]	pol [deg.]	fit [Hz]	ν <sub>fit</sub> [Hz]	DC <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	0 [Hz]	240 [Hz]	rts. [%]	lata Type
$\begin{array}{c} 1350\\ 1351\\ 1352\\ 1353\\ 1354\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1355\\ 1356\\ 13661\\ 13662\\ 13663\\ 13662\\ 13663\\ 13664\\ 13665\\ 13667\\ 1367\\ 1371\\ 1372\\ 1373\\ 1374\\ 1375\\ 1376\\ 1378\\ 1378\\ 1378\\ 1378\\ 1388\\ 1389\\ 1389\\ 1389\\ 13882\\ 1388\\ 1388\\ 1388\\ 13889\\ 13892\\ 13934\\ 1393\\$		100           100	$\begin{smallmatrix} 60\\ 22.5\\ 222.5\\ 222.5\\ 37.5\\ 15\\ 15\\ 15\\ 337.5\\ 55\\ 222.5\\ 337.5\\ 55\\ 222.5\\ 337.5\\ 55\\ 222.5\\ 337.5\\ 55\\ 222.5\\ 337.5\\ 55\\ 222.5\\ 55\\ 222.5\\ 55\\ 222.5\\ 55\\ 222.5\\ 55\\ 222.5\\ 55\\ 55\\ 55\\ 55\\ 55\\ 55\\ 55\\ 55\\ 55\\ $	$\begin{array}{c} -14.286\\ -14.286\\ 14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -4.762\\$	$\begin{array}{c} \mathbf{J} \\ 170 $	2 2 3 3 3 3 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 5 4 3 4 5 4 3 4 5 4 3 4 5 4 3 4 5 5 5 5 5 5 5 5 5 5 5 5 5	$\begin{array}{c} 1 \\ 182 \\ 2177 \\ 157 \\ 1212 \\ 129 \\ 154 \\ 206 \\ 192 \\$		$\begin{array}{c} 3\\ 87,77\\ 87,75\\ 88,77,75\\ 88,77$	$\begin{array}{c} 5\\ 3999\\ 1398\\ 1388\\ 1422\\ 1339\\ 1433\\ 1432\\ 1433\\ 1432\\ 1433\\$	$\frac{1}{1} \\ \frac{1}{1} \\ \frac{1}{3} \\ \frac{3}{3} \\ \frac{3}{3} \\ \frac{3}{6} \\ \frac{6}{6} \\ \frac{2}{2} \\ \frac{2}{2} \\ \frac{2}{2} \\ \frac{2}{2} \\ \frac{2}{6} \\ \frac{6}{6} \\ \frac{1}{11} \\ $	$\begin{array}{c} -& -260\\ -& -260\\ 157\\ +& 522\\ -& -347\\ -& -282\\ -$	202 2334 1820 2234 1229 1271 2214 2265 1271 2201 200 202 202 197 200 202 203 197 209 203 203 203 203 203 203 203 203 203 203	0.000           0.000 </td <td>L UUPLB UUPL</td>	L UUPLB UUPL

Table A.2 Continued from previous page

un:	[su]	[su]	[m]	[Gauss]	ol [deg.]	t [Hz]	∕fit [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	[Hz]	SC [Hz]	[Hz]	<sup>70</sup> [Hz]	s. [%]	ıta Type
2 1449	F 300	Q 100	<u>م</u> 15	n 14 286	0 170	₩ 2 87590	Ž	о 87527	I 87 5	SC 01	₫	20 02	م 260	<u><u></u></u>	
$\begin{smallmatrix} 1 & 490 \\ 1 & 451 \\ 1 & 455 \\ 1 & 555 \\ 1 $	$\begin{array}{c} 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300$	$\begin{array}{c} 1 & 0 & 0 \\$	$\begin{array}{c} 37.5, 5\\ 600\\ 600\\ 22.5, 5\\ 22.1, 5\\ 67.5, 5\\ 22.5$	$\begin{array}{c} 14.286\\ 14.286\\ 4.762\\ 4.762\\ 4.762\\ 14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -4.762\\ 14.286\\ -4.762\\ 4.762\\ -4.762\\ 14.286\\ -4.762\\$	$ \begin{array}{c} 1 \\ 7 \\ 7 \\ 0 \\ 1 \\ 1 \\ 7 \\ 0 \\ 1 \\ 1 \\ 7 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$	$\begin{array}{l} & 81044\\ 887483\\ 10156\\ 10195\\ 87733\\ 887483\\ 80156\\ 87952\\ 97842\\ 97855\\ 880167\\ 10205\\ 10205\\ 10205\\ 10205\\ 9769\\ 9769\\ 99621\\ 10205\\ 10205\\ 10205\\ 10205\\ 10205\\ 10205\\ 10205\\ 10205\\ 10205\\ 87867\\ 10205\\ 87817\\ 89417\\ 87840\\ 9962\\ 10205\\ 87867\\ 87810\\ 10205\\ 87840\\ 9962\\ 10205\\ 87867\\ 87810\\ 10205\\ 87840\\ 9962\\ 10205\\ 87867\\ 10205\\ 87840\\ 9962\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 10205\\ 87867\\ 87570\\ 87550\\ 87773\\ 87969\\ 9769\\ 9724\\ 87763\\ 87969\\ 97769\\ 9769\\ 9774\\ 87773\\ 87969\\ 97769\\ 9774\\ 87773\\ 87969\\ 9774\\ 87773\\ 87550\\ 87778\\ 8837\\ 8837\\ 88322\\ 87778\\ 88378\\ 8839\\ 87788\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8839\\ 87778\\ 887778\\ 8839\\ 87778\\ 8839\\ 87778\\ 8877$	$\begin{array}{c} 3073\\ 2179\\ 1478\\ 213\\ 1478\\ 213\\ 192\\ 2151\\ 1661\\ 142\\ 2201\\ 2215\\ 1661\\ 1442\\ 2201\\ 2215\\ 1661\\ 1442\\ 2201\\ 2215\\ 1661\\ 1611\\ 3029\\ 215\\ 1661\\ 1611\\ 3029\\ 215\\ 1661\\ 1611\\ 3029\\ 215\\ 2287\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 1841\\ 2212\\ 2285\\ 2463\\ 240\\ 240\\ 240\\ 240\\ 240\\ 2564\\ 240\\ 240\\ 2564\\ 240\\ 240\\ 2551\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 2086\\ 357\\ 245\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 3311\\ 245\\ 345\\ 356\\ 356\\ 356\\ 356\\ 356\\ 356\\ 356\\ 35$	$\begin{array}{r} +876529\\ +876549\\ +97654\\ +875248\\ +87528\\ +875528\\ +875528\\ +875528\\ +875528\\ +97266\\ +97266\\ +97265\\ +97266\\ +97634\\ +97648\\ +97663\\ +97636\\ +97664\\ +97663\\ +97664\\ +97663\\ +97266\\ +97664\\ +97664\\ +97664\\ +97665\\ +97266\\ +97266\\ +97665\\ +97664\\ +97664\\ +97665\\ +97664\\ +97664\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ +97665\\ +97664\\ $	$\begin{array}{l} 7.7688855555577.76677.78886668855588777.778662866558877777888888555888885555577.6666655577.755577777766677665566777766688888866677.78886668777888666778886667788866677888666888888$	$\begin{array}{c} 244\\ 2401\\ 403\\ 403\\ 143\\ 92\\ 454\\ 503\\ 244\\ 503\\ 244\\ 503\\ 244\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 505\\ 143\\ 298\\ 2505\\ 143\\ 298\\ 2505\\ 143\\ 298\\ 2505\\ 143\\ 298\\ 2505\\ 143\\ 298\\ 298\\ 244\\ 288\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 246\\ 208\\ 208\\ 208\\ 208\\ 208\\ 208\\ 208\\ 208$	66000033221112288116655883377722442233399776622211166991166666666000335522244433112244411188222111331115588222777777777777777777777777777777	$\begin{array}{c} 5081\\-410\\-108\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-194\\-128\\-1$	$\begin{array}{c} 319\\ 2179\\ 2179\\ 1171\\ 2230\\ 1192\\ 232\\ 167\\ 232\\ 232\\ 167\\ 232\\ 232\\ 167\\ 232\\ 232\\ 232\\ 167\\ 232\\ 232\\ 232\\ 232\\ 232\\ 232\\ 232\\ 23$		UPUDPLEBER UPUDPLEBER UPUDPLEBER UPUDPLEBER UPUDPLEBER UPUDPLEBER UPUDPLEBER UPUDDUDUDUDUDUDUDUDUDUDUDUDUDUDUDUDUDUD

Table	A.2	Continued	from	previous	page

run	[us]	[us]	[w]	[Gauss]	ool [deg.]	āt [Hz]	. <i>v</i> <sub>fit</sub> [Hz]	$C_{B}$ [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	[Hz] (	ν0 [Hz]	ts. [%]	ata Type
$\begin{array}{c} 1546\\ 1547\\ 1548\\ 1549\\ 1551\\ 1552\\ 1552\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1555\\ 1556\\ 15662\\ 15662\\ 15662\\ 15662\\ 15662\\ 15662\\ 15662\\ 15568\\ 15568\\ 15568\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15588\\ 15592\\ 1552$	$\begin{array}{c} 300\\ 300\\ 300\\ 300\\ 300\\ 400\\ 400\\ 400\\$	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 30\\ 30\\ 30\\ 45\\ 45\\ 67.5\\ 67.5\\ 67.5\\ 60\\ 74.25\\ 52.22\\ 22.25\\ 52.22\\ 22.25\\ 52.22\\ 22.25\\ 52.22\\ 22.25\\ 52.22\\ 60\\ 67.5\\ 52.22\\ 22.25\\ 52.22\\ 60\\ 67.5\\ 52.5\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.22\\ 60\\ 67.5\\ 52.22\\ 60\\ 67.5\\ 52.25\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.25\\ 60\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 52.5\\ 67.5\\ 77.5\\ 52.5\\ 67.5\\ 77.5\\ 52.5\\ 67.5\\ 77.5\\ 67.5\\ 77.5\\ 75.5\\ 7$	$\begin{array}{c} -14.286\\ -14.286\\ -14.286\\ -14.286\\ -14.286\\ -4.762\\ -4.762\\ -4.762\\ -4.762\\ -4.762\\ -4.762\\ -14.286\\ -4.762\\$	$\begin{array}{c} 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\ 170\\$	$\begin{array}{r} 88022\\ 87855\\ 87833\\ 87957\\ 10125\\ 98862\\ 10162\\ 98662\\ 10189\\ 87747\\ 881186\\ 89186\\ 80112260\\ 87747\\ 88118\\ 89186\\ 80112260\\ 87747\\ 88011\\ 88011\\ 87366\\ 8795\\ 88013\\ 10132\\ 88041\\ 880132\\ 10132\\ 88042\\ 880132\\ 10132\\ 88042\\ 88042\\ 88055\\ 88075\\ 10266\\ 87740\\ 880255\\ 88075\\ 10266\\ 87740\\ 87740\\ 880255\\ 88075\\ 10032\\ 88042\\ 880255\\ 88075\\ 99261\\ 10266\\ 88042\\ 88033\\ 87766\\ 9926\\ 10266\\ 88016\\ 87740\\ 880255\\ 88075\\ 9924\\ 88010\\ 88038\\ 88010\\ 88010\\ 887740\\ 88025\\ 88075\\ 9924\\ 88025\\ 8805\\ 8805\\ 8805\\ 8805\\ 87740\\ 8805$	$\begin{array}{r} 343\\ 2818\\ 2828\\ 2818\\ $	$\begin{array}{r} -87528\\ -87528\\ -87528\\ -87528\\ -87528\\ -9727\\ -97263\\ -9727\\ -9763\\ -9764\\ -9764\\ -9764\\ -9765\\ -9723\\ -9765\\ -9723\\ -9765\\ -97723\\ -9765\\ -97723\\ -9765\\ -9765\\ -97723\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -97723\\ -9765\\ -9765\\ -97723\\ -9765\\ -9765\\ -97723\\ -9765\\ -9765\\ -97723\\ -9765\\ -97723\\ -9765\\ -97723\\ -9765\\ -97723\\ -9765\\ -97723\\ -9765\\ -97723\\ -97723\\ -97765\\ -97723\\ -97765\\ -97723\\ -97765\\ -97724\\ -97765\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97722\\ -97723\\ -9765\\ -9765\\ -9765\\ -97722\\ -97722\\ -97722\\ -97723\\ -9765\\ -9765\\ -97723\\ -9766\\ -9765\\ -97722\\ -97722\\ -97723\\ -97722\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -97722\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -9766\\ -9765\\ -97723\\ -977$	$\begin{array}{c} 87.55\\ 87.55\\ 87.55\\ 99.7\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 88.7\\ 99.9\\ 99.7\\ 99.7\\ 77.7\\ 88.8\\ 88.7\\ 99.9\\ 99.7\\ 77.7\\ 78.8\\ 88.8\\ 88.7\\ 99.9\\ 99.7\\ 77.7\\ 78.8\\ 88.8\\ 88.7\\ 99.9\\ 99.7\\ 77.7\\ 78.8\\ 88.7\\ 99.9\\ 99.7\\ 77.7\\ 78.8\\ 88.8\\ 88.7\\ 99.9\\ 99.7\\ 77.7\\ 78.8\\ 88.8\\ 88.7\\ 99.9\\ 99$	$\begin{array}{c} 194\\ 194\\ 295\\ 297\\ 3520\\ 3520\\ 3520\\ 3520\\ 3520\\ 3520\\ 3520\\ 3520\\ 4520\\ 3520\\ 4520\\ 3520\\ 4520$ 4520\\ 4520 4520\\ 4520\\ 4520\\ 4520 4520 45200\\ 4520 4520 4520 4520 45	5577887755880022332200111882221111166111887722244116622266883559922336677332221111188999113339955998811155111111111111	$\begin{array}{c} 301\\ 130\\ 59\\ 135\\ 48\\ -191\\ 92\\ 277\\ 48\\ -192\\ 2278\\ -67\\ -79\\ 284\\ 225\\ -67\\ -79\\ 284\\ 225\\ -67\\ -750\\ -334\\ -733\\ -334\\ -739\\ -376\\ -334\\ -750\\ -334\\ -750\\ -334\\ -750\\ -334\\ -750\\ -334\\ -750\\ -334\\ -750\\ -336\\ -334\\ -110\\ -265\\ -764\\ -120\\ -265\\ -345\\ -264\\ -256\\ -345\\ -264\\ -256\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -36\\ -205\\ -205\\ -36\\ -205$	$\begin{array}{c} 354\\ 295\\ 308\\ 295\\ 308\\ 1197\\ 3080\\ 3559\\ 2606\\ 2131\\ 2259\\ 2606\\ 2131\\ 2259\\ 2666\\ 3265\\ 3269\\ 2159\\ 2259\\ 2250\\ 2266\\ 3265\\ 3269\\ 2272\\ 2959\\ 1245\\ 2253\\ 2265\\ 2272\\ 2269\\ 2267\\ 2269\\ 2262\\ 22406\\ 2240\\ 224$	$\begin{array}{c} 0.00\\$	UPLLBB UUPPLBB UUPPLBB UUPPLBB UUPPLBB UUPPLBB UUPPLBBB UUPPLBBB UUPPLBBBB UUPPLBBBBBBBBBB

Nrun	T [ns]	D [ns]	P [W]	B [Gauss]	$\theta_{\rm pol} \ [\rm deg.]$	$\frac{\nu_{\rm fit}}{\nu_{\rm fit}}$ [Hz]	$\Delta \nu_{\rm fit}  [\rm Hz]$	DCB [Hz]	DCB [Hz]	SC [Hz]	ASC [Hz]	[Hz]	$\Delta \nu_0  [\mathrm{Hz}]$	wts. [%]	] Data Type
$\begin{array}{c} 1646\\ 1647\\ 1648\\ 1649\\ 1647\\ 1648\\ 1649\\ 1651\\ 1652\\ 1653\\ 1655\\ 1656\\ 1656\\ 1665\\ 1665\\ 1665\\ 1665\\ 1665\\ 1665\\ 16661\\ 1666\\ 1666\\ 1666\\ 1666\\ 1666\\ 1667\\ 1667\\ 1667\\ 1678\\ 1679\\ 1678\\ 1679\\ 1678\\ 1679\\ 1678\\ 1679\\ 1682\\ 1683\\ 1682\\ 1683\\ 1687\\ 1687\\ 1678\\ 1678\\ 1679\\ 1678\\ 1679\\ 1678\\ 1679\\ 1678\\ 1679\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1678\\ 1682\\ 1683\\ 1682\\ 1683\\ 1682\\ 1683\\ 1682\\ 1683\\ 1682\\ 1683\\ 1682\\ 1683\\ 1682\\ 1683\\ 1686\\ 1687\\ 1678$	$\begin{array}{c} 4000\\ 4000\\ 3000\\ 4000\\ 4000\\ 4000\\ 3000\\ 3000\\ 3000\\ 3000\\ 3000\\ 3000\\ 4000\\ 3000\\$	$\begin{array}{c} 1000\\$	$\begin{array}{c} 52.5\\$	$\begin{array}{c} 4,762\\ 4,$	$\begin{array}{c} 1700\\ 1770\\$	$\begin{array}{l} 100892\\ 100842\\ 100111\\ 100161\\$	$\begin{array}{l} 1888\\ 2054\\ 1962\\ 2054\\ 1962\\ 2054\\ 1962\\ 2054\\ 1962\\ 2054\\ 1962\\ 2054\\ 1972\\ 1972\\ 2180\\ 2578\\ 1995\\ 1252\\ 2491\\ 2578\\ 1995\\ 1252\\ 2491\\ 2252\\ 2491\\ 2252\\ 2491\\ 2252\\ 2492\\ 218\\ 2255\\ 2491\\ 2262\\ 2212\\ 2282\\ 2212\\ 2282\\ 2212\\ 2282\\ 2292\\ 2188\\ 2422\\ 2179\\ 2315\\ 2422\\ 2179\\ 2315\\ 2422\\ 2179\\ 2315\\ 2422\\ 2179\\ 2315\\ 2422\\ 2179\\ 2315\\ 2422\\ 218\\ 2422\\ 2179\\ 2315\\ 2422\\ 218\\ 2422\\ 2179\\ 2339\\ 3383\\ 454\\ 454\\ 811\\ 5557\\ 6563\\ 366\\ 887\\ 66\\ 881\\ 668\\ 876\\ 688\\ 876\\ 881\\ 110\\ 876\\ 881\\ 110\\ 886\\ 876\\ 881\\ 110\\ 886\\ 886\\ 876\\ 881\\ 110\\ 886\\ 886\\ 886\\ 886\\ 886\\ 886\\ 886\\ 88$	$\begin{array}{r} -9766\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9765\\ -9766\\ -9765\\ -9766\\ -9765\\ -9766\\ -9762\\ -9772\\ -9772\\ -9772\\ -9772\\ -9776\\ -9766\\ -9761\\ -9772\\ -9772\\ -9776\\ -9766\\ -9761\\ -9772\\ -9776\\ -9766\\ -9766\\ -9762\\ -9772\\ -9772\\ -9776\\ -9766\\ -9766\\ -9762\\ -9772\\ -9772\\ -9776\\ -9766\\ -9766\\ -9762\\ -9772\\ -9772\\ -9776\\ -9766\\ -9766\\ -9766\\ -9762\\ -9772\\ -9772\\ -9776\\ -9766\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9776\\ -9766\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9772\\ -9772\\ -9776\\ -9766\\ -9766\\ -9766\\ -9766\\ -9766\\ -9766\\ -9766\\ -9762\\ -9722\\ -9772\\ -9772\\ -9772\\ -9772\\ -9776\\ -9766\\ -9$	$\begin{array}{c} 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\ 9.8\\$	$\begin{array}{c} 2581\\ 2991\\ 2105\\ 2399\\ 3422\\ 494\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 4946\\ 3882\\ 2409\\ 1881\\ 180\\ 1402\\ 2409\\ 1402\\ 1020\\ 1409\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 1882\\ 2992\\ 2414\\ 400\\ 2411\\ 3554\\ 444\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13524\\ 4446\\ 900\\ 2411\\ 13526\\ 4466\\ 35\\ 4471\\ 1448\\ 897\\ 4471\\ 1061\\ 520\\ 846\\ 35\\ 466\\$	667733668866229955777222244667773344332233223322387744444444444444444	$\begin{smallmatrix} 656\\ 549\\ 2719\\ 486\\ -1319\\ -2021\\ -577\\ -3052\\ -1186\\ -757\\ -2162\\ -1757\\ -2162\\ -757\\ -2162\\ -757\\ -2162\\ -773\\ -2162\\ -773\\ -2162\\ -773\\ -2162\\ -773\\ -2162\\ -773\\ -2162\\ -773\\ -2162\\ -773\\ -298\\ -2$	$\begin{array}{c} 1888\\ 2055\\ 1972\\ 1990\\ 1848\\ 1723\\ 1990\\ 1848\\ 2055\\ 1972\\ 1990\\ 1848\\ 1783\\ 1831\\ 2678\\ 2242\\ 1992\\ 2219\\ 12221\\ 1885\\ 1992\\ 2242\\ 1997\\ 2315\\ 1123\\ 1976\\ 3339\\ 1685\\ 5766\\ 812\\ 8768\\ 769\\ 2842\\ 8768\\ 769\\ 584\\ 287\\ 687\\ 687\\ 687\\ 687\\ 687\\ 687\\ 687\\ 6$	$\begin{array}{c} 0.00\\$	UUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUUU

E	ns]	[su	[M	Gauss]	1 [deg.]	[Hz]	fit [Hz]	B [Hz]	C <sub>B</sub> [Hz]	[Hz]	C [Hz]	[Hz]	[Hz] [	. [%]	ta Type
$N_{\rm rt}$	T	D [	Ρ[	B [	$\theta_{\mathrm{po}}$	νĥt	$\Delta \nu_{i}$	DC	ΔD	SC	ΔS	$\nu_0$	$\Delta  u_0$	wts	Dat
$\begin{array}{l} 17423\\ 17443\\ 17445\\ 17446\\ 17447\\ 17448\\ 17551\\ 17552\\ 17552\\ 17557\\ 17559\\ 17661\\ 17652\\ 17557\\ 17557\\ 17559\\ 17661\\ 17662\\ 17662\\ 17662\\ 17662\\ 17662\\ 17662\\ 17662\\ 17662\\ 1777\\ 17784\\ 17782\\ 17778\\ 17784\\ 17782\\ 17778\\ 17784\\ 17782\\ 17778\\ 17799\\ 17791\\ 17784\\ 17782\\ 17778\\ 17799\\ 17791\\ 17793\\ 17792\\ 17797\\ 17799\\ 18012\\ 18034\\ 180$	$\begin{array}{c} 3000\\ 3000\\ 4000\\ 5000\\$	$\begin{array}{c} 100\\ 100\\ 50\\ 100\\ 50\\ 125\\ 50\\ 50\\ 125\\ 50\\ 125\\ 50\\ 125\\ 50\\ 125\\ 50\\ 125\\ 50\\ 125\\ 50\\ 125\\ 50\\ 100\\ 125\\ 50\\ 100\\ 125\\ 50\\ 100\\ 125\\ 50\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{smallmatrix} 155\\ 300\\ 72.5\\ 6300\\ 27.1555555555555555555555555555555555555$	$\begin{array}{c} -5, 1992\\ -9, 762\\ -9, 762\\ -9, 762\\ -9, 9921\\ -3, 811\\ -9, 762\\ -9, 9921\\ -3, 811\\ -9, 762\\ -9, 9921\\ -3, 811\\ -5, 159\\ -7, 622\\ -3, 811\\ -5, 159\\ -7, 622\\ -3, 811\\ -5, 159\\ -5, 159\\ -9, 762\\ -3, 811\\ -3, 811\\ -3, 811\\ -3, 811\\ -5, 1599\\ -5, 066\\ $	1700 - 1700 -	$\begin{array}{l} 11326\\ 111226\\ 111270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11270\\ 11295\\ $	$\begin{array}{c} 105\\ 105\\ 107\\ 117\\ 108\\ 107\\ 117\\ 108\\ 107\\ 117\\ 108\\ 107\\ 117\\ 108\\ 107\\ 112\\ 108\\ 107\\ 108\\ 108\\ 107\\ 108\\ 108\\ 107\\ 108\\ 108\\ 107\\ 108\\ 108\\ 107\\ 108\\ 108\\ 107\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108$	$\begin{array}{c} -11466\\ -40943\\ -11056\\ -40943\\ -11056\\ -40945\\ -42351\\ -40945\\ -42351\\ -40945\\ -24993\\ -42351\\ -42351\\ -4298\\ -24993\\ -42351\\ -6241\\ -11466\\ -25021\\ -9775\\ -9775\\ -9775\\ -9775\\ -9777\\ -409412\\ -9775\\ -9775\\ -9777\\ -11038\\ -9775\\ -9772\\ -97$	$ 10.9 \\ 11.1.4 \\ 40.9 \\ 12.4 \\ 6.2.4 \\ 40.9 \\ 42.4 \\ 40.2 \\ 42.4 \\ 40.2 \\ 52.8 \\ 42.4 \\ 11.2 \\ 52.8 \\ 9.9 \\ 9.8.4 \\ 40.1 \\ 52.2 \\ 39.9 \\ 40.1 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 52.3 \\ 40.1 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 52.2 \\ 42.4 \\ 11.1 \\ 12.5 \\ 42.1 \\ 11.1 \\ 12.5 \\ 42.1 \\ 11.1 \\ 12.5 \\ 42.1 \\ 11.1 \\ 12.5 \\ 42.1 \\ 11.1 \\ 11.5 \\ 11.5 \\ 82.3 \\ 11.1 \\ 11.1 \\ 12.3 \\ 22.5 \\ 11.1 \\ 11.5 \\ 11.5 \\ 82.3 \\ 11.1 \\ 11.1 \\ 11.2 \\ 22.2 \\ 11.1 \\ 11.1 \\ 12.3 \\ 22.5 \\ 11.1 \\ 11.1 \\ 12.3 \\ 12.3 \\ 11.1 \\ 11.1 \\ 12.3 \\ 12.3 \\ 11.1 \\ 11.1 \\ 12.3 \\ 12.3 \\ 11.1 \\ 12.3 \\ 12.3 \\ 11.1 \\ 12.3 \\ 1$	$\substack{80\\1459\\2289\\7765}{438976} + \substack{72\\2299\\15765}{438976} + \substack{72\\2299\\15765}{438976} + \substack{72\\2299}{15765} + \substack{72\\2299}{15762} + \substack{72\\299}{15762} + \substack{72\\299}{15$	2832515115913729206501193766133211193822365354481924393305572113913486116026789111766210548716244739985397388111123822365354481322311112382236535448132231111238231111123823111112382311111238231111123823111123823111112382311111111	$\begin{array}{c} -292\\ -222\\ -228\\ -228\\ -228\\ -228\\ -228\\ -236\\ -296\\ -1625\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -518\\ -294\\ -9-6\\ -1625\\ -294\\ -9-6\\ -94\\ -94\\ -235\\ -282\\ -236\\ -282\\ -282\\ -236\\ -282\\$	$\begin{smallmatrix} 1072\\1071\\1778\\1459\\1587\\1032\\1383\\1201\\1895\\2966\\9829\\2966\\9829\\2966\\9829\\2966\\1003\\1820\\118\\9926\\217\\227\\217\\227\\217\\2270\\217\\2270\\217\\2270\\2270$	$\begin{array}{c} 0.204\\ 0.$	KRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\underset{N}{\operatorname{unr}_{N}} \underbrace{ \begin{array}{c} & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & $	$\begin{bmatrix} \mathrm{sul} \\ \mathrm{sul} \end{bmatrix} . I = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 &$	$\begin{bmatrix} M \end{bmatrix} \begin{array}{c} d \\ 0 \\ 1822555 \\ 500 \\ 1512555 \\ 605 \\ 22305 \\ 227555 \\ 300 \\ 22755 \\ 5525 \\ 3755 \\ 5555 \\ 3755 \\ 5555 \\ 5555 \\ 3755 \\ 5555 \\ 5555 \\ 3755 \\ 5555 \\ 3755 \\ 5555 \\ 37$	B [Gauss] B [Gau	θ <sup>pol</sup> [deg.]	$\begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix}^{1 \mathbf{H}_{\mathcal{A}}} \\ \begin{array}{c} \mathbf{z} 2 2 1 0 0 0 \\ 1 1 1 2 0 2 2 0 1 0 \\ 1 2 2 0 2 0 1 \\ 1 2 0 2 2 0 1 \\ 1 2 2 2 2 0 0 0 \\ 1 1 2 2 2 2 0 0 0 \\ 1 1 2 2 2 2 0 0 0 \\ 1 1 2 2 2 2 0 0 0 \\ 1 1 2 2 3 2 3 0 3 0 0 \\ 1 1 2 2 3 2 3 0 1 \\ 4 2 2 2 3 9 3 3 0 \\ 1 1 1 2 3 2 3 6 4 \\ 1 1 2 2 3 2 3 1 \\ 1 1 2 3 2 3 1 \\ 1 1 2 3 2 3 2 3 1 \\ 1 1 2 3 2 3 2 3 2 3 2 3 1 \\ 1 1 2 3 2 3 2 3 2 3 2 3 1 \\ 1 2 2 3 2 3 2 3 2 3 2 3 2 3 2 3 2 3 2 3 2 3 2 3 3 3 2 3 3 3 3 3 3 3 3$	$\begin{bmatrix} r_{\rm H} \\ 1900 \\ r_{\rm H} \end{bmatrix} \xrightarrow{\rm tH} 1046 \\ 8011 \\ 1046 \\ 1046 \\ 1046 \\ 1046 \\ 1046 \\ 1046 \\ 1046 \\ 1090 \\ 909 \\ 91455 \\ 7972 \\ 2994 \\ 1464 \\ 7400 \\ 1841 $	[ <sup>Z</sup> H] <sup>B</sup> OG 219684 -2198673 -2198674 -2198673 -2389951 -4233480 -2298975 -2298977 -2298977 -229807 -2	$\begin{smallmatrix} \mathbf{z}_{\mathbf{z}_{1}} \\ \mathbf{z}_{2} \\ \mathbf{z}_{1} \\ \mathbf{z}_{2} \\ $	$ \begin{smallmatrix} [\mathbf{z}\mathbf{H}] \\ \mathbf{OS} \\ \hline \\ & \begin{array}{c} 2628 \\ 22551 \\ 4999 \\ 4605 \\ 1982 \\ 2645 \\ 22144 \\ 82214 \\ 1679 \\ 21448 \\ 2244 \\ 2244 \\ 2244 \\ 2244 \\ 2244 \\ 2844 \\ 275 \\ 75 \\ \end{array} } $	$\begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \mathbf{OSV} \\ 5 \overset{6}{5} \overset{6}{11199230244753263524179751} \\ 5 \overset{6}{1179230244179751} \\ 5 \overset{6}{1179751} \\ 5 6$	[zH] 07 -1293-4-324 -2244 -22460 -22460 -2383 -13104 -2804 -2704 -2804 -2704 -2804 -2704 -2804 -2704 -2804 -2704 -2804 -2704 -2804 -2704 -2804 -270 -2704 -2	$ \begin{bmatrix} \mathbf{z}\mathbf{H} \end{bmatrix} \begin{array}{ c c c c c c c c c c c c c c c c c c c$	00000000000000000000000000000000000000	
1901 400 50 67.5 9.524 260 39186 93 -38995 39 111 22 80 103 0.00	$\begin{array}{c} 1865 & 4\\ 18666 & 4\\ 18678 & 3\\ 18670 & 3\\ 1871 & 4\\ 1871 & 4\\ 1872 & 4\\ 1872 & 4\\ 1873 & 4\\ 1874 & 4\\ 1876 & 3\\ 18778 & 3\\ 18778 & 3\\ 18778 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18876 & 3\\ 18890 & 4\\ 18878 & 3\\ 18890 & 3\\ 18891 & 3\\ 18891 & 3\\ 18891 & 3\\ 18891 & 3\\ 18892 & 4\\ 18892 & 4\\ 18894 & 4\\ 18894 & 4\\ 18895 & 4\\ 18896 & 4\\ 18896 & 4\\ 18898 & 3\\ 18898 & 4\\ 18894 & 4\\ 18896 & 4\\ 18898 & 4\\ 18888 & 4\\ 1$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{r} -9.524\\ 9.521\\ 9.921\\ 5.159\\ -9.921\\ 5.506\\ 5.159\\ 9.524\\ -9.524\\ 5.159\\ 9.524\\ -5.159\\ 9.524\\ -5.159\\ 9.921\\ -5.159\\ 9.921\\ -5.159\\ -9.524\\ -5.159\\ 9.921\\ -5.159\\ -5.159\\ 9.921\\ -5.159\\ -9.524\\ 9.924\\ -5.159\\ -9.524\\ 9.921\\ -9.524\\ 9.524\\ -5.066\\ -9.921\\ -5.066\\ -9.921\\ -5.066\\ -9.524\\ 9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -9.524\\ -5.066\\ -5.566\\ $	$\begin{array}{c} 2600\\ 200\\ 2$	$\begin{array}{r} 38783\\ 39076\\ 42252\\ 417722\\ 42512\\ 11112\\ 11811\\ 10833\\ 39491\\ 38585\\ 11510\\ 38585\\ 11510\\ 38585\\ 11808\\ 38999\\ 116666\\ 42047\\ 422149\\ 42067\\ 22149\\ 42572\\ 22125\\ 11736\\ 42995\\ 22125\\ 11736\\ 42995\\ 221222\\ 114456\\ 119290\\ 39121\\ 1192203\\ 39128\\ 39128\\ 39158\\ 11130\\ 39128\\ 39158\\ 39158\\ 39158\\ 39158\\ 39158\\ 39158\\ 39186\\ 39188\\ 39186\\ 3$	$\begin{array}{c} 141\\ 293\\ 139\\ 104\\ 130\\ 181\\ 64\\ 401\\ 124\\ 177\\ 109\\ 191\\ 97\\ 73\\ 68\\ 94\\ 997\\ 75\\ 68\\ 997\\ 77\\ 68\\ 997\\ 7141\\ 136\\ 68\\ 997\\ 741\\ 137\\ 247\\ 124\\ 81\\ 221\\ 293\\ \end{array}$	$\begin{array}{r} -88970\\ -38996\\ -42348\\ -11482\\ -42348\\ -11482\\ -11040\\ -11054\\ -38970\\ -11483\\ -389970\\ -11483\\ -389970\\ -11483\\ -389970\\ -11483\\ -42348\\ -42348\\ -42348\\ -42348\\ -42348\\ -42348\\ -11041\\ -42347\\ -11468\\ -11468\\ -11468\\ -38968\\ -219867\\ -11483\\ -11468\\ -38968\\ -219867\\ -11483\\ -11468\\ -38968\\ -219867\\ -11468\\ -38968\\ -219867\\ -11468\\ -38968\\ -219867\\ -11468\\ -38968\\ -219867\\ -11468\\ -38968\\ -11040\\ -42319\\ -38968\\ -38999\\ -1054\\ -38968\\ -38999\\ -3898\\ -3899\\ -3898\\ -3899\\ -3899\\ -3898\\ -3899\\ -3899\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3899\\ -3898\\ -3$	$\begin{array}{c} 39\\ 39\\ 39\\ 42.3\\ 11.5\\ 42.3\\ 11.1\\ 11.1\\ 11.1\\ 39\\ 11.5\\ 39\\ 11.5\\ 39\\ 212\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 11.5\\ 39\\ 39\\ 11.1\\ 12.3\\ 39\\ 39\\ 39\\ 39\\ 39\\ 39\\ 39\\ 39\\ 39\\ 3$	$\begin{array}{c} 58\\ 9\\ 933\\ 111\\ 67\\ 3901\\ 9\\ 70\\ 41\\ 338\\ 589\\ 111\\ 338\\ 589\\ 111\\ 152\\ 1820\\ 61\\ 1339\\ 2389\\ 2441\\ 113\\ 2089\\ 2384\\ 147\\ 198\\ 2441\\ 198\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 198\\ 2289\\ 2441\\ 102\\ 202\\ 201\\ 211\\ 2266\\ 210\\ 211\\ 211\\ 2266\\ 211\\ 211\\ 2266\\ 211\\ 211$	$11\\218\\322\\9\\1\\24\\11\\229\\31\\4\\1239\\222\\422\\61\\159514\\62\\2554\\4\\22\\554\\4\\22$	$\begin{array}{c} -245\\ -189\\ 82\\ -622\\ -513\\ -252\\ -513\\ -14\\ -14\\ -25\\ -513\\ -252\\ -513\\ -14\\ -14\\ -14\\ -2\\ -52\\ -513\\ -109\\ -310\\ -786\\ -499\\ -310\\ -786\\ -499\\ -310\\ -786\\ -499\\ -310\\ -786\\ -499\\ -310\\ -127\\ -513\\ -122\\ -27\\ -161\\ -128\\ -280\\$	$\begin{array}{c} 1476\\ 2496\\ 1474\\ 1388\\ 1659\\ 4031\\ 1773\\ 1302\\$	$\begin{array}{c} 0.00\\ 0.00\\ 0.00\\ 0.20\\ 0.20\\ 0.20\\ 0.10\\ 0.13\\ 0.00\\ 0.13\\ 0.00\\ 0.13\\ 0.00\\ 0.13\\ 0.00\\ 0.13\\ 0.00\\ 0.13\\ 0.00\\$	

Table	A.2	Continued	from	previous	page
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$r_{ m run}$	[us]	[us]	[M]	f [Gauss]	pol [deg.]	fit [Hz]	whit [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	0 [Hz]	170 [Hz]	ts. [%]	ata Type
$\begin{array}{c} 1938\\ 1939\\ 1940\\ 1941\\ 1942\\ 1944\\ 1944\\ 1944\\ 1945\\ 1947\\ 1945\\ 1952\\ 1952\\ 1955\\ 1955\\ 1955\\ 1955\\ 1956\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1966\\ 1970\\ 1972\\ 1974\\ 1976\\ 1978\\ 1980\\ 1997\\ 1978\\ 1980\\ 19960\\ 1970\\ 1972\\ 1976\\ 1978\\ 1980\\ 19960\\ 1997\\ 19980\\ 19960\\ 1997\\ 19980\\ 19960\\ 1997\\ 19980\\ 19980\\ 19900\\ 1997\\ 1988\\ 1988\\ 1988\\ 1998\\ 19900\\ 1992\\ 20000\\ 20000\\ 20005\\ 20007\\ 20009\\ 20001\\ 20003\\ 20005\\ 20007\\ 20009\\ 20011\\ 20013\\ 2005\\ 20007\\ 20090\\ 20011\\ 20013\\ 2005\\ 20007\\ 20090\\ 20011\\ 20013\\ 2005\\ 2007\\ 20090\\ 20011\\ 2002\\ 2002\\ 2002\\ 2002\\ 2003\\ 200$	800           700           700	$\begin{array}{c} 1 \\ 100 \\ 1$	$\begin{array}{c} 60\\ 60\\ 60\\ 60\\ 60\\ 60\\ 60\\ 60\\ 60\\ 60\\$	$\begin{array}{c} .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ .\\ $	$\begin{array}{c} 3 \\ 3 \\ 260 \\ 170 \\ 260 \\ $	$\begin{array}{c} 9824\\ 9824\\ 9831\\ 10217\\ 9973\\ 10606\\ 10493\\ 9773\\ 10606\\ 10493\\ 9773\\ 10301\\ 10301\\ 10301\\ 1033\\ 10130\\ 10130\\ 1023\\ 9873\\ 9987\\ 9987\\ 9986\\ 9977\\ 9987\\ 9986\\ 99986\\ 99986\\ 99986\\ 99986\\ 10046\\ 9715\\ 10025\\ 9986\\ 10025\\ 9986\\ 10025\\ 9986\\ 10025\\ 9986\\ 99965\\ 10025\\ 9950\\ 10032\\ 99374\\ 9953\\ 10032\\ 10032\\ 10035\\ 10035\\ 9966\\ 9396\\ 99965\\ 99973\\ 99374\\ 99374\\ 99374\\ 99374\\ 99374\\ 99374\\ 99374\\ 99374\\ 9939\\ 9939\\ 993$	$\begin{array}{c} & & \\ &$	$\begin{array}{c} - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - $	9.958 9.9599 9.959 9.959 9.959 9.959 9.959 9.959 9.959 9.959 9.959 9.959	$\begin{array}{c} \\ 155\\ 1554\\ 154\\ 154\\ 155\\ 1552\\ 1554\\ 155\\ 1552\\ 1552\\ 1554\\ 1555\\ 1766\\ 1765\\ 1775$	$\begin{smallmatrix} 4&4&4&4&4&4&4&4&4&4&4&4&4&4&4&4&4&4&4&$	$\begin{array}{c} - \\ - & 1000 \\ - & 295 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 573 \\ - & 171 \\ - & 354 \\ - & 267 \\ - & 201 \\ - & 201 \\ - & 201 \\ - & 202 \\ - & $	$\begin{array}{c} 17\\ 3720\\ 3341\\ 3720\\ 3343\\ 3439\\ 2721\\ 2724\\ 2722\\ 2724\\ 2724\\ 2722\\ 2724\\ 2724\\ 2722\\ 2724\\ 2724\\ 2722\\ 2724\\ 2724\\ 2722\\ 2724\\ 2724\\ 2722\\ 2724$ 2724\\ 2724 2724\\ 2724 2724\\ 2724 2724 2724 2724 2	$\begin{array}{c} 0.07\\ 0.02\\ 0.05\\ 0.03\\ 0.02\\ 0.05\\ 0.02\\ 0.002\\ 0.002\\ 0.002\\ 0.002\\ 0.002\\ 0.002\\ 0.005\\ 0.005\\ 0.018\\ 0.029\\ 0.005\\ 0.018\\ 0.009\\ 0.001\\ 0.010\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.011\\ 0.02\\ 0.000\\ 0.0$	NNRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRRR

Table A.2 Continued from previous page

$I_{run}$	[ns]	[su] (	[M]	3 [Gauss]	pol [deg.]	fit [Hz]	₩ <sup>hft</sup> [Hz]	DC <sub>B</sub> [Hz]	ADC <sub>B</sub> [Hz]	C [Hz]	NSC [Hz]	0 [Hz]	$\nu_0  [\mathrm{Hz}]$	ts. [%]	lata Type
$\begin{array}{c} 2036\\ 2037\\ 2038\\ 2039\\ 2041\\ 2043\\ 20442\\ 20443\\ 20442\\ 20443\\ 2045\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2055\\ 2056\\ 2066\\ 2066\\ 2066\\ 2066\\ 2066\\ 2067\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2077\\ 2078\\ 2088\\ 2099\\ 2091\\ 2093\\ 2093\\ 2095\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2099\\ 2097\\ 2098\\ 2095\\ 2097\\ 2099\\ 2097\\ 2098\\ 2098\\ 2095\\ 2097\\ 2099\\ 2101\\ 2103\\ 2103\\ 2106\\ 2107\\ 2108\\ 2$	300           300	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 74.25\\ 74$	$\begin{array}{c} 4,762\\ -4,762\\ $	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 10324\\ 10287\\ 10339\\ 10338\\ 10193\\ 10135\\ 10291\\ 10087\\ 10187\\ 10187\\ 10291\\ 10087\\ 10210\\ 10276\\ 10263\\ 10223\\ 10276\\ 10263\\ 10$	$\begin{array}{c} 103\\85\\81\\86\\85\\86\\86\\86\\86\\86\\86\\86\\86\\86\\86\\86\\86\\86\\$	-9771 -9763 -9774 -9763 -97763 -97763 -97763 -97763 -97764 -97764 -97774 -97764 -97764 -97773 -97763 -97763 -97763 -97763 -97763 -97763 -97773 -97763 -97773 -97763 -97773 -97763 -97773 -97763 -97773 -97763 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97763 -97763 -97763 -97763 -97773 -97763 -97762 -9763 -9762 -9763 -9762 -9763 -97762 -9763 -97762 -9763 -97762 -9763 -97762 -97763 -97762 -97763 -97762 -97763 -97762 -97763 -97763 -97762 -97763 -97763 -97762 -97763 -97762 -97763 -97762 -97763 -97763 -97762 -97763 -97762 -97763 -97762 -97763 -97772 -97763 -97763 -97772 -97763 -97763 -97763 -97763 -97763 -97763	9.88 9.88 9.88 9.88 9.88 9.88 9.88 9.88	$\begin{array}{c} 504\\ 504\\ 505\\ 505\\ 505\\ 505\\ 505\\ 505\\$	$\begin{array}{c} 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\$	$\begin{array}{c} 48\\ 200\\ 81\\ -75\\ -1537\\ 14\\ -84\\ 12\\ 255\\ -86\\ -33\\ -18\\ 32\\ 255\\ -86\\ -339\\ -28\\ -28\\ -37\\ -29\\ -265\\ -339\\ -28\\ -265\\ -339\\ -28\\ -265\\ -339\\ -28\\ -265\\ -339\\ -28\\ -265\\ -346\\ -28\\ -265\\ -346\\ -448\\ -294\\ -20\\ -20\\ -20\\ -20\\ -20\\ -20\\ -20\\ -20$	$\begin{array}{c} 104\\ 877\\ 878\\ 879\\ 899\\ 844\\ 865\\ 865\\ 875\\ 100\\ 875\\ 100\\ 875\\ 875\\ 100\\ 875\\ 875\\ 100\\ 875\\ 875\\ 100\\ 875\\ 875\\ 100\\ 875\\ 875\\ 875\\ 100\\ 875\\ 875\\ 875\\ 875\\ 875\\ 875\\ 875\\ 875$	$\begin{array}{c} 0.00\\$	NR NR NR NR NR NR NR NR NR NR NR NR NR N

g	us]	ns]	[M	Gauss]	[deg.]	[Hz]	<sub>ft</sub> [Hz]	B [Hz]	C <sub>B</sub> [Hz]	[Hz]	C [Hz]	[Hz]	[Hz] (	[%] .	a Type
$N_{\rm rt}$	T	D [	Ρ.	B	$\theta_{\mathrm{po}}$	νfit	$\Delta \nu_j$	DC	ΔD	SC	Δs	01	$\Delta  u_0$	wts	Dat
$\begin{array}{c} 2134\\ 2135\\ 2137\\ 2136\\ 2137\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2138\\ 2142\\ 2142\\ 2142\\ 2142\\ 2142\\ 2142\\ 2142\\ 2142\\ 2145\\ 2152\\ 2155\\ 2255\\$	300         300           300	$\begin{array}{c} 1000\\$	$\begin{array}{c} 74.255\\$	$\begin{array}{c} -4,762\\ 4,762\\ 4,762\\ 4,762\\ -4$	260 260 260 260 260 260 260 260	$\begin{array}{l} 103014\\ 10672\\ 10672\\ 10672\\ 11269\\ 9272\\ 9724\\ 9724\\ 100065\\ 9726\\ 9726\\ 9972\\ 9972\\ 9972\\ 9972\\ 9972\\ 9972\\ 9972\\ 9972\\ 9972\\ 9992\\ 10566\\ 11327\\ 9992\\ 10562\\ 10047\\ 10209\\ 9981\\ 10047\\ 10434\\ 10221\\ 10434\\ 10221\\ 10434\\ 10221\\ 10434\\ 10221\\ 10433\\ 10437\\ 10055\\ 10205\\ 10006\\ 10016\\ 10006\\ 10016\\ 10006\\ 100161\\ 10035\\ 10047\\ 10035\\ 10047\\ 10035\\ 10047\\ 10035\\ 10047\\ 10035\\ 10046\\ 100161\\ 10035\\ 10046\\ 100161\\ 10035\\ 10205\\ 10205\\ 10025\\ 10205\\ 10006\\ 10015\\ 10035\\ 10205\\ 10205\\ 10035\\ 10205\\ 10035\\ 10205\\ 10036\\ 10035\\ 10205\\ 10036\\ 10006\\ 10005\\ 10006\\ 10005\\ 10006\\ 10005\\ 10006\\ 10005\\ 10006\\ 10005\\ 10006\\ 10000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 100000\\ 10000\\$	$\begin{array}{c} 4317\\ 4366\\ 33601\\ 4495\\ 4305\\ 4412\\ 4011\\ 43336\\ 452\\ 4305\\ 4305\\ 452\\ 4305\\ 4305\\ 452\\ 4305\\ 4014\\ 4305\\ 4014\\ 403\\ 336\\ 404\\ 403\\ 336\\ 404\\ 404\\ 337\\ 401\\ 401\\ 402\\ 3361\\ 404\\ 402\\ 3373\\ 4741\\ 401\\ 402\\ 3373\\ 4741\\ 401\\ 402\\ 3373\\ 4741\\ 401\\ 402\\ 3373\\ 4741\\ 401\\ 402\\ 3373\\ 4741\\ 401\\ 402\\ 3361\\ 404\\ 402\\ 3373\\ 477\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 4363\\ 3391\\ 424\\ 4778\\ 514\\ 436\\ 3391\\ 426\\ 4771\\ 514\\ 436\\ 3391\\ 426\\ 477\\ 514\\ 436\\ 3391\\ 426\\ 833\\ 8907\\ 775\\ 914\\ 883\\ 905\\ 101\\ 913\\ 280\\ 280\\ 330\\ 406\\ 775\\ 914\\ 436\\ 883\\ 905\\ 101\\ 913\\ 280\\ 330\\ 406\\ 775\\ 914\\ 883\\ 905\\ 101\\ 913\\ 280\\ 330\\ 406\\ 775\\ 914\\ 883\\ 905\\ 101\\ 913\\ 280\\ 330\\ 406\\ 775\\ 914\\ 883\\ 905\\ 101\\ 913\\ 280\\ 300\\ 80\\ 100\\ 80\\ 100\\ 100\\ 100\\ 100\\ 100$	-9762 -9773 -97762 -97763 -97762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -9762 -97761 -97761 -97761 -97762 -97774 -97760 -97761 -97760 -97761 -97760 -97761 -97760 -97761 -97760 -97774 -97774 -97774 -97760 -97774 -97774 -97774 -97774 -97760 -97760 -97760 -97760 -97760 -97760 -97774 -97774 -97774 -97760 -97760 -97760 -97760 -97760 -97760 -97760 -	39999999999999999999999999999999999999	$\begin{array}{c} 53334445513551444883112233333322222222222222222222222$	$\begin{array}{c} 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\$	$\begin{array}{c} 1229\\ 3284\\ -1016\\ -376$	$\begin{array}{c} 4317\\ 4066\\ 33601\\ 4930$	0.000             0.000	MOTO MOTO MOTO MOTO MOTO MOTO MOTO MOTO

run	[su]	[us]	[w]	[Gauss]	ool [deg.]	īt [Hz]	$ u_{\rm fit}  [{\rm Hz}] $	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	[Hz] (	ν0 [Hz]	ts. [%]	ata Type
<pre>2 2229 2229 2229 22231 22332 2233 2233 2</pre>	$ \begin{array}{c} L \\ 3000 \\ 300 $	$\begin{array}{c} \square \\ 1000 $	$\begin{array}{c} \mathbf{A} \\ 74.25\\ 74$	$ \begin{array}{c} \mathbf{g} \\ -4.762$	6           2600 <td>S           10348           10239           10246           10119           10278           10208           10706           10208           10706           10426           104278           10426           10426           10426           10426           104273           10426           10427           10428           10429           10228           10429           10228           10221           10221           10228           10218           10228           10228           10221           10221           10223           10231           102323           102341           10252           102382           10352           10434           10352           10435           10434           10298           10352           10434           10211           102223           10624</td> <td><math display="block">  \begin{tabular}{ c c c c c } \hline \$\nabla\$ \\ \$2779\$ \\ \$2072\$ \\ \$2043\$ \\ \$2480\$ \\ \$2480\$ \\ \$2480\$ \\ \$2480\$ \\ \$255\$ \\ \$1421\$ \\ \$282\$ \\ \$2351\$ \\ \$282\$ \\ \$2256\$ \\ \$2254\$ \\ \$2282\$ \\ \$237\$ \\ \$2282\$ \\ \$2</math></td> <td>□           -9764           -9763           -9764           -9763           -9764           -9763           -9762           -9763           -9763           -9764           -9762           -9763           -9772           -9761           -9772           -9763           -9773           -9773           -9763           -9773           -9763           -9763           -9764           -9763           -9763           -9763           -9763           -9763           -9764           -9763           -9763           -9764           -9763           -9764           -9763           -9764           -9763           -9772           -9763           -9772           -9763           -9772           -9763           -9772           -9773           -9773           -9773           -9773</td> <td></td> <td><math display="block">\frac{\delta_1}{\delta_1} = \frac{\delta_2}{\delta_1} + \frac{\delta_1}{\delta_2} + \frac{\delta_2}{\delta_1} + \frac{\delta_2}{\delta_2} + </math></td> <td><math display="block">\bigtriangledown</math></td> <td><math display="block">\begin{array}{c} \overbrace{S} \\ 69 \\ -40 \\ -34 \\ -34 \\ -17 \\ -34 \\ -279 \\ -70 \\ -34 \\ -279 \\ -70 \\ -28 \\ -279 \\ -70 \\ -28 \\ -279 \\ -279 \\ -70 \\ -28 \\ -336 \\ -152 \\ -279 \\ -279 \\ -270 \\ -28 \\ -336 \\ -28 \\ -38 \\ -35 \\ -26 \\ -28 \\ -38</math></td> <td></td> <td>▶ 0.000</td> <td>CI LLAP LLAP LLAP LLAP LLAP LLAP LLAP LLA</td>	S           10348           10239           10246           10119           10278           10208           10706           10208           10706           10426           104278           10426           10426           10426           10426           104273           10426           10427           10428           10429           10228           10429           10228           10221           10221           10228           10218           10228           10228           10221           10221           10223           10231           102323           102341           10252           102382           10352           10434           10352           10435           10434           10298           10352           10434           10211           102223           10624	$  \begin{tabular}{ c c c c c } \hline $\nabla$ \\ $2779$ \\ $2072$ \\ $2043$ \\ $2480$ \\ $2480$ \\ $2480$ \\ $2480$ \\ $255$ \\ $1421$ \\ $282$ \\ $2351$ \\ $282$ \\ $2256$ \\ $2254$ \\ $2282$ \\ $237$ \\ $2282$ \\ $2$	□           -9764           -9763           -9764           -9763           -9764           -9763           -9762           -9763           -9763           -9764           -9762           -9763           -9772           -9761           -9772           -9763           -9773           -9773           -9763           -9773           -9763           -9763           -9764           -9763           -9763           -9763           -9763           -9763           -9764           -9763           -9763           -9764           -9763           -9764           -9763           -9764           -9763           -9772           -9763           -9772           -9763           -9772           -9763           -9772           -9773           -9773           -9773           -9773		$\frac{\delta_1}{\delta_1} = \frac{\delta_2}{\delta_1} + \frac{\delta_1}{\delta_2} + \frac{\delta_2}{\delta_1} + \frac{\delta_2}{\delta_2} + $	$\bigtriangledown$	$\begin{array}{c} \overbrace{S} \\ 69 \\ -40 \\ -34 \\ -34 \\ -17 \\ -34 \\ -279 \\ -70 \\ -34 \\ -279 \\ -70 \\ -28 \\ -279 \\ -70 \\ -28 \\ -279 \\ -279 \\ -70 \\ -28 \\ -336 \\ -152 \\ -279 \\ -279 \\ -270 \\ -28 \\ -336 \\ -28 \\ -38 \\ -35 \\ -26 \\ -28 \\ -38$		▶ 0.000	CI LLAP LLAP LLAP LLAP LLAP LLAP LLAP LLA

Table A.2 Continued from previous page

$N_{ m run}$	T [ns]	D [ns]	[M]	B [Gauss]	$\theta_{\rm pol}  [{\rm deg.}]$	$   \nu_{\rm fit}  [{\rm Hz}] $	$\Delta \nu_{\rm fit} ~[{\rm Hz}]$	DC <sub>B</sub> [Hz]	$\Delta DC_{B}$ [Hz]	SC [Hz]	ASC [Hz]	ν0 [Hz]	$\Delta \nu_0 \; [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{r} 2324\\ 23226\\ 23228\\ 232328\\ 23320\\ 23322\\ 23332\\ 23332\\ 23332\\ 23334\\ 23356\\ 23372\\ 23342\\ 23342\\ 23344\\ 23346\\ 23342\\ 23342\\ 23342\\ 23342\\ 23355\\ 23556\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23557\\ 23556\\ 23557\\ 23556\\ 23557\\ 23557\\ 23557\\ 23557\\ 23557\\ 23557\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\ 235777\\$	3000 3000	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 74.255\\$	$\begin{array}{c} 4,762\\ 4,762\\ 4,762\\ -4$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 10344\\ 10134\\ 10138\\ 10403\\ 10013\\ 10387\\ 10078\\ 10000\\ 10000\\ 10000\\ 10000\\ 10000\\ 10000\\ 10000\\ 10000\\ 10000\\ 10$	$\begin{array}{c} 199\\ 1893\\ 1799\\ 1845\\ 2556\\ 1556\\ 2559\\ 2787\\ 217\\ 1991\\ 1992\\ 2211\\ 227\\ 2211\\ 227\\ 2211\\ 227\\ 2211\\ 227\\ 2211\\ 227\\ 2231\\ 2217\\ 2233\\ 200\\ 184\\ 227\\ 2331\\ 2217\\ 217\\ 2331\\ 226\\ 227\\ 153\\ 208\\ 2226\\ 227\\ 153\\ 208\\ 2226\\ 227\\ 153\\ 208\\ 2226\\ 227\\ 153\\ 208\\ 2226\\ 227\\ 153\\ 208\\ 2226\\ 227\\ 153\\ 208\\ 226\\ 227\\ 153\\ 208\\ 226\\ 227\\ 227\\ 200\\ 221\\ 199\\ 250\\ 209\\ 251\\ 199\\ 252\\ 200\\ 221\\ 258\\ 239\\ 209\\ 251\\ 199\\ 252\\ 200\\ 221\\ 258\\ 239\\ 209\\ 251\\ 199\\ 255\\ 209\\ 251\\ 199\\ 255\\ 209\\ 251\\ 199\\ 255\\ 209\\ 251\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 255\\ 209\\ 202\\ 255\\ 200\\ 202\\ 202\\ 255\\ 202\\ 202$	$\begin{array}{c} -9773\\ -9773\\ -9773\\ -9773\\ -97762\\ -9762\\ -9762\\ -9762\\ -9762\\ -97762\\ -97762\\ -97762\\ -9774\\ -9776\\ -9760\\ -9760\\ -9761\\ -9760\\ -9760\\ -9760\\ -9775\\ -9776\\ -9776\\ -9775\\ -9776\\ -9760$	\$	$\begin{array}{c} 514\\ 5513\\ 5514\\ 443\\ 5514\\ 444\\ 5514\\ 5514\\ 5514\\ 444\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5514\\ 5513\\ 551$	$\begin{array}{c} 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\ 12\\$	$\begin{array}{c} 593\\ -148\\ 1322\\ -262\\ 1133\\ -3069\\ -320\\ -264\\ 1392\\ -266\\ -320\\ -264\\ -252\\ -275\\ -320\\ -279\\ -244\\ -252\\ -275\\ -320\\ -275\\ -275\\ -320\\ -275\\ -275\\ -320\\ -275\\ -320\\ -275\\ -320\\ -275\\ -275\\ -320\\ -275\\$	$\begin{array}{c} 199\\ 1840\\ 1856\\ 1559\\ 278\\ 2002\\ 2222\\ 2222\\ 2228\\ 2112\\ 1961\\ 1228\\ 2212\\ 2222\\ 2222\\ 2228\\ 2112\\ 1961\\ 1228\\ 2217\\ 1961\\ 1228\\ 2217\\ 2178\\ 2217\\ 2178\\ 2266\\ 2268\\ 2266\\ 2268\\ 2268\\ 2268\\ 2268\\ 2268\\ 2268\\ 2268\\ 2268\\ 2259\\ 2251\\ 1954\\ 2259\\ 2$	$egin{aligned} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 $	LLAP LLAP LLAAP

Table A.2 Continued from previous page

Vrun	r [ns]	[su] 0	[M]	B [Gauss]	) <sub>pol</sub> [deg.]	∕fit [Hz]	$\Delta \nu_{\rm fit}  [{ m Hz}]$	OC <sub>B</sub> [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	∆SC [Hz]	<sup>0</sup> [Hz]	$\Delta \nu_0  [{ m Hz}]$	vts. [%]	Oata Type
$\begin{array}{l} 2419\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2422\\ 2433\\ 2433\\ 2433\\ 2433\\ 2433\\ 2433\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2442\\ 2445\\$	3000 3000	$\begin{array}{c} 1000\\$	$\begin{array}{c} 2525\\ 7.4,225\\$	$\begin{array}{c} -4,762\\ -4,762\\ +4,762\\ +4,762\\ -4,762\\ -4,762\\ +4,762\\$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 10519\\ 10294\\ 10425\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 10452\\ 1051\\ 105$	$\begin{array}{c} 331\\ 2321\\ 2464\\ 2976\\ 1242\\ 2977\\ 655\\ 565\\ 5770\\ 2238\\ 466\\ 588\\ 57770\\ 55126\\ 446\\ 33956\\ 00\\ 33750\\ 33956\\ 00\\ 33750\\ 33956\\ 00\\ 33750\\ 33956\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 33750\\ 00\\ 00\\ 00\\ 00\\ 00\\ 00\\ 00\\ 00\\ 00\\ $	-9761 -9774 -9774 -9774 -9774 -97762 -97762 -97762 -97762 -97774 -97773 -97762 -9762 -9762 -9763 -97763 -97763 -97763 -97763 -97763 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97762 -9762 -9762 -9762 -97762 -97763 -97773	\$	$\begin{array}{c} 22222222222222234444444444444444444444$	$\begin{array}{c} 1222222222222222222222222222222222222$	$\begin{array}{c} 2462\\ 2139\\ 1765\\ 1780\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -108\\ -3940\\ -201\\ -202$	$\begin{array}{c} 332\\ 2507\\ 2382\\ 2475\\ 22986\\ 657\\ 4586\\ 661\\ 5781\\ 2298\\ 661\\ 5781\\ 2322\\ 2939\\ 657\\ 4586\\ 661\\ 5781\\ 2229\\ 3956\\ 661\\ 5781\\ 2322\\ 2939\\ 661\\ 5781\\ 2323\\ 433956\\ 661\\ 8437\\ 5516\\ 7781\\ 23333\\ 4433\\ 5102\\ 2426\\ 4433\\ 3335\\ 4062\\ 2333\\ 3355\\ 4062\\ 235\\ 2426\\ 4022\\ 2222\\ 235\\ 235\\ 235\\ 235\\ 235\\ 235\\ $	0.000 0	LLAP LLAP LLAP LLAP LLAP LLAP LLAP LLAP

Table A.2 Continued from previous page

un	[su]	[su]	[m]	[Gauss]	ol [deg.]	t [Hz]	'fit [Hz]	<sup>3</sup> B [Hz]	OC <sub>B</sub> [Hz]	[Hz]	5C [Hz]	[Hz]	<sup>0</sup> [Hz]	s. [%]	ta Type
N	Ь	P	٩,	B	$\theta_{\rm pc}$	ΗŻ	$\Delta_{L}$	ğ	ΔI	SC	Δ.	ν <sub>0</sub>	$\Delta_{\nu}$	wt	Da
$\begin{array}{l} 25518\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 255222\\ 2552222\\ 2552222\\ 25522222222$	3000         3000           3000 <td>1000           1000</td> <td><math display="block">\begin{array}{c} 74.255\\</math></td> <td><math display="block">\begin{array}{c} + 762 \\ - 4.762 \\ -</math></td> <td><math display="block">\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\</math></td> <td><math display="block">\begin{array}{l} 9987\\ 9987\\ 9987\\ 9987\\ 9980\\ 10080\\ 10275\\ 11275\\ 10172\\ 9733\\ 10321\\ 10172\\ 10172\\ 10172\\ 10172\\ 10172\\ 10236\\ 10077\\ 10236\\ 1077\\ 10236\\ 1077\\ 10331\\ 10707\\ 10362\\ 1077\\ 10362\\ 10362\\ 1037\\ 10362\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10162\\ 1037\\ 10162\\ 1037\\ 10162\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1047\\ 10162\\ 10371\\ 1047\\ 10172\\ 1048\\ 10272\\ 1047\\ 1024\\ 10272\\ 10072\\ 10264\\ 10238\\ 10224\\ 11277\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10378\\ 10326\\ 103</math></td> <td><math display="block">\begin{array}{c} 2908\\ 4936\\ 4484\\ 4569\\ 3362\\ 225\\ 55602\\ 5362\\ 4483\\ 3492\\ 432\\ 4432\\ 4525\\ 55602\\ 5422\\ 007\\ 113\\ 2882\\ 5422\\ 007\\ 5417\\ 3288\\ 5422\\ 4433\\ 4919\\ 4334\\ 4919\\ 5422\\ 4432\\ 555\\ 502\\ 5422\\ 007\\ 5417\\ 3288\\ 544\\ 495\\ 532\\ 445\\ 524\\ 495\\ 3376\\ 638\\ 3376\\ 514\\ 3386\\ 514\\ 777\\ 96\\ 562\\ 562\\ 562\\ 562\\ 562\\ 562\\ 562\\ 56</math></td> <td>-9773 -97762 -9761 -9761 -9761 -9761 -9761 -97761 -9777 -97773 -97773 -97774 -97761 -9760 -9761 -9760 -9761 -9760 -9761 -9760 -97761 -9760 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97771 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97774 -97773 -97</td> <td></td> <td><math display="block">\begin{array}{c} 514\\ 514\\ 514\\ 514\\ 514\\ 512\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513</math></td> <td><math display="block">\begin{smallmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 </math></td> <td><math display="block">\begin{array}{c} -269\\ -299\\ -397\\ -196\\ 999\\ -480\\ -568\\ -114\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -295\\ -382\\ -125\\ 278\\ -897\\ -410\\ -295\\ -236\\ -331\\ -305\\ -295\\ -266\\ -331\\ -305\\ -295\\ -338\\ -338\\ -338\\ -338\\ -338\\ -338\\ -336\\ -338\\ -336\\ -316\\ -382\\ -338\\ -336\\ -316\\ -382\\ -338\\ -336\\ -</math></td> <td><math display="block">\begin{array}{c} 2918\\ 2914\\ 4937\\ 4484\\ 5603\\ 3622\\ 24433\\ 456\\ 6035\\ 3622\\ 24433\\ 455\\ 503\\ 3622\\ 24433\\ 455\\ 503\\ 362\\ 225\\ 4433\\ 455\\ 503\\ 514\\ 492\\ 91\\ 2883\\ 342\\ 524\\ 455\\ 501\\ 332\\ 876\\ 670\\ 21\\ 2883\\ 3287\\ 670\\ 670\\ 670\\ 672\\ 682\\ 155\\ 773\\ 6670\\ 670\\ 670\\ 682\\ 155\\ 773\\ 6670\\ 721\\ 883\\ 3860\\ 88</math></td> <td></td> <td>IPPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRP</td>	1000           1000	$\begin{array}{c} 74.255\\$	$\begin{array}{c} + 762 \\ - 4.762 \\ -$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{l} 9987\\ 9987\\ 9987\\ 9987\\ 9980\\ 10080\\ 10275\\ 11275\\ 10172\\ 9733\\ 10321\\ 10172\\ 10172\\ 10172\\ 10172\\ 10172\\ 10236\\ 10077\\ 10236\\ 1077\\ 10236\\ 1077\\ 10331\\ 10707\\ 10362\\ 1077\\ 10362\\ 10362\\ 1037\\ 10362\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 1037\\ 10362\\ 1037\\ 10362\\ 1037\\ 10162\\ 1037\\ 10162\\ 1037\\ 10162\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 10625\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1062\\ 10371\\ 1047\\ 10162\\ 10371\\ 1047\\ 10172\\ 1048\\ 10272\\ 1047\\ 1024\\ 10272\\ 10072\\ 10264\\ 10238\\ 10224\\ 11277\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 11178\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10326\\ 10378\\ 10326\\ 103$	$\begin{array}{c} 2908\\ 4936\\ 4484\\ 4569\\ 3362\\ 225\\ 55602\\ 5362\\ 4483\\ 3492\\ 432\\ 4432\\ 4525\\ 55602\\ 5422\\ 007\\ 113\\ 2882\\ 5422\\ 007\\ 5417\\ 3288\\ 5422\\ 4433\\ 4919\\ 4334\\ 4919\\ 5422\\ 4432\\ 555\\ 502\\ 5422\\ 007\\ 5417\\ 3288\\ 544\\ 495\\ 532\\ 445\\ 524\\ 495\\ 3376\\ 638\\ 3376\\ 514\\ 3386\\ 514\\ 777\\ 96\\ 562\\ 562\\ 562\\ 562\\ 562\\ 562\\ 562\\ 56$	-9773 -97762 -9761 -9761 -9761 -9761 -9761 -97761 -9777 -97773 -97773 -97774 -97761 -9760 -9761 -9760 -9761 -9760 -9761 -9760 -97761 -9760 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97761 -97771 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97774 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97773 -97774 -97773 -97		$\begin{array}{c} 514\\ 514\\ 514\\ 514\\ 514\\ 512\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513\\ 513$	$\begin{smallmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 $	$\begin{array}{c} -269\\ -299\\ -397\\ -196\\ 999\\ -480\\ -568\\ -114\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -294\\ -567\\ -295\\ -382\\ -125\\ 278\\ -897\\ -410\\ -295\\ -236\\ -331\\ -305\\ -295\\ -266\\ -331\\ -305\\ -295\\ -338\\ -338\\ -338\\ -338\\ -338\\ -338\\ -336\\ -338\\ -336\\ -316\\ -382\\ -338\\ -336\\ -316\\ -382\\ -338\\ -336\\ -$	$\begin{array}{c} 2918\\ 2914\\ 4937\\ 4484\\ 5603\\ 3622\\ 24433\\ 456\\ 6035\\ 3622\\ 24433\\ 455\\ 503\\ 3622\\ 24433\\ 455\\ 503\\ 362\\ 225\\ 4433\\ 455\\ 503\\ 514\\ 492\\ 91\\ 2883\\ 342\\ 524\\ 455\\ 501\\ 332\\ 876\\ 670\\ 21\\ 2883\\ 3287\\ 670\\ 670\\ 670\\ 672\\ 682\\ 155\\ 773\\ 6670\\ 670\\ 670\\ 682\\ 155\\ 773\\ 6670\\ 721\\ 883\\ 3860\\ 88$		IPPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRPRP

Table A.2 Continued from previous page

run	[us]	[ns]	[m]	[Gauss]	ol [deg.]	it [Hz]	$ u_{\rm fit}  [{\rm Hz}] $	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	[Hz]	SC [Hz]	[Hz]	$\nu_0 ~[{ m Hz}]$	ts. [%]	ata Type
$\underset{\mathcal{N}}{\overset{\mathrm{uni}}{\underset{\mathcal{N}}{2}}} \left( \begin{array}{c} 26156\\ 26117\\ 262112\\ 26623\\ 26623\\ 26624\\ 26625\\ 26627\\ 26623\\ 266334\\ 26635\\ 26637\\ 26633\\ 26636\\ 26637\\ 26644\\ 26646\\ 26646\\ 26646\\ 26645\\ 26556\\ 26567\\ 26566\\ 2656$	[st]         J           3000         3000           3000	$\begin{bmatrix} 3 \\ 8 \\ -3 \\ -3 \\ -3 \\ -3 \\ -3 \\ -3 \\ -$	$ \begin{bmatrix} M \end{bmatrix} q \\ 74.255 \\$	$ \begin{bmatrix} s \\ s \\ r \\ r \\ s \\ r \\ r \\ s \\ r \\ r \\$	$\begin{bmatrix} \exists e_p \end{bmatrix} & \log_{\theta} \\ 2660 & 2$	FE           10182           100182           10211           10334           10182           10247           10263           10339           10231           10339           10231           10339           10231           10339           102253           102301           103125           102253           102241           10247           102241           10247           102241           10247           102241           10247           1	$[{\rm ^{2}H}] ~{\rm ^{19}A}\nabla ~~ \\ 627 ~~ 603 ~~ 900 ~~ 8647 ~~ 300 ~~ 556 ~~ 556 ~~ 577 ~~ 567 ~~ 627 ~~ 866 ~~ 502 ~~ 356 ~~ 107 ~~ 128 ~~ 878 ~~ 597 ~~ 627 ~~ 666 ~~ 662 ~~ 295 ~~ 666 ~~ 66 ~~ 666 ~~ 66 ~~~ 66 ~~ 666 ~~ 666 ~~ 666 ~~ 666 ~~ 66 ~~~$	[14] 9770 97764 9764 9764 9764 9764 9765 9765 9765 9765 9765 9765 9764 9764 9764 9764 9764 9764 9764 9764 9764 9763 97763 97764 97764 97763 97769 97770 97770 97770 97770 97770 97770 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97764 97770 97770 97772	$\Delta DC_{B} \left[ Hz \right]$	$ \begin{bmatrix} \mathbf{x} \mathbf{H} \end{bmatrix} \\ \begin{array}{c} \mathbf{OS} \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5223 \\ 5223 \\ 5223 \\ 5223 \\ 5223 \\ 5223 \\ 5223 \\ 5223 \\ 5224 \\ 5223 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5224 \\ 5223 \\ 523 \\ 523 \\ 523 \\ 523 \\ 52$	ZRU [Hz] 230 [133333333333333333333333333333333333	$ \begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \begin{smallmatrix} 0_{\mathcal{H}} \\ -1116 \\ -464 \\ -1220 \\ -201 \\ -226 \\ -370 \\ -122 \\ -370 \\ -226 \\ -1460 \\ -1460 \\ -1420 \\ -226 \\ -1460 \\ -1420 \\ -226 \\ -388 \\ -388 \\ -388 \\ -388 \\ -388 \\ -388 \\ -479 \\ -226 \\ -120 \\ -226 \\ -316 \\ -845 \\ -120 \\ -120 \\ -29 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -150 \\ -109 \\ -764 \\ -109 \\ -764 \\ -109 \\ -764 \\ -109 \\ -109 \\ -764 \\ -100 \\ -764 \\ -100 \\ -764 $	$ \begin{bmatrix} \mathbf{z} \mathbf{H} \end{bmatrix} \begin{smallmatrix} 0_{4} \nabla \\ 65222 \\ 5522 \\ 55625 \\ $	0000         0000 <td< td=""><td>Det TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT</td></td<>	Det TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT
$\begin{array}{r} 20099\\ 26701\\ 26771\\ 26773\\ 26774\\ 26775\\ 26775\\ 26776\\ 26778\\ 26776\\ 26780\\ 26880\\ 26882\\ 26884\\ 26885\\ 26886\\ 26890\\ 26901\\ 2692\\ 2693\\ 26994\\ 2692\\ 26994\\ 27001\\ 27003\\ 27004\\ 27005\\ 27005\\ 27007\\ 27005\\ 27007\\ 27009\\ 27101\\ 27112\\ 27112\\ 27122\\ 27122\\ 27122\\ 27032\\ 27009\\ 27101\\ 27112\\ 27122\\ 27032\\ 27009\\ 27110\\ 27112\\ 27122$	300         300           300         300	$\begin{array}{c} 1000\\$	$\substack{(4,25)\\74,25\\74,25}\\74,25\\$	$\begin{array}{r} 4, 762\\$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{c} 10340\\ 10310\\ 10310\\ 10330\\ 10330\\ 10332\\ 10332\\ 10332\\ 10332\\ 10280\\ 10280\\ 10280\\ 10293\\ 10280\\ 10293\\ 10293\\ 10293\\ 10293\\ 10238\\ 10264\\ 10320\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10370\\ 10298\\ 10286\\ 10$	$\substack{45\\7768}{666630}\\25555711\\666653255766255573\\8069913\\8329790\\87377879\\894\\805\\82297$	-9772 -9772 -9772 -9772 -9772 -9771 -9771 -9771 -9772	**************************************	$\begin{array}{c} 523\\ 523\\ 523\\ 523\\ 523\\ 523\\ 523\\ 523\\$	$\begin{smallmatrix} 133\\133\\133\\133\\133\\133\\133\\133\\133\\133$	$\begin{smallmatrix}&44\\15\\108\\8\\68\\43\\-119\\0\\-22\\39\\-58\\39\\-164\\5\\-33\\9\\-164\\-100\\918\\-107\\-167\\-103\\-107\\-103\\-107\\-103\\-91\\-103\\-103\\-103\\-103\\-103\\-103\\-103\\-10$	$\substack{\substack{472\\7720}\\767}, \substack{767\\651}\\767, \substack{767\\654}\\655, \substack{565\\573}\\664, \substack{100\\5743}\\10934\\8854\\881\\881\\881\\881\\882\\784\\881\\881\\882\\784\\881\\882\\882\\784\\881\\882\\882\\784\\881\\882\\882\\882\\882\\882\\882\\882\\882\\882$	0.000 0	F DET FDET FDET FDET FDET FDET FDET FDET F

c	[2]	[2]	~	auss]	[deg.]	[Hz]	t [Hz]	3 [Hz]	<sup>℃</sup> B [Hz]	[zH	[Hz]	Hz]	[Hz]	[%]	1 Type
$N_{ m ru}$	T [n	D [r	P [\	B [C	$\theta_{\mathrm{pol}}$	μĥt	$\Delta \nu_{ m ff}$	DCI	ΔDo	SC	ΔSC	.] 0 <sub>1</sub>	$\Delta \nu_0$	wts.	Data
$\begin{array}{c} 27134\\ 27715\\ 27717\\ 27715\\ 27717\\ 27717\\ 277120\\ 27722\\ 27722\\ 27722\\ 27722\\ 27722\\ 27722\\ 27722\\ 27722\\ 27733\\ 22733\\ 27733\\ 2$	300         300           300	$\begin{array}{c} 1000\\$	$\begin{array}{c} (4.25)\\ (4.25)\\ (7.$	$\begin{array}{c} -4, 762\\ -4, 7$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{l} 10265\\ 10024\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100264\\ 100265\\ 100251\\ 100253\\ 1$	$\begin{array}{c} 949\\ 949\\ 949\\ 1071\\ 766\\ 8064\\ 876\\ 776\\ 876\\ 775\\ 876\\ 775\\ 876\\ 775\\ 876\\ 775\\ 877\\ 768\\ 877\\ 758\\ 877\\ 688\\ 777\\ 988\\ 776\\ 887\\ 762\\ 887\\ 762\\ 887\\ 762\\ 887\\ 762\\ 887\\ 762\\ 887\\ 762\\ 887\\ 762\\ 888\\ 944\\ 887\\ 894\\ 887\\ 894\\ 887\\ 897\\ 910\\ 1574\\ 197\\ 952\\ 887\\ 940\\ 1032\\ 996\\ 1032\\ 996\\ 1032\\ 996\\ 1032\\ 1393\\ 1301\\ 116\\ 116\\ 116\\ 116\\ 116\\ 116\\ 116\\ 1$	-9763 -9763 -9763 -9763 -9762 -9761 -9763 -9762 -9762 -9762 -9762 -9762 -9763 -9763 -9763 -9763 -9763 -9763 -9763 -97763 -97762 -97772 -97763 -9763 -9763 -9763 -9763 -9763 -9763 -9763 -9763 -9763 -97772 -97772 -9	$\frac{1}{2}$	$\begin{array}{l} 5255\\ 5225\\ 5224\\ 5225\\$	133333333333333333333333333333333333333	$\begin{array}{c} -263\\$	$\begin{array}{c} 950\\ 950\\ 600\\ 1008\\ 877\\ 762\\ 898\\ 859\\ 977\\ 888\\ 877\\ 788\\ 887\\ 778\\ 806\\ 877\\ 788\\ 887\\ 778\\ 806\\ 877\\ 788\\ 877\\ 788\\ 877\\ 788\\ 877\\ 788\\ 877\\ 788\\ 877\\ 788\\ 877\\ 806\\ 877\\ 670\\ 767\\ 881\\ 956\\ 675\\ 114\\ 1966\\ 896\\ 875\\ 191\\ 906\\ 896\\ 875\\ 191\\ 906\\ 896\\ 875\\ 191\\ 996\\ 101\\ 157\\ 496\\ 298\\ 101\\ 198\\ 888\\ 941\\ 1042\\ 1042\\ 101\\ 111\\ 111\\ 111\\ 111\\ 111\\ 111\\ 11$	$0.000 \\ 0.00$	FDEETFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF

Table A.2 Continued from previous page

un	[su]	[ns]	[w]	[Gauss]	ol [deg.]	t [Hz]	v <sub>fit</sub> [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	[Hz]	SC [Hz]	[Hz]	04 [Hz]	s. [%]	ata Type
2811	H 300	۹ 100	۵ <u>م</u> 37.5	-4.762	م ص 260	ی 10108	<ul><li></li><li></li><li></li><li>136</li></ul>	-9764	9.8	244	₹ 6	ຼິ 100	137	<u>ک</u> 0.00	<u> </u>
$\begin{array}{l} 28123\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2814\\ 2825\\ 2825$	300         300           300	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 3,7,5,5,5,5,5,5,5,5,5,5,5,5,5,5,5,5,5,5,$	$\begin{array}{c} -4,762\\$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	$\begin{array}{l} 9927\\ 9928\\ 9028\\$	$\begin{array}{c} 1246\\ 1160\\ 1166\\ 1160\\ 116\\ 116\\ 123\\ 133\\ 1567\\ 171\\ 115\\ 1221\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 125\\ 121\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	-9762 -9762 -9763 -9762 -9763 -9762 -9763 -9763 -9763 -97763 -97762 -97762 -97762 -97762 -97762 -97762 -97762 -97772 -97771 -97771 -97771 -97771 -97771 -97771 -97772 -97771 -97772 -97773 -97773 -97763 -97763 -97763 -97763 -97763 -97763 -97763 -97763 -97763 -97763 -97771 -977	$\frac{1}{2}$	$\begin{array}{l} 2443\\ 2443\\ 2443\\ 2443\\ 2443\\ 2442\\ 2443\\ 22442\\ 2442\\ 224442\\ 22442\\ 22442\\ 22442\\ 22442\\ 22442\\ 22442\\ 22442\\ 22442\\ 22$	666666666666666666666666666666666666	$\begin{array}{c} -78\\ -78\\ -78\\ -78\\ -78\\ -78\\ -78\\ -78\\$	$\begin{array}{c} 1247\\ 1101\\ 1111\\ 1164\\ 1354\\ 1597\\ 1781\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1175\\ 1226\\ 1216\\ 1175\\ 1226\\ 1216\\ 1175\\ 1226\\ 1216\\ 1216\\ 1226\\ 1216\\ 1216\\ 1226\\ 1216\\$	$\begin{array}{c} 0.00\\$	SPARAPARAPARAPARAPARAPARAPARAPARAPARAPAR

Table A.2 Continued from previous page

Irun	, [ns]	[su] (	[M]	[Gauss]	pol [deg.]	fit [Hz]	νν <sub>fit</sub> [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	0 [Hz]	170 [Hz]	ts. [%]	ata Type
$\begin{array}{c} & & \\$	300           300      300	$\begin{array}{c} 3\\ 1000\\ 10$	$\begin{array}{c} 37.5\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 37.5\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 37.5\\$	$\begin{array}{c} -4, 762\\ -4, 7$	$\begin{array}{c} \mathbf{C} \\ 260 $	2 9673 99674 9834 10177 10104 10206 10155 10155 1004 10206 10155 10055 9845 9845 9845 9845 9845 9845 9845 98	$\begin{array}{c} 3 \\ 136 \\ 117 \\ 168 \\ 120 \\ 164 \\ 945 \\ 977 \\ 80 \\ 78$		7 9.888 9.9.588 9.	$\begin{array}{c} & & \\$	7 = 66666666666666666666666666666666666	$\begin{array}{c} -& -& -& -& -& -& -& -& -& -& -& -& -& $	$\begin{array}{c} 3 \\ 136 \\ 117 \\ 160 \\ 117 \\ 160 \\ 197 \\ 120 \\ 100 \\ 1$	$\begin{array}{c} & & \\ & 0.000 \\ & 0$	LUBBP LUBBP LUBBP AND

Table A.2 Continued from previous page

run	[ns]	[us]	[w]	[Gauss]	ol [deg.]	<sub>it</sub> [Hz]	$ u_{\rm fit}  [{\rm Hz}] $	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	[Hz] (	$ u_0  [\mathrm{Hz}] $	ts. [%]	ata Type
$\begin{array}{c} \underset{N}{\underset{N}{1}} \\ 3007 \\ 3008 \\ 3010 \\ 30112 \\ 3014 \\ 3016 \\ 3016 \\ 3017 \\ 3018 \\ 3020 \\ 3022 \\ 3023 \\ 3024 \\ 3022 \\ 3025 \\ 3055 \\$	[s]         L           3000         3000           3000	$\begin{bmatrix} \mathrm{sti} \end{bmatrix} Q$	$ \begin{bmatrix} M \end{bmatrix}_{\mathcal{A}} \\ \begin{array}{c} 337,555,555,555,555,555,555,555,555,555,$	$ \begin{bmatrix} g \\ g$	$ \begin{bmatrix} 1 \\ 3 \\ 0 \\ 0 \\ 2 \\ 2 \\ 6 \\ 6 \\ 0 \\ 2 \\ 2 \\ 6 \\ 6 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0$	$ \begin{bmatrix} \mathbf{x} \mathbf{H} \\ \mathbf{y} \\$	$ \begin{smallmatrix} \mathbf{\bar{r}} \mathbf{H} \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 4 \\ \mathbf{\nabla} \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ $	<ul> <li>[X]H</li> <li><sup>II</sup> O O</li> <li><sup>II</sup> O</li> <li< td=""><td>verseseseseseseseseseseseseseseseseseses</td><td><math display="block"> \begin{bmatrix} \mathbf{x} \mathbf{H} \end{bmatrix} \mathbf{OS} \\ \begin{array}{c} 255332255122500\\ 2253322551222500\\ 22532225222222222222222222222222222222</math></td><td>[ZH]         OSO           666666666666666666666666666666666666</td><td><math display="block"> \begin{bmatrix} \mathbf{R} \mathbf{H} \end{bmatrix} <b>0</b> \mathbf{Z} \\ \begin{array}{c} -104 \\ -3405 \\ -1794 \\ -262 \\ -1120 \\ -878 \\ -264 \\ -22238 \\ -2238 \\ -2238 \\ -2338 \\ </math></td><td><math display="block"> \begin{bmatrix} \mathbf{\bar{z}} \mathbf{H} \end{bmatrix}_{0 \land \nabla} \\ \begin{bmatrix} <b>0</b> \land \nabla \\ 1085 \\ 1095 \\ 1090 \\ 1000 \\ 1</math></td><td>Mathematical         Mathematical         Mathematical&lt;</td><td>аттататататататататататататататататата</td></li<></ul>	verseseseseseseseseseseseseseseseseseses	$ \begin{bmatrix} \mathbf{x} \mathbf{H} \end{bmatrix} \mathbf{OS} \\ \begin{array}{c} 255332255122500\\ 2253322551222500\\ 22532225222222222222222222222222222222$	[ZH]         OSO           666666666666666666666666666666666666	$ \begin{bmatrix} \mathbf{R} \mathbf{H} \end{bmatrix} 0 \mathbf{Z} \\ \begin{array}{c} -104 \\ -3405 \\ -1794 \\ -262 \\ -1120 \\ -878 \\ -264 \\ -22238 \\ -2238 \\ -2238 \\ -2338 \\ $	$ \begin{bmatrix} \mathbf{\bar{z}} \mathbf{H} \end{bmatrix}_{0 \land \nabla} \\ \begin{bmatrix} 0 \land \nabla \\ 1085 \\ 1095 \\ 1090 \\ 1000 \\ 1$	Mathematical         Mathematical<	аттататататататататататататататататата
3104	300	100	37.5	-4.762	260	9942	125	-9764	9.8	244	6	-66	126	0.00	LLBP

Table A.2 Continued from previous page

run	[us]	[ns]	[m]	[Gauss]	ool [deg.]	ft [Hz]	ν <sub>fit</sub> [Hz]	C <sub>B</sub> [Hz]	DC <sub>B</sub> [Hz]	C [Hz]	SC [Hz]	[Hz] (	[Hz] 04	ts. [%]	ata Type
$\begin{array}{c} 3105\\ 3106\\ 3107\\ 3108\\ 31107\\ 3108\\ 31107\\ 3112\\ 311$	300 300 300 300 300 300 300 300 300 300	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 37.5\\$	$\begin{array}{c} -4.762\\$	$\begin{array}{c} 2 \\ 2 \\ 6 \\ 2 \\ 6 \\ 6 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 2 \\ 6 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0$	$\begin{array}{c} 9943\\ 9794\\ 9794\\ 10022\\ 10013\\ 10027\\ 1007\\ 10$	$\begin{array}{c} 113\\141\\142\\151\\161\\161\\161\\161\\161\\161\\161\\161\\161$	-9764 -9765 -9764 -9764 -9764 -9764 -9764 -9764 -97764 -97764 -97764 -97771 -97771 -97772 -97772 -97772 -97772 -97770 -97763 -9763 -9763 -9763 -97763 -97763 -97763 -97763 -97763 -97772 -97763 -9763	$\begin{array}{c} 0.88\\ 9.88\\ 9.88\\ 9.88\\ 9.88\\ 9.88\\ 8.88\\$	$\begin{array}{c} 244\\ 2445\\ 2446\\ 2447\\ 2448\\ 247\\ 2489\\ 517\\ 5212\\ 2522\\ 2532\\ 2532\\ 2532\\ 2532\\ 2533\\ 2525\\ 5225\\ 2253\\ 22$	$\begin{smallmatrix} 6 & 6 & 6 & 6 & 6 & 6 & 6 & 6 & 6 & 6 $	$\begin{array}{c} -65\\ -215\\ -215\\ -215\\ -215\\ -215\\ -215\\ -215\\ -215\\ -216\\ -182\\ -2179\\ -252\\ -279\\ -2282\\ -279\\ -2282\\ -279\\ -2282\\ -279\\ -2282\\ -279\\ -2282\\ -279\\ -2282\\ -279\\ -2282\\ -$	$\begin{array}{c} 113\\ 141\\ 152\\ 101\\ 128\\ 86\\ 1092\\ 1365\\ 1015\\ 1166\\ 128\\ 876\\ 1092\\ 1365\\ 1012\\ 128\\ 876\\ 1092\\ 1365\\ 1012\\ 1252\\ 1393\\ 101\\ 1365\\ 1364\\ 1425\\ 1392\\ 1365\\ 1364\\ 1425\\ 1392\\ 1365\\ 1010\\ 108\\ 869\\ 978\\ 869\\ 978\\ 869\\ 978\\ 869\\ 978\\ 1066\\ 1098\\ 869\\ 978\\ 1066\\ 1098\\ 869\\ 978\\ 1066\\ 1098\\ 869\\ 978\\ 1066\\ 1098\\ 869\\ 978\\ 1066\\ 1008\\ 869\\ 978\\ 1066\\ 1008\\ 1008\\ 1006\\ 1008\\ 1008\\ 1006\\ 1008\\ $	$\begin{array}{c} 0.00\\$	

Table A.2 Continued from previous page

$N_{ m run}$	$T \; [\mathrm{ns}]$	D [ns]	P [W]	B [Gauss]	$\theta_{ m pol}~[{ m deg.}]$	$ u_{ m fit}$ [Hz]	$\Delta \nu_{\rm fit}   [{ m Hz}]$	DC <sub>B</sub> [Hz]	ΔDC <sub>B</sub> [Hz]	SC [Hz]	$\Delta SC [Hz]$	ν0 [Hz]	$\Delta \nu_0 \; [{ m Hz}]$	wts. [%]	Data Type
$\begin{array}{c} 3203\\ 3204\\ 3205\\ 3206\\ 3207\\ 3208\\ 3207\\ 3209\\ 3210\\ 3211\\ 3212\\ 3213\\ 3214\\ 3215\\ 3216\\ 3226\\ 3221\\ 3222\\ 32221\\ 3222\\ 32223\\ 3224\\ 32223\\ 3224\\ 3223\\ 3234\\ 3235\\ 3234\\ 3235\\ 3234\\ 3236\\ 3236\\ 3237\\ 3234\\ 3236\\ 3237\\ 3234\\ 3236\\ 3236\\ 3237\\ 3236\\ 3246\\ 3246\\ 3246\\ 3243\\ 32$	$\begin{array}{c} 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300\\ 300$	$\begin{array}{c} 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100$	$\begin{array}{c} 37.5\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 74.25\\ 37.5\\$	$\begin{array}{c} -4.762\\$	$\begin{array}{c} 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\ 260\\$	9871 10281 10306 10220 10111 10233 10173 10122 10250 10220 10220 10220 10220 10220 10220 10220 10230 10247 10291 10270 10240 10247 10291 10270 10240 10247 10270 10240 10240 10270 10240 10270 10240 10247 10250 10240 10247 10250 10240 10247 10250 10240 10247 10250 10240 10247 10250 10240 10250 10247 10250 10247 10250 10240 10250 10247 10250 10270 10000 10000 10000 10000000000	$\begin{array}{c} 151\\ 103\\ 90\\ 99\\ 99\\ 117\\ 99\\ 99\\ 107\\ 104\\ 109\\ 107\\ 108\\ 109\\ 107\\ 108\\ 109\\ 108\\ 109\\ 108\\ 109\\ 108\\ 109\\ 108\\ 109\\ 108\\ 108\\ 109\\ 108\\ 108\\ 109\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108\\ 108$	-9763 -97763 -97771 -9771 -9771	9.8 9.8 9.8 9.8 9.8 9.8 9.8 9.8 9.8 9.8	253 5120 520 521 522 523 523 523 523 523 523 523 523 523	$\begin{smallmatrix} 6\\ 12\\ 12\\ 13\\ 13\\ 13\\ 13\\ 13\\ 13\\ 13\\ 13\\ 13\\ 13$	$\begin{array}{c} -145\\ -11\\ 23\\ -64\\ -173\\ -69\\ -52\\ -111\\ -121\\ -366\\ -839\\ -36\\ -839\\ -180\\ -180\\ -180\\ -180\\ -107\\ -455\\ -210\\ -107\\ -288\\ -172\\ -2316\\ -151\\ -120\\ -2316\\ -151\\ -120\\ -2316\\ -357\\ -357\\ -54\\ -142\\ -128\\ -128\\ -128\\ -128\\ -128\\ -112$	$\begin{array}{c} 151\\ 105\\ 91\\ 95\\ 91\\ 100\\ 1106\\ 100\\ 100\\ 100\\ 100\\ 100\\ 1$	$\begin{array}{c} 0.00\\$	LLBP LLBP LLBP LLBP LLBP LLBP LLBP LLBP
	End of Table														

Table A.2 Continued from previous page